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LOGARITHMIC
REDUCTION TABLES
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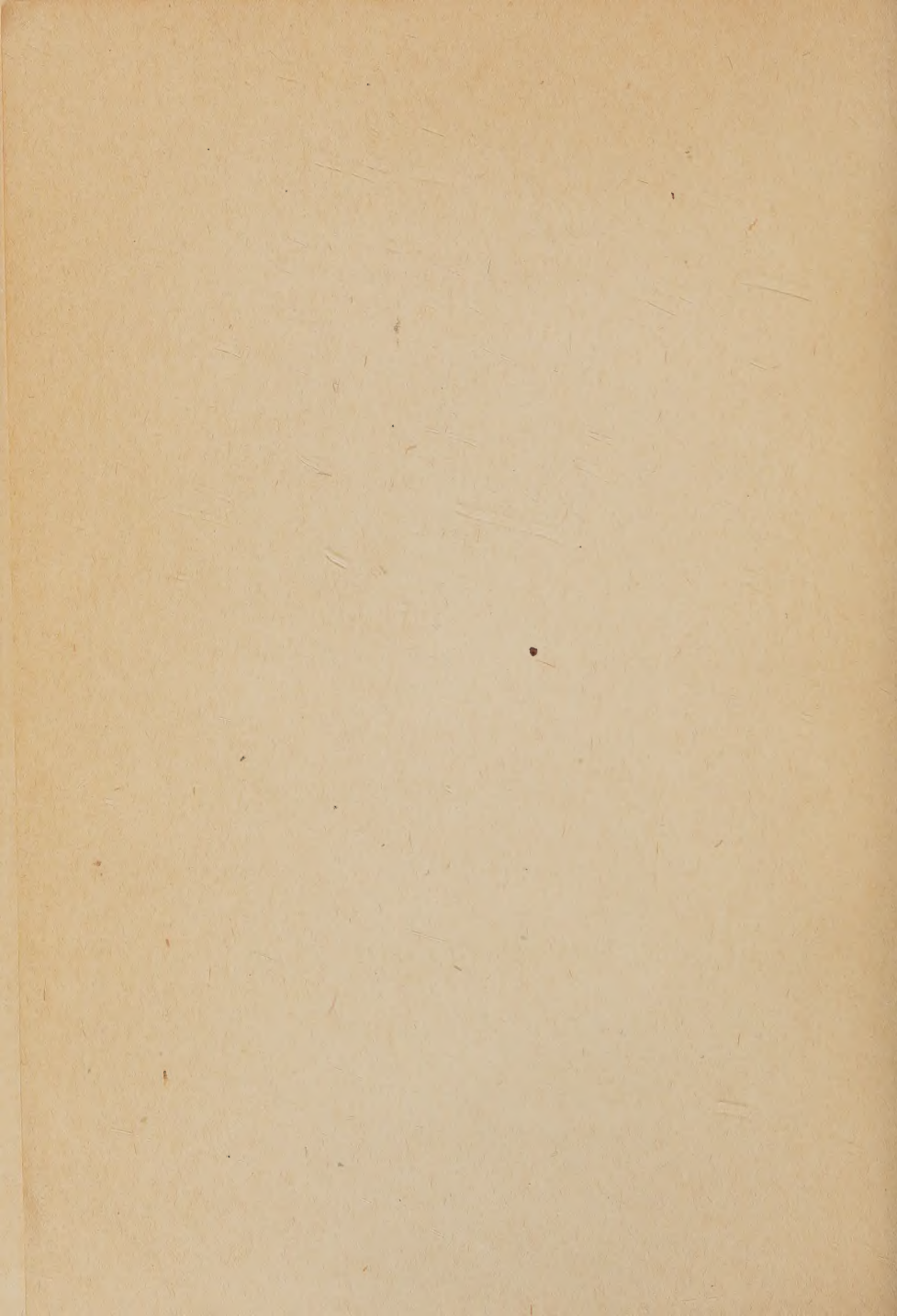
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LOGARITHMIC REDUCTION TABLES

FOR STUDENTS OF
ANALYTICAL CHEMISTRY

BY

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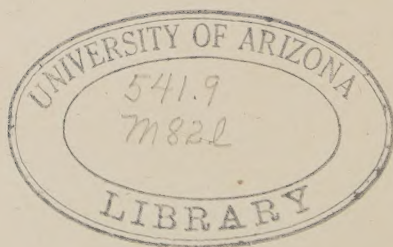
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TO
THE MEMORY OF
MY DEVOTED MOTHER
THIS LITTLE VOLUME
IS DEDICATED

136670

PREFACE

These tables are intended primarily for students of analytical chemistry. My aim has been to produce a book adapted to the needs of the beginner, and, at the same time, to arrange the material in such a way that it may be *conveniently* used by advanced students and chemists.

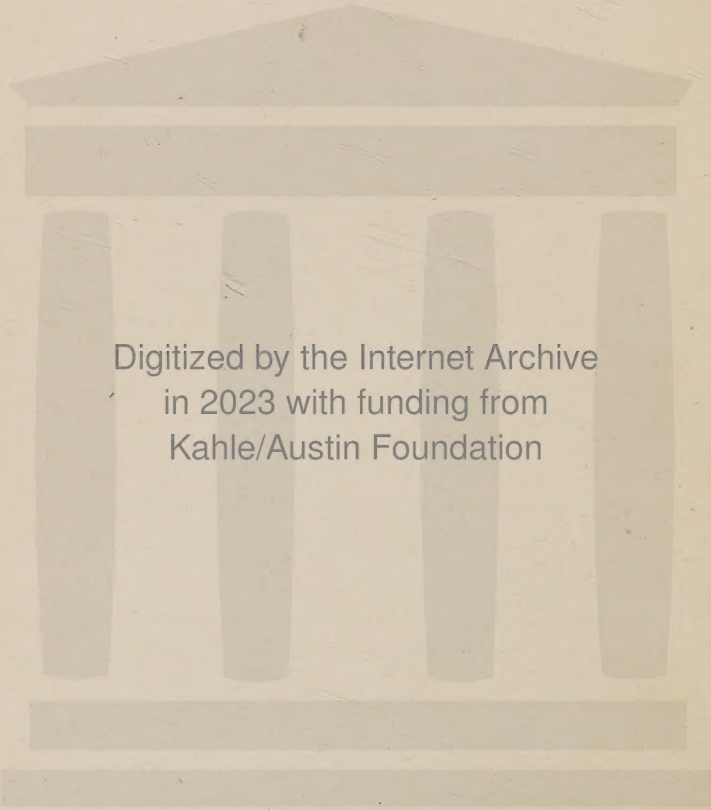
In discussing logarithms I realize I have encroached on foreign territory, but, in my experience as a teacher, I have known many students who were unfamiliar with the use of logarithms, and who were unwilling to acquaint themselves with the subject unless it be presented as a part of their present work. The subject is important for any one to know who has many arithmetical computations to make, and I hope that a sufficient number will profit by the explanations to justify me in including them.

The tables contain the most recent trustworthy values to be found in the literature. These values and their logarithms have been checked three times in order to eliminate possible errors.

I have used freely Landolt-Börnstein's *Physikalisch-chemische Tabellen*, Ostwald-Luther's *Physiko-chemische Messungen*, and many original articles.

C. J. MOORE

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LOGARITHMIC REDUCTION TABLES

THE ATOMIC WEIGHTS OF THE ELEMENTS AND THEIR LOGARITHMS

	Symbol	Atomic weight	Logarithm
Aluminum	Al	27.1	.432 969
Antimony	Sb	119.86	.078 674
Argon	A	39.9	.600 973
Arsenic	As	74.95	.874 772
Barium	Ba	137.36	.137 860
Bismuth	Bi	208.0	.318 063
Boron	B	11.0	.041 393
Bromine	Br	79.909	.902 596
Cadmium	Cd	112.41	.050 805
Cæsium	Cs	132.80	.123 198
Calcium	Ca	40.07	.602 819
Carbon	C	12.00	.079 181
Cerium	Ce	140.24	.146 872
Chlorine	Cl	35.454	.549 665
Chromium	Cr	52.00	.716 003
Cobalt	Co	58.96	.770 557
Columbium	Cb	93.5	.970 812
Copper	Cu	63.57	.803 252
Dysprosium	Dy	162.5	.210 853
Erbium	Er	167.4	.223 755
Europium	Eu	152.0	.181 844
Fluorine	F	19.0	.278 754
Gadolinum	Gd	157.3	.196 729
Gallium	Ga	69.9	.844 477
Germanium	Ge	72.5	.860 338
Glucinum	Gl	9.1	.959 041
Gold	Au	197.2	.294 907
Helium	He	4.0	.602 060
Hydrogen	H	1.0078	.003 375
Indium	In	114.8	.059 942
Iodine	I	126.91	.103 496
Iridium	Ir	193.1	.285 782
Iron	Fe	55.83	.746 868
Krypton	Kr	81.8	.912 753
Lanthanum	La	139.0	.143 015
Lead	Pb	207.07	.316 117
Lithium	Li	6.939	.841 297
Lutecium	Lu	174.0	.240 549
Magnesium	Mg	24.32	.385 964
Manganese	Mn	54.92	.739 731

TABLE I (CONTINUED)

	Symbol	Atomic weight	Logarithm
Mercury	Hg	200.61	.302 353
Molybdenum	Mo	96.0	.982 271
Neodymium	Nd	144.26	.159 146
Neon	Ne	20.0	.301 030
Nickel	Ni	58.67	.768 416
Nitrogen	N	14.01	.146 438
Osmium	Os	190.9	.280 806
Oxygen	O	16.000	.204 120
Palladium	Pd	106.7	.028 164
Phosphorus	P	31.03	.491 782
Platinum	Pt	195.0	.290 035
Potassium	K	39.091	.592 077
Praseodymium	Pr	140.6	.147 985
Radium	Ra	225.95	.354 012
Rhodium	Rh	102.9	.002 415
Rubidium	Rb	85.44	.931 661
Ruthenium	Ru	101.7	.007 321
Samarium	Sa	150.4	.177 248
Scandium	Sc	44.1	.644 439
Selenium	Se	79.2	.898 725
Silicon	Si	28.3	.451 786
Silver	Ag	107.87	.032 901
Sodium	Na	22.993	.361 595
Strontium	Sr	87.613	.942 569
Sulphur	S	32.07	.506 099
Tantalum	Ta	181.5	.258 877
Tellurium	Te	127.5	.105 510
Terbium	Tb	159.2	.201 943
Thallium	Tl	204.0	.309 630
Thorium	Th	232.40	.366 236
Thulium	Tu	168.5	.226 600
Tin	Sn	119.0	.075 547
Titanium	Ti	48.1	.682 145
Tungsten	W	184.0	.264 818
Uranium	U	238.40	.377 306
Vanadium	V	51.2	.709 270
Xenon	Xe	128.0	.107 210
Ytterbium	Yb	172.0	.235 528
Yttrium	Y	89.0	.949 390
Zinc	Zn	65.36	.815 312
Zirconium	Zr	90.6	.957 128

SECOND TO SEVENTH MULTIPLES OF THE ATOMIC WEIGHTS OF
COMMON ELEMENTS AND THEIR LOGARITHMS

	2	log	3	log	4	log
Aluminum	54.2	733 999	81.3	910 090	108.4	035 029
Antimony	239.72	379 704	359.58	555 796	479.44	680 734
Arsenic	149.90	175 802	224.85	351 892	299.80	476 832
Barium	274.72	438 890	412.08	614 982	549.44	739 920
Bismuth	416.0	619 093	624.0	795 185	832.0	920 123
Boron	22.0	342 423	33.0	518 514	44.0	643 453
Bromine	159.818	203 626	239.727	379 717	319.636	504 656
Cadmium	224.82	351 835	337.23	527 927	449.64	652 865
Calcium	80.14	903 849	120.21	079 941	160.28	204 879
Carbon	24.00	380 211	36.00	556 303	48.00	681 241
Chlorine	70.908	850 695	106.362	026 787	141.816	151 725
Chromium	104.00	017 033	156.00	193 125	208.00	318 063
Cobalt	117.92	071 588	176.88	247 679	235.84	372 618
Copper	127.14	104 282	190.71	280 374	254.28	405 312
Fluorine	38.0	579 784	57.0	755 875	76.0	880 814
Gold	394.4	595 937	591.6	772 028	788.8	896 967
Hydrogen	2.0156	304 405	3.0234	480 496	4.0312	605 434
Iodine	253.82	404 526	380.73	580 617	507.64	705 556
Iron	111.66	047 898	167.49	223 989	223.32	348 928
Lead	414.14	617 147	621.21	793 238	828.28	918 177
Lithium	13.878	142 327	20.817	318 418	27.756	443 357
Magnesium	48.64	686 994	72.96	863 085	97.28	988 024
Manganese	109.84	040 760	164.76	216 852	219.68	341 790
Mercury	401.22	603 383	601.83	779 474	802.44	904 413
Molybdenum	192.0	283 301	288.0	459 392	384.0	584 331
Nickel	117.34	069 446	176.01	245 537	234.68	370 476
Nitrogen	28.02	447 468	42.03	623 559	56.04	748 498
Oxygen	32.000	505 150	48.000	681 241	64.000	806 181
Phosphorus	62.06	792 812	93.09	968 903	124.12	093 842
Platinum	390.0	591 065	585.0	767 156	780.0	892 095
Potassium	78.182	893 107	117.273	069 198	156.364	194 137
Silicon	56.6	752 816	84.9	928 908	113.2	053 846
Silver	215.74	333 930	323.61	510 022	431.48	634 961
Sodium	45.986	662 626	68.979	838 717	91.972	963 655
Strontium	175.226	243 598	262.839	419 690	350.452	544 628
Sulphur	64.14	807 129	96.21	983 220	128.28	108 159
Tin	238.0	376 577	357.0	552 668	476.0	677 607
Titanium	96.2	983 175	144.3	159 266	192.4	284 205
Tungsten	368.0	565 848	552.0	741 939	736.0	866 878
Uranium	476.8	678 336	715.2	854 428	953.6	979 366
Zinc	130.72	116 343	196 08	292 433	261.44	417 372

TABLE II (CONTINUED)

	5	log	6	log	7	log
Aluminum	135.5	131 939	162.6	211 121	189.7	278 067
Antimony	599.30	777 644	719.16	856 826	839.02	923 772
Arsenic	374.75	573 742	449.70	652 923	524.65	719 869
Barium	686.80	836 830	824.16	916 012	961.52	982 958
Bismuth	1040.0	017 033	1248.0	096 215	1456.0	163 161
Boron	55.0	740 363	66.0	819 544	77.0	886 491
Bromine	399.545	601 566	479.454	680 747	559.363	747 694
Cadmium	562.05	749 775	674.46	828 956	786.87	895 903
Calcium	200.35	301 789	240.42	380 971	280.49	447 917
Carbon	60.00	778 151	72.00	857 333	84.00	924 279
Chlorine	177.270	248 635	212.724	327 816	248.178	394 763
Chromium	260.00	414 973	312.00	494 155	364.00	561 101
Cobalt	294.80	469 528	353.76	548 709	412.72	615 656
Copper	317.85	502 222	381.42	581 404	444.99	648 350
Fluorine	95.0	977 724	114.0	056 905	133.0	123 852
Gold	986.0	993 877	1183.2	073 058	1380.4	140 005
Hydrogen	5.0390	702 344	6.0468	781 526	7.0546	848 472
Iodine	634.55	802 466	761.46	881 647	888.37	948 594
Iron	279.15	445 838	334.98	525 019	390.81	591 966
Lead	1035.35	015 087	1242.42	094 269	1449.49	161 215
Lithium	34.695	540 267	41.634	619 448	48.573	686 395
Magnesium	121.60	084 934	145.92	164 115	170.24	231 062
Manganese	274.60	438 701	329.52	517 881	384.44	584 828
Mercury	1003.05	001 323	1203.66	080 504	1404.27	147 451
Molybdenum	480.0	681 241	576.0	760 422	672.0	827 369
Nickel	293.35	467 386	352.02	546 567	410.69	613 514
Nitrogen	70.05	845 408	84.06	924 589	98.07	991 536
Oxygen	80.000	903 090	96.000	982 271	112.000	049 218
Phosphorus	155.15	190 752	186.18	269 933	217.21	336 880
Platinum	975.0	989 005	1170.0	068 186	1365.0	135 133
Potassium	195.455	291 047	234.546	370 228	273.637	437 175
Silicon	141.5	150 756	169.8	229 938	198.1	296 884
Silver	539.35	731 870	647.22	811 052	755.09	877 998
Sodium	114.965	060 566	137.958	139 747	160.951	206 694
Strontium	438.065	641 538	525.678	720 720	613.291	787 667
Sulphur	160.35	205 069	192.42	284 250	224.49	351 197
Tin	595.0	774 517	714.0	853 698	833.0	920 645
Titanium	240.5	381 115	288.6	460 296	336.7	527 243
Tungsten	920.0	963 788	1104.0	042 969	1288.0	109 916
Uranium	1192.0	076 276	1430.4	155 457	1668.8	222 404
Zinc	326.80	514 282	392.16	593 463	457.52	660 410

MOLECULAR WEIGHTS OF COMMON COMPOUNDS AND THEIR LOGARITHMS

	Mol. wt.	log		Mol. wt.	log
AgBr	187.779	273 647	CrO ₃	100.00	000 000
AgCN	133.88	126 716	CrO ₃	116.00	064 458
AgCl	143.324	156 319	Cu ₂ O	143.14	155 761
AgI	234.78	370 661	CuO	79.57	900 749
AgNO ₃	169.88	230 142	Cu ₂ S	159.21	201 970
Al ₂ O ₃	102.2	009 451	CuS	95.64	980 640
Al ₂ (SO ₄) ₃ · 18 H ₂ O	666.69	823 924	CuSO ₄	159.64	203 142
As ₂ O ₃	197.90	296 446	CuSO ₄ · 5 H ₂ O	249.72	397 453
As ₂ O ₅	229.90	361 539	FeCO ₃	115.83	063 821
AsO ₃	122.95	089 729	FeCl ₃ · 4 H ₂ O	198.80	298 416
AsO ₄	138.95	142 859	FeCl ₃	162.19	210 024
As ₂ S ₃	246.11	391 130	FeO	71.83	856 306
As ₂ S ₅	310.25	491 712	Fe ₂ O ₃	159.66	203 196
B ₂ O ₃	70.0	845 098	FePO ₄	150.86	178 574
BaCO ₃	197.36	295 259	FeS	87.90	943 939
BaCl ₂	208.27	318 627	FeSO ₄	151.90	181 558
BaCl ₂ · 2 H ₂ O	244.30	387 923	FeSO ₄ · 7 H ₂ O	278.01	444 060
BaCrO ₄	253.36	403 738	H ₃ BO ₃	62.0	792 392
Ba(NO ₃) ₂	261.38	417 273	HBr	80.917	908 040
BaO	153.36	185 712	HCHO	46.02	662 947
Ba(OH) ₂ · 8 H ₂ O	315.50	498 999	HC ₂ H ₃ O ₂	60.03	778 368
BaSO ₄	233.43	368 157	H ₂ C ₂ O ₄	90.02	954 339
BaSiF ₆	279.66	446 630	H ₂ C ₂ O ₄ · 2 H ₂ O	126.05	100 543
Bi ₂ O ₃	464.0	666 518	H ₂ C ₄ H ₄ O ₆	150.05	176 236
Bi ₂ S ₃	512.2	709 440	H ₃ C ₆ H ₅ O ₇ · H ₂ O	210.08	322 323
CO ₂	44.00	643 453	HCl	36.462	561 840
C ₂ O ₄	88.00	944 483	HClO ₄	100.462	002 002
CO	60.00	778 151	H ₂ Cr ₂ O ₇	218.02	338 496
CaCO ₃	100.07	000 304	H ₂ CrO ₄	118.02	071 956
CaCl ₂	110.98	045 245	HF	20.0	301 030
CaCl ₂ · 6 H ₂ O	219.07	340 583	HI	127.918	106 932
CaO	56.07	748 731	HNO ₃	63.02	799 478
CaSO ₄	136.14	133 986	H ₂ O	18.0156	255 649
CaSO ₄ · 2 H ₂ O	172.17	235 958	H ₂ O ₂	34.0156	531 678
CdO	128.41	108 599	H ₃ PO ₄	98.05	991 448
CdS	144.48	159 808	H ₂ PtCl ₆	409.7	612 466
CdSO ₄	208.48	319 064	H ₂ S	34.09	532 627
CoO	74.96	874 830	H ₂ SO ₃	82.09	914 290
CoSO ₄	155.03	190 416	H ₂ SO ₄	98.09	991 625
CoSO ₄ · 7 H ₂ O	281.14	448 923	Hg ₂ Cl ₂	472.13	674 062
Cr ₂ O ₃	152.00	181 844	HgCl ₂	271.52	433 802

	Mol. wt.	log		Mol. wt.	log
$\text{KAl}(\text{SO}_4)_2 \cdot 12 \text{H}_2\text{O}$	474.5	676 236	NH_4Cl	53.50	728 354
KAlSi_3O_8	279.1	445 760	$(\text{NH}_4)_2\text{Fe}(\text{SO}_4)_2 \cdot 6 \text{H}_2\text{O}$	392.14	593 441
KBr	119.000	075 547	$\text{NH}_4\text{Fe}(\text{SO}_4)_2 \cdot 12 \text{H}_2\text{O}$	482.19	683 218
KCN	65.10	813 581	NH_4OH	35.05	544 688
K_2CO_3	138.13	140 288	$(\text{NH}_4)_3\text{PO}_4(\text{MoO}_3)_{12}$	1877.2	273 511
KCl	74.545	872 419	$(\text{NH}_4)_2\text{PtCl}_6$	443.8	647 187
KClO_3	122.545	088 296	$(\text{NH}_4)_2\text{SO}_4$	132.15	121 067
KClO_4	138.545	141 591	$\text{NaAlSi}_3\text{O}_8$	263.0	419 956
$\text{K}_3\text{Co}(\text{NO}_2)_6$	452.29	655 417	$\text{Na}_2\text{B}_4\text{O}_7$	202.0	305 351
K_2CrO_4	194.18	288 205	$\text{Na}_2\text{B}_4\text{O}_7 \cdot 10 \text{H}_2\text{O}$	382.1	582 177
$\text{K}_2\text{Cr}_2\text{O}_7$	294.18	468 613	NaBr	102.902	012 424
$\text{KCr}(\text{SO}_4)_2 \cdot 12 \text{H}_2\text{O}$	499.42	698 466	$\text{NaC}_2\text{H}_3\text{O}_2 \cdot 3 \text{H}_2\text{O}$	136.06	133 730
$\text{K}_3\text{Fe}(\text{CN})_6$	329.15	517 394	Na_2CO_3	105.99	025 265
$\text{K}_4\text{Fe}(\text{CN})_6$	368.24	566 131	$\text{Na}_2\text{CO}_3 \cdot 10 \text{H}_2\text{O}$	286.14	456 579
KI	166.001	220 111	NaCl	58.447	766 762
KIO_3	214.001	330 416	$\text{Na}_2\text{Cr}_2\text{O}_7 \cdot 2 \text{H}_2\text{O}$	298.02	474 245
KMnO_4	158.01	198 685	NaHCO_3	84.00	924 279
KNO_2	85.10	929 930	$\text{Na}_2\text{HPO}_4 \cdot 12 \text{H}_2\text{O}$	358.24	554 174
KNO_3	101.10	004 751	NaHSO_4	120.07	079 435
$\text{KNaC}_4\text{H}_4\text{O}_6 \cdot 4 \text{H}_2\text{O}$	282.18	450 526	NaNO_2	69.00	838 849
K_2O	94.182	973 968	NaNO_3	85.00	929 419
KOH	56.099	748 955	Na_2O	61.986	792 294
K_2PtCl_6	485.9	686 547	Na_2O_2	77.986	892 017
K_2SO_4	174.25	241 173	NaOH	40.00	602 060
MgCO_3	84.32	925 931	$\text{Na}_2\text{S}_2\text{O}_3 \cdot 5 \text{H}_2\text{O}$	248.20	394 802
$\text{MgCl}_2 \cdot 6 \text{H}_2\text{O}$	203.32	308 180	$\text{Na}_2\text{SO}_3 \cdot 7 \text{H}_2\text{O}$	252.17	401 693
MgO	40.32	605 521	Na_2SO_4	142.06	152 472
$\text{Mg}_2\text{P}_2\text{O}_7$	222.70	347 720	$\text{Na}_2\text{SO}_4 \cdot 10 \text{H}_2\text{O}$	322.21	508 139
MgSO_4	120.39	080 590	NiO	74.67	873 146
$\text{MgSO}_4 \cdot 7 \text{H}_2\text{O}$	246.50	391 817	NiSO_4	154.74	189 603
MnCO_3	114.92	060 396	$\text{NiSO}_4 \cdot 7 \text{H}_2\text{O}$	280.85	448 474
MnO	70.92	850 769	NO_3	62.01	792 462
Mn_2O_3	157.84	198 217	PbCl_3	137.39	137 955
Mn_3O_4	228.76	359 380	PBr_3	270.76	432 585
MnO_2	86.92	939 120	P_2O_3	110.06	041 630
$\text{Mn}_2\text{P}_2\text{O}_7$	283.90	453 165	P_2O_5	142.06	152 472
MnS	86.99	939 469	PO_5	95.03	977 861
MnSO_4	150.99	178 948	PbCO_3	267.07	426 625
$\text{MnSO}_4 \cdot 4 \text{H}_2\text{O}$	223.05	348 402	PbCl_2	277.98	444 014
NH_3	17.03	231 215	PbCrO_4	323.07	509 297
NH_4	18.04	256 237	$\text{Pb}(\text{NO}_3)_2$	331.09	549 946
$(\text{NH}_4)_2\text{C}_2\text{O}_4 \cdot \text{H}_2\text{O}$	142.10	152 594	PbO	223.07	348 441

TABLE III (CONTINUED)

	Mol.wt.	log		Mol. wt.	log
PbS	239.14	378 652	SnO	135.0	130 334
PbSO ₄	303.14	481 643	SnO ₂	151.0	178 977
PtCl ₄	336.8	527 372	SrCO ₃	147.61	169 116
SO ₂	64.07	806 655	Sr(NO ₃) ₂	211.63	325 577
SO ₃	80.07	903 470	SrO	103.613	015 414
SO ₄	96.07	982 588	Sr(OH) ₂ · 8 H ₂ O	265.754	424 480
SiO ₂	60.3	780 317	SrSO ₄	183.68	264 062
SiO ₃	76.3	882 525	ZnCO ₃	125.36	098 159
SiO ₄	92.3	965 202	ZnO	81.36	910 411
SnCl ₂	189.9	278 525	ZnS	97.43	988 693
SnCl ₂ · 2 H ₂ O	225.9	353 916	ZnSO ₄ · 7 H ₂ O	287.54	458 698
SnCl ₄	260.8	416 308			

SECOND TO FIFTH MULTIPLES OF THE MOLECULAR WEIGHTS OF SOME
COMMON COMPOUNDS AND OF THE WEIGHTS OF A FEW RADICALS
TOGETHER WITH THEIR LOGARITHMS

	2	log	3	log	4	log	5	log
AgBr	375.558	574 677	563.337	750 768	751.116	875 707	938.895	972 617
AgCl	286.648	457 349	429.972	633 440	573.296	758 379	716.620	855 289
AgI	469.56	671 691	704.34	847 782	939.12	922 721	1173.90	069 631
Al ₂ O ₃	204.4	310 481	306.6	486 572	408.8	611 511	511.0	708 421
Ba(OH) ₂	342.75	534 977	514.13	711 073	685.50	836 007	856.88	932 920
Ba(OH) ₂ ·8H ₂ O	631.00	800 029	946.50	976 121	1262.00	101 059	1577.5	197 969
CO ₂	88.00	944 483	132.00	120 574	176.00	245 513	220.00	342 423
CO ₂	120.00	079 181	180.00	255 273	240.00	380 211	300.00	477 121
CaO	112.14	049 761	168.21	225 852	224.28	350 791	280.35	447 701
Cr ₂ O ₃	304.00	482 874	456.00	658 965	608.00	783 904	760.00	880 814
CuO	159.14	201 779	238.71	377 871	318.28	502 809	397.85	599 719
FeO	143.64	157 275	215.46	333 367	287.28	458 305	359.10	555 215
Fe ₂ O ₃	319.28	504 172	478.92	680 263	638.56	805 202	798.20	902 112
HCHO	92.03	963 929	138.05	140 036	184.06	264 959	230.10	361 917
H ₂ C ₂ O ₄	120.06	079 398	180.09	255 490	240.13	380 446	300.15	477 338
H ₂ C ₂ O ₄	180.03	255 345	270.05	431 444	360.06	556 375	450.10	653 309
H ₂ C ₂ O ₄ ·2H ₂ O	252.09	401 556	378.14	577 653	504.19	702 594	630.25	799 513
H ₂ C ₂ H ₄ O ₆	300.09	477 251	450.14	653 348	600.19	778 289	750.25	875 206
H ₃ C ₆ H ₅ O ₇ ·H ₂ O	420.16	623 415	630.23	799 499	840.31	924 440	1050.2	021 293
HCl	72.924	862 870	109.385	038 958	145.847	163 898	182.31	260 810
HNO ₃	126.04	100 508	189.05	276 577	252.07	401 521	315.10	498 448
H ₂ O	36.0312	556 700	54.0468	732 828	72.0614	857 724	90.0780	954 619
H ₂ SO ₄	196.17	292 633	294.26	468 731	392.34	593 663	490.45	690 595
K ₂ O	188.364	274 998	282.546	451 089	376.728	576 028	470.910	672 938
KOH	112.198	049 985	168.296	226 074	224.395	351 013	280.49	447 925
MgO	80.64	906 551	120.96	082 642	161.28	207 581	201.60	304 491
NH ₃	34.07	532 372	51.10	708 421	68.13	833 338	85.15	930 185
NH ₄	36.08	557 267	54.12	733 358	72.16	858 297	92.30	965 207
NH ₄ OH	70.1	845 718	105.15	021 809	140.20	146 748	175.25	243 658
NO ₃	124.02	093 492	186.03	269 583	248.04	394 522	310.05	491 432
Na ₂ CO ₃	211.97	326 274	317.96	502 372	423.94	627 304	529.95	724 235
NaOH	80.002	903 100	120.002	079 188	160.003	204 128	200.00	301 030
OH	34.0156	531 678	51.0234	707 769	68.0312	832 708	85.039	929 618
PO ₄	190.06	278 891	285.09	454 982	380.12	579 921	475.15	676 831
P ₂ O ₅	284.12	453 502	426.18	629 593	568.24	754 532	710.30	851 442
SO ₂	128.14	107 685	192.21	283 776	256.28	408 715	320.35	505 625
SO ₃	160.14	204 500	240.21	380 591	320.28	505 530	400.35	602 440
SO ₄	192.14	283 618	288.21	459 709	384.28	584 648	480.35	681 558
SiO ₂	120.6	081 347	180.9	257 439	241.2	382 377	301.5	479 287
SiO ₃	152.6	183 555	228.9	359 646	305.2	484 585	381.5	581 495
SiO ₄	184.6	266 232	276.9	442 323	369.2	567 262	461.5	664 172

REDUCTION OF COMPOUNDS FOUND TO CONSTITUENTS SOUGHT
BY MULTIPLICATION

Sought	Found	Factor	log
Ag	AgBr	.57 445	759 254
	AgCl	.75 263	876 582
Al	Al ₂ O ₃	.53 033	724 548
As	As ₂ O ₃	.75 745	879 356
	As ₂ O ₅	.65 202	814 263
	As ₂ S ₃	.60 908	784 672
	As ₂ S ₅	.48 316	684 090
	MgNH ₄ AsO ₄ · H ₂ O	.37 601	575 200
	Mg ₂ As ₂ O ₇	.48 270	683 684
	As ₂ O ₃	.86 081	934 907
	As ₂ S ₃	.80 411	905 316
	As ₂ S ₅	.63 787	804 734
	MgNH ₄ AsO ₄ · H ₂ O	.49 641	695 844
As ₂ O ₃	Mg ₂ As ₂ O ₇	.63 728	804 328
	As ₂ S ₃	.93 413	970 409
	As ₂ S ₅	.99 914	999 629
	As ₂ O ₅	1.12 917	052 759
	As ₂ S ₃	.89 568	952 148
	BaO	.69 599	842 601
	BaCO ₃	.54 213	734 103
	BaSO ₄	.58 844	769 703
	BaSiF ₆	.49 117	691 230
	BaO	.77 706	890 453
BaO	BaSO ₄	.65 698	817 555
	Bi ₂ O ₃	.89 655	952 575
Bi	Bi ₂ S ₃	.81 217	909 645
	B ₂ O ₃	.31 428	497 325
B	KBF ₄	.08 723	940 666
	Br	.42 555	628 949
C	CO ₂	.27 273	435 728
	CaCO ₃	.43 969	643 149
CO ₂	CaO	.78 473	894 722
	MgO	1.09 127	037 932
	CO ₂	1.36 363	134 698
	Ca ₃	.40 042	602 515
Ca	CaCO ₃	.71 464	854 088
	CaO	.29 433	468 833
	CaSO ₄	1.78 473	251 573
	CaO	.73 505	866 318
CaCO ₃	CaSO ₄	1.27 432	105 278
	CO ₂		

TABLE V (CONTINUED)

Sought	Found	Factor	log
CaO	CaCO ₃	.56 031	748 427
	CaSO ₄	.41 186	614 745
Cd	CdO	.87 540	942 206
	CdS	.77 803	890 997
	CdSO ₄	.53 919	731 741
CdO	CdS	.88 877	948 791
	CdSO ₄	.61 593	789 535
Cl	Ag	.32 867	516 764
Cl	AgCl	.24 737	393 346
Co	CoO	.78 655	895 727
	CoSO ₄	.38 031	580 141
	2 CoSO ₄ · 3 K ₂ SO ₄	.14 159	151 041
	2 CoK ₃ (NO ₂) ₆ · 3 H ₂ O	.12 300	089 922
CoO	Co	1.27 137	104 273
	CoSO ₄	.48 352	684 414
	2 CoSO ₄ · 3 K ₂ SO ₄	.18 002	255 314
	2 CoSO ₄ K ₃ (NO ₂) ₆ · 3 H ₂ O	.15 638	194 195
Cr	BaCrO ₄	.20 524	312 265
	Cr ₂ O ₃	.68 421	835 189
	PbCrO ₄	.16 096	206 706
Cr ₂ O ₃	BaCrO ₄	.29 997	477 076
	PbCrO ₄	.23 524	371 517
CrO ₃	BaCrO ₄	.39 470	596 262
	Cr ₂ O ₃	1.31 579	119 186
	PbCrO ₄	.30 953	490 703
CrO ₄	BaCrO ₄	.45 784	660 710
	Cr ₂ O ₃	1.52 631	183 644
	PbCrO ₄	.35 905	555 161
Cu	CuO	.79 892	902 503
	CuS	.79 857	902 312
CuO	Cu	1.25 169	097 497
	Cu ₂ S	.99 956	999 809
F	CaF ₂	.48 662	687 189
	SiF ₄	.72 866	862 530
Fe	Fe ₂ O ₃	.69 932	844 678
	FeS	.63 511	802 851
FeO	Fe	1.28 663	109 455
	Fe ₂ O ₃	.89 977	954 133
Fe ₂ O ₃	Fe	1.42 995	155 322
H	H ₂ O	.11 188	048 756
HBr	AgBr	.43 092	634 393
HCl	AgCl	.25 440	405 521

Sought	Found	Factor	log
HI	AgI	.54 484	736 271
HNO ₃	NH ₄ Cl	1.17 794	071 124
	(NH ₄) ₂ PtCl ₆	.28 400	453 321
	Pt	.64 635	810 473
H ₂ SO ₄	BaSO ₄	.42 021	623 468
Hg	Hg ₂ Cl ₂	.84 981	929 321
	HgS	.86 217	935 594
Hg ₂ O	Hg	1.03 988	016 982
HgO	Hg	1.07 976	033 326
I	AgI	.54 055	732 835
	PdI ₂	.70 408	847 621
K	KCl	.52 439	719 658
	K ₂ PtCl ₆	.16 090	206 560
K	Pt	.40 093	603 072
	K ₂ SO ₄	.44 868	651 934
KCl	K ₂ PtCl ₆	.30 683	486 902
	Pt	.76 457	883 414
K ₂ O	KCl	.63 171	800 519
	KNO ₃	.46 579	668 187
	K ₂ PtCl ₆	.19 383	287 421
	Pt	.48 298	683 933
	K ₂ SO ₄	.54 050	732 795
K ₂ SO ₄	BaSO ₄	.74 648	873 016
Li	Li ₂ O	.46 449	666 975
	Li ₂ CO ₃	.18 784	273 800
	Li ₃ PO ₄	.17 967	254 483
	Li ₂ SO ₄	.12 622	101 131
Li ₂ O	Li ₂ CO ₃	.40 441	606 825
	Li ₃ PO ₄	.38 682	587 506
	Li ₂ SO ₄	.27 174	434 156
Mg	MgO	.60 317	780 443
	Mg ₂ P ₂ O ₇	.21 839	339 235
MgCO ₃	MgO	2.09 127	320 410
	Mg ₂ P ₂ O ₇	.75 718	879 199
MgO	Mg ₂ P ₂ O ₇	.36 207	558 792
Mn	MnO	.77 439	888 962
	Mn ₂ O ₃	.69 590	842 544
	Mn ₃ O ₄	.72 023	857 472
	Mn ₂ P ₂ O ₇	.38 690	587 596
	MnS	.63 134	800 262
	MnSO ₄	.36 373	560 783
MnO	MnS	.81 527	911 300

TABLE V (CONTINUED)

Sought	Found	Factor	log
MnO	MnSO ₄	.46 970	671 821
N	NH ₃	.82 266	915 223
	(NH ₄) ₂ PtCl ₆	.06 314	800 281
NH ₃	Pt	.14 369	157 433
	N	1.21 556	084 777
	NH ₄ Cl	.31 832	502 861
	(NH ₄) ₂ PtCl ₆	.07 675	885 058
NH ₄	Pt	.17 466	242 210
	NH ₄ Cl	.33 720	527 883
	(NH ₄) ₂ PtCl ₆	.08 130	910 080
NO ₃	NH ₄ Cl	1.15 907	064 108
	(NH ₄) ₂ PtCl ₆	.27 945	446 305
	Pt	.63 600	803 457
Na	Na ₂ O	.74 187	870 331
	NaCl	.39 340	594 833
	NaNO ₃	.27 051	432 176
	Na ₂ SO ₄	.32 371	510 153
NaCl	Na ₂ SO ₄	.82 285	915 320
Na ₂ O	NaCl	.53 028	724 502
	NaNO ₃	.36 462	561 845
	Na ₂ SO ₄	.43 634	639 822
Na ₂ SO ₄	BaSO ₄	.60 858	784 315
Ni	NiO	.78 572	895 270
NiO	Ni	1.27 271	104 730
P	P ₂ O ₅	.43 686	640 340
	Mg ₂ P ₂ O ₇	.27 867	445 092
	(NH ₄) ₃ PO ₄ · 12 MoO ₃	.01 653	218 271
P ₂ O ₅	Ag ₃ PO ₄	.16 967	229 601
	Mg ₂ P ₂ O ₇	.63 790	804 752
	(NH ₄) ₃ PO ₄ · 12 MoO ₃	.03 784	577 931
	(UO ₂) ₂ P ₂ O ₇	.19 872	298 251
PO ₄	Mg ₂ P ₂ O ₇	.85 344	931 171
	(NH ₄) ₃ PO ₄ · 12 MoO ₃	.05 062	704 350
Pb	PbCrO ₄	.64 094	806 820
	PbO	.92 827	967 676
	PbO ₂	.86 615	937 592
	PbS	.86 589	937 465
	PbSO ₄	.68 309	834 474
PbO	PbCrO ₄	.69 047	839 144
	PbS	.93 280	969 789
	PbSO ₄	.73 586	866 798
PbS	PbSO ₄	.78 888	897 009

TABLE V (CONTINUED)

Sought	Found	Factor	log
Pt	NaCl	1.66 818	222 243
S	BaSO ₄	.13 738	137 942
	As ₂ S ₃	.39 092	592 090
SO ₃	BaSO ₄	.34 302	535 313
SO ₄	BaSO ₄	.41 156	614 431
Sb	Sb ₂ O ₃	.83 317	920 734
	Sb ₂ O ₄	.78 928	897 230
	Sb ₂ S ₃	.71 360	853 455
	Sb ₂ S ₅	.59 919	777 568
Sb ₂ O ₃	Sb ₂ O ₄	.94 732	976 496
	Sb ₂ S ₃	.85 649	932 721
	Sb ₂ S ₅	.71 917	856 834
Si	SiO ₂	.46 932	671 469
SiO ₃	SiO ₂	1.26 534	102 208
SiO ₄	SiO ₂	1.53 068	184 885
Si ₂ O ₇	SiO ₂	1.39 800	145 510
Sn	SnO ₂	.78 808	896 570
SnO	SnO ₂	.89 404	951 357
Sr	SrCO ₃	.59 354	773 453
	SrO	.84 558	927 155
	SrSO ₄	.47 699	678 507
SrO	SrCO ₃	.70 194	846 298
	SrSO ₄	.56 409	751 352
Ti	TiO ₂	.60 050	778 512
U	UO ₂	.88 166	945 299
	U ₃ O ₈	.84 820	928 497
W	WO ₃	.79 310	899 330
Zn	ZnO	.80 334	904 901
	ZnS	.67 084	826 619
ZnO	ZnS	.83 506	921 718
ZnS	ZnO	1.19 752	078 282

REDUCTION OF BAROMETRIC READINGS TO 0°

(For temperatures above zero the corrections are negative and for temperatures below zero positive.)

Temperature	Glass Scale					Brass Scale				
	740 mm.	750 mm.	760 mm.	770 mm.	780 mm.	740 mm.	750 mm.	760 mm.	770 mm.	780 mm.
0°	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
1°	13	13	13	13	14	12	12	12	13	13
2°	26	26	26	27	27	24	25	25	25	25
3°	38	39	39	40	41	36	37	37	38	38
4°	51	52	53	53	54	48	49	50	50	51
5°	0.64	0.65	0.66	0.67	0.68	0.60	0.61	0.62	0.63	0.64
6°	77	78	79	80	81	72	73	74	75	76
7°	0.90	0.91	0.92	0.93	0.95	85	86	0.87	0.88	0.89
8°	1.02	1.04	1.05	1.07	1.08	0.97	0.98	1.99	1.01	1.02
9°	15	17	18	20	21	1.09	1.10	12	13	15
10°	1.28	1.30	1.31	1.33	1.35	1.21	1.22	1.24	1.26	1.27
11°	41	43	45	46	48	33	35	36	38	40
12°	53	56	58	60	62	45	47	49	51	53
13°	66	69	71	73	75	57	59	61	63	65
14°	79	81	84	1.86	1.89	69	71	73	76	78
15°	1.92	1.94	1.97	2.00	2.02	1.81	1.83	1.86	1.88	1.91
16°	2.05	2.07	2.10	13	16	1.93	1.96	1.98	2.01	2.03
17°	17	20	23	26	29	2.05	2.08	2.10	13	16
18°	30	33	36	39	43	17	20	23	26	29
19°	43	46	49	53	56	29	32	35	38	41
20°	2.56	2.59	2.62	2.66	2.69	2.41	2.44	2.47	2.51	2.54
21°	68	72	76	79	83	53	56	60	63	67
22°	81	85	2.89	2.92	2.96	65	69	72	76	79
23°	2.94	2.98	3.02	3.06	3.10	77	81	84	2.88	2.92
24°	3.06	3.11	15	19	23	2.89	2.93	2.97	3.01	3.05
25°	3.19	3.23	3.28	3.32	3.36	3.01	3.05	3.09	3.13	3.17
26°	32	36	41	45	50	13	17	21	26	30
27°	45	49	54	59	63	25	29	34	38	42
28°	57	62	67	72	77	37	41	46	51	55
29°	70	75	80	85	3.90	49	54	58	63	68
30°	3.83	3.88	3.93	3.98	4.03	3.61	3.66	3.71	3.75	3.80
31°	3.95	4.01	4.06	4.11	17	73	78	83	3.88	3.93
32°	4.08	14	19	25	30	85	3.90	3.95	4.00	4.05
33°	21	26	32	38	43	3.97	4.02	4.07	13	18
34°	33	39	45	51	57	4.09	14	20	25	31
35°	4.46	4.52	4.58	4.65	4.71	4.21	4.26	4.32	4.38	4.43

GEOGRAPHICAL LATITUDE, ELEVATION, AND GRAVITY (REFERRED TO
45° AND SEA LEVEL) OF SOME IMPORTANT CITIES

	Latitude	Height above sea level <i>m.</i>	Gravity	log
Baltimore, Met.	39° 18'	23.	0.9 994 705	999 770
Berlin, New Obs.	52° 30' 16.7"	37.00	1.0 006 736	000 292
Bonn, Obs.	50° 43' 45.0"	61.92	1.0 005 054	000 219
Boston, Met.	42° 21'	38.	0.9 997 438	999 889
Brüssels, Old Obs.	50° 51' 10.7"	56.	1.0 005 179	000 225
Cambridge, Eng., Obs.	52° 12' 51.6"	28.	1.0 006 504	000 282
Cambridge, Mass., Harvard Obs.	42° 22' 47.6"	24.	0.9 997 509	999 892
Cincinnati, Obs.	39° 8' 19.5"	263.	0.9 993 803	999 731
Dublin, Dunsink Obs.	53° 23' 13.1"	86.	1.0 007 365	000 320
Freiberg	47° 59' 40"	270.6	1.0 001 907	000 083
Göttingen, Obs.	51° 31' 48.2"	159.2	1.0 005 478	000 238
Greenwich, Obs.	51° 28' 38.1"	47.	1.0 005 783	000 251
Heidelberg, Obs.	49° 23' 54.9"	113.6	1.0 003 688	000 160
Kopenhagen, Obs.	55° 41' 12.9"	14.	1.0 009 602	000 317
London, Camden Sq., Met.	51° 32' 30"	34.	1.0 005 881	000 255
Madrid, Obs.	45° 27' 59.2"	120.	1.0 000 053	000 002
Montreal, McGill Col. Obs.	45° 30' 17.0"	57.	1.0 000 287	000 012
New Haven, Yale Obs.	41° 19' 22.3"	32.	0.9 996 521	999 848
New Orleans, Met.	29° 58'	16.	0.9 986 721	999 423
New York, Rutherford Obs.	40° 43' 48.5"	96.	0.9 995 774	999 817
Paris, Nat. Obs.	48° 50' 11.2"	59.	1.0 003 345	000 145
Philadelphia, Obs.	39° 57' 7.5"	36.	0.9 995 254	999 794
Prag, Obs.	50° 5' 15.8"	197.	1.0 004 053	000 176
Quebec, Obs.	46° 48' 20.8"	70.	1.0 001 446	000 063
St. Louis, Obs.	38° 38' 3.6"	171.	0.9 993 611	999 722
San Francisco, Davidson Obs.	37° 47' 28.0"	47.2	0.9 993 272	999 708
Strassburg, New Obs.	48° 35' 0.3"	144.66	1.0 002 845	000 124
Washington, Georgetown Hts. Obs.	38° 55' 14.7"	285.	0.9 993 537	999 719
Zürich, Obs. d. Polyt.	47° 22' 40"	468.24	1.0 000 718	000 031

REDUCTION OF BAROMETRIC READINGS TO NORMAL GRAVITY

(From Landolt-Börnstein)

A. REDUCTION TO 45° LATITUDE

(From 0° to 45° the correction is always negative, and from 45° to 90° positive.)

Latitude	Barometric Readings in mm., corrected for Temperature															Latitude
	640 mm.	650 mm.	660 mm.	670 mm.	680 mm.	690 mm.	700 mm.	710 mm.	720 mm.	730 mm.	740 mm.	750 mm.	760 mm.	770 mm.	780 mm.	
0°	1.66	1.68	1.71	1.74	1.76	1.79	1.81	1.84	1.86	1.89	1.92	1.94	1.97	1.99	2.02	90°
5°	63	66	68	71	73	76	79	81	84	86	89	91	94	96	1.99	85°
10°	56	58	61	63	65	68	70	73	75	78	80	83	85	87	90	80°
15°	44	46	48	50	53	55	57	59	61	64	66	68	70	73	75	75°
20°	27	29	31	33	35	37	39	41	43	45	47	49	51	53	55	70°
25°	1.07	1.08	1.10	1.12	1.13	1.15	1.17	1.18	1.20	1.22	1.23	1.25	1.27	28	30	65°
30°	0.83	0.84	0.85	0.87	0.88	0.89	0.91	0.92	0.93	0.95	0.96	0.97	0.98	1.00	1.01	60°
35°	57	58	58	59	60	61	62	63	64	65	66	66	67	0.68	0.69	55°
40°	29	29	30	30	31	31	31	32	32	33	33	34	34	35	35	50°
45°	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	45°

B. REDUCTION TO SEA LEVEL

(These corrections are all negative.)

Height above sea level m.	Barometric Readings in mm., corrected for Temperature									Height above sea level m.
	620 mm.	640 mm.	660 mm.	680 mm.	700 mm.	720 mm.	740 mm.	760 mm.	780 mm.	
100					0.01	0.01	0.01	0.01	0.02	100
200					0.03	03	03	03	0.03	200
300					04	04	04	04		300
400				0.05	05	05	06	06		400
500				06	07	07	07	07	0.07	500
600				08	08	08	08	09		600
700			0.09	09	09	10	10	10		700
800			10	10	11	11	11	0.12		800
900			0.11	0.12	0.12	0.12	0.13			900
1000	0.12	0.13	0.13	0.13	0.14	0.14				1000
1100	13	14	14	15	15	0.16				1100
1200	15	15	16	16	16					1200
1300	16	16	17	17	18					1300
1400	17	18	18	19	0.19					1400
1500	18	19	19	20						1500
1600	19	20	21	21						1600
1700	21	21	22	0.23						1700
1800	22	23	23							1800
1900	0.23	0.24	0.25							1900
2000	0.24	0.25								2000

CAPILLARY DEPRESSION OF MERCURY

(Interpolated by F. Kohlrausch from Mendeleeff and Gutkowsky.)

Height of Meniscus in mm.								
Diameter of tube <i>mm.</i>	0.4 <i>mm.</i>	0.6 <i>mm.</i>	0.8 <i>mm.</i>	1.0 <i>mm.</i>	1.2 <i>mm.</i>	1.4 <i>mm.</i>	1.6 <i>mm.</i>	1.8 <i>mm.</i>
4	0.83	1.22	1.54	1.98	2.37			
5	47	0.65	0.86	1.19	1.45	1.80		
6	27	41	56	0.78	0.98	1.21	1.43	
7	18	28	40	53	67	0.82	0.97	1.13
8		20	29	38	46	56	65	0.77
9		15	21	28	33	40	46	52
10			15	20	25	29	33	37
11			10	14	18	21	24	27
12			07	10	13	15	18	19
13			04	07	10	12	13	14

TENSION OF AQUEOUS VAPOR OVER WATER—EXPRESSED IN TERMS
OF NORMAL MERCURY UNITS

(Taken from Landolt-Börnstein. Observations by Regnault.)

Degrees	Hydrogen Scale. Tenth Degrees									
	.0 mm.	.1 mm.	.2 mm.	.3 mm.	.4 mm.	.5 mm.	.6 mm.	.7 mm.	.8 mm.	.9 mm.
0	4.579	4.612	4.646	4.679	4.713	4.747	4.782	4.816	4.851	4.886
1	4.921	4.957	4.992	5.028	5.064	5.101	5.137	5.174	5.211	5.248
2	5.286	5.324	5.362	5.400	5.438	5.477	5.516	5.555	5.595	5.635
3	5.675	5.715	5.755	5.796	5.837	5.878	5.920	5.961	6.003	6.046
4	6.088	6.131	6.174	6.217	6.261	6.305	6.349	6.393	6.438	6.483
5	6.528	6.574	6.620	6.666	6.712	6.759	6.806	6.853	6.901	6.949
6	6.997	7.045	7.094	7.143	7.192	7.242	7.292	7.342	7.392	7.443
7	7.494	7.546	7.598	7.650	7.702	7.755	7.808	7.861	7.914	7.968
8	8.023	8.077	8.132	8.187	8.243	8.299	8.355	8.412	8.469	8.526
9	8.584	8.642	8.700	8.759	8.818	8.877	8.937	8.997	9.057	9.118
10	9.179	9.240	9.302	9.364	9.427	9.490	9.553	9.616	9.680	9.745
11	9.810	9.875	9.940	10.006	10.072	10.139	10.206	10.274	10.342	10.410
12	10.479	10.548	10.617	10.687	10.757	10.828	10.899	10.970	11.042	11.114
13	11.187	11.260	11.333	11.407	11.481	11.556	11.631	11.706	11.782	11.859
14	11.936	12.013	12.091	12.169	12.247	12.326	12.406	12.486	12.566	12.647
15	12.728	12.810	12.892	12.974	13.057	13.141	13.225	13.309	13.394	13.480
16	13.565	13.651	13.738	13.825	13.913	14.001	14.090	14.179	14.269	14.359
17	14.450	14.541	14.632	14.724	14.817	14.910	15.003	15.097	15.192	15.287
18	15.383	15.479	15.575	15.672	15.770	15.868	15.967	16.066	16.166	16.266
19	16.367	16.469	16.571	16.673	16.776	16.880	16.984	17.088	17.193	17.299
20	17.406	17.513	17.620	17.728	17.837	17.947	18.057	18.167	18.278	18.390
21	18.503	18.616	18.729	18.844	18.959	19.074	19.190	19.307	19.424	19.542
22	19.661	19.780	19.900	20.021	20.142	20.264	20.386	20.510	20.634	20.758
23	20.883	21.010	21.137	21.264	21.393	21.522	21.652	21.782	21.913	22.045
24	22.178	22.311	22.446	22.581	22.716	22.853	22.990	23.128	23.266	23.406
25	23.546	23.686	23.828	23.970	24.113	24.257	24.401	24.547	24.693	24.839
26	24.987	25.135	25.284	25.434	25.584	25.736	25.888	26.041	26.195	26.349
27	26.505	26.661	26.818	26.976	27.134	27.294	27.454	27.615	27.777	27.939
28	28.103	28.267	28.432	28.599	28.766	28.933	29.102	29.271	29.442	29.613
29	29.785	29.958	30.132	30.307	30.482	30.659	30.836	31.015	31.194	31.374
30	31.555	31.737	31.919	32.103	32.288	32.473	32.660	32.847	33.036	33.225
31	33.416	33.607	33.799	33.992	34.187	34.382	34.578	34.775	34.973	35.172
32	35.372	35.573	35.775	35.978	36.182	36.387	36.593	36.800	37.008	37.217
33	37.427	37.638	37.851	38.064	38.278	38.493	38.710	38.927	39.146	39.365
34	39.586	39.807	40.030	40.254	40.479	40.705	40.933	41.161	41.390	41.621
35	41.853	42.085	42.319	42.554	42.791	43.028	43.266	43.506	43.747	43.989

REDUCTION OF WATER PRESSURE TO MERCURY PRESSURE

(Calculated from the following: temperature of the water 4°, of the mercury 0°;
density of the water 1, of the mercury 13.59545)

(Thiesen and Schul. Z. S. f. Instrk. 18, 138)

Water	Mercury	Water	Mercury	Water	Mercury	Water	Mercury	Water	Mercury
10	0.74	50	3.68	90	6.62	130	9.56	170	12.50
11	81	51	75	91	69	131	64	171	58
12	88	52	82	92	77	132	71	172	65
13	0.96	53	90	93	84	133	78	173	72
14	1.03	54	3.97	94	91	134	86	174	80
15	10	55	4.05	95	6.99	135	9.93	175	87
16	18	56	12	96	7.06	136	10.00	176	12.95
17	25	57	19	97	13	137	08	177	13.02
18	32	58	27	98	21	138	15	178	09
19	40	59	34	99	28	139	22	179	17
20	1.47	60	4.41	100	7.36	140	10.30	180	13.24
21	54	61	49	101	43	141	37	181	31
22	62	62	56	102	50	142	44	182	38
23	69	63	63	103	58	143	52	183	46
24	77	64	71	104	65	144	59	184	53
25	84	65	78	105	72	145	67	185	61
26	91	66	85	106	80	146	74	186	68
27	1.99	67	4.93	107	87	147	81	187	75
28	2.06	68	5.00	108	7.94	148	89	188	83
29	13	69	08	109	8.02	149	10.96	189	90
30	2.21	70	5.15	110	8.09	150	11.03	190	13.98
31	28	71	22	111	16	151	11	191	14.05
32	35	72	30	112	24	152	18	192	12
33	43	73	37	113	31	153	25	193	20
34	50	74	44	114	39	154	33	194	27
35	57	75	52	115	46	155	40	195	34
36	65	76	59	116	53	156	47	196	42
37	72	77	66	117	61	157	55	197	49
38	79	78	74	118	68	158	62	198	56
39	87	79	81	119	75	159	69	199	64
40	2.94	80	5.88	120	8.83	160	11.77	200	14.71
41	3.02	81	5.96	121	90	161	84	300	22.07
42	09	82	6.03	122	8.97	162	92	400	29.42
43	16	83	10	123	9.05	163	11.99	500	36.78
44	24	84	18	124	12	164	12.06	600	44.13
45	31	85	25	125	19	165	14	700	51.49
46	38	86	33	126	27	166	21	800	58.84
47	46	87	40	127	34	167	28	900	66.20
48	53	88	47	128	41	168	36	1000	73.55
49	60	89	55	129	49	169	43		

REDUCTION OF THE VOLUME OF GASES TO NORMAL PRESSURE

(This table contains the values of $\frac{h}{760}$ where $h = 500$ to 839 mm.)

(Landolt-Börnstein)

h mm.	$\frac{h}{760}$	$\log \frac{h}{760}$	h mm.	$\frac{h}{760}$	$\log \frac{h}{760}$	h mm.	$\frac{h}{760}$	$\log \frac{h}{760}$
500	0.65 789	818 153	540	0.71 053	851 582	580	0.76 316	882 616
501	0.65 921	9 024	541	184	2 382	581	447	3 360
502	0.66 053	819 893	542	316	3 187	582	579	4 110
503	184	820 753	543	447	3 984	583	711	4 858
504	316	1 618	544	579	4 786	584	842	5 599
505	447	2 475	545	711	5 586	585	0.76 974	6 344
506	579	3 337	546	842	6 378	586	0.77 105	7 083
507	711	4 198	547	0.71 974	7 176	587	237	7 825
508	842	5 049	548	0.72 105	7 965	588	368	8 561
509	0.66 974	5 906	549	237	8 760	589	500	889 302
510	0.67 105	826 755	550	0.72 368	859 547	590	0.77 632	890 041
511	237	7 608	551	500	860 338	591	763	0 773
512	368	8 454	552	632	1 128	592	0.77 895	1 510
513	500	829 304	553	763	1 911	593	0.78 026	1 682
514	632	830 152	554	0.72 895	2 698	594	158	2 973
515	763	0 993	555	0.73 026	3 478	595	289	3 701
516	0.67 895	1 838	556	158	4 262	596	421	4 432
517	0.68 026	2 675	557	289	5 039	597	553	5 163
518	158	3 517	558	421	5 820	598	684	5 886
519	289	4 351	559	553	6 600	599	816	6 614
520	0.68 421	835 189	560	0.73 684	867 373	600	0.78 947	897 336
521	553	6 027	561	816	8 151	601	0.79 079	8 061
522	684	6 856	562	0.73 947	8 921	602	211	8 786
523	816	7 689	563	0.74 079	869 695	603	342	899 503
524	0.68 947	8 515	564	211	870 468	604	474	900 225
525	0.69 079	839 346	565	342	1 234	605	605	0 940
526	211	840 175	566	474	2 005	606	737	1 660
527	342	0 996	567	605	2 768	607	0.79 868	2 373
528	474	1 822	568	737	3 536	608	0.80 000	3 090
529	605	2 640	569	0.74 868	4 296	609	132	3 806
530	0.69 737	843 463	570	0.75 000	875 061	610	0.80 263	904 515
531	0.69 868	4 278	571	132	5 825	611	395	5 229
532	0.70 000	5 098	572	263	6 582	612	526	5 936
533	132	5 916	573	395	7 343	613	658	6 647
534	263	6 727	574	526	8 097	614	789	7 352
535	395	7 542	575	658	8 855	615	0.80 921	8 061
536	526	8 349	576	789	879 606	616	0.81 053	8 769
537	658	9 161	577	0.75 921	880 362	617	184	909 470
538	789	849 966	578	0.76 053	1 116	618	316	910 176
539	921	850 775	579	184	1 864	619	447	0 875

TABLE XII (CONTINUED)

$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$	$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$	$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$
620	0.81 579	911 578	660	0.86 842	938 730	700	0.92 105	964 283
621	711	2 281	661	0.86 974	939 389	701	237	4 905
622	842	2 976	662	0.87 105	940 043	702	368	5 522
623	0.81 974	3 676	663	237	0 701	703	500	6 142
624	0.82 105	4 370	664	368	1 352	704	632	6 761
625	237	5 067	665	500	2 008	705	763	7 375
626	368	5 759	666	632	2 663	706	0.92 895	7 992
627	500	6 454	667	763	3 312	707	0.93 026	8 604
628	632	7 148	668	0.87 895	3 964	708	158	9 220
629	763	7 836	669	0.88 026	4 611	709	289	969 830
630	0.82 895	918 528	670	0.88 158	945 262	710	0.93 421	970 445
631	0.83 026	9 214	671	289	5 907	711	553	1 058
632	158	919 904	672	421	6 555	712	684	1 665
633	289	920 588	673	553	7 203	713	816	2 277
634	421	1 275	674	684	7 845	714	0.93 947	2 883
635	553	1 962	675	816	8 491	715	0.94 079	3 493
636	684	2 642	676	0.88 947	9 131	716	211	4 102
637	816	3 327	677	0.89 079	949 775	717	342	4 705
638	0.83 947	4 005	678	211	950 418	718	474	5 312
639	0.84 079	4 688	679	342	1 056	719	605	5 914
640	0.84 211	925 369	680	0.89 474	951 697	720	0.94 737	976 520
641	342	6 044	681	605	2 332	721	0.94 868	7 120
642	474	6 723	682	737	2 972	722	0.95 000	7 724
643	605	7 396	683	0.89 868	3 605	723	132	8 327
644	737	8 073	684	0.90 000	4 243	724	263	8 924
645	0.84 868	8 744	685	132	4 879	725	394	979 521
646	0.85 000	929 419	686	263	5 510	726	526	980 122
647	132	930 093	687	395	6 144	727	658	0 721
648	263	0 761	688	526	6 773	728	789	1 316
649	395	1 432	689	658	7 406	729	0.95 921	1 914
650	0.85 526	932 098	690	0.90 789	958 033	730	0.96 053	982 511
651	658	2 768	691	0.90 921	8 664	731	184	3 103
652	790	3 437	692	0.91 053	9 294	732	316	3 698
653	0.85 921	4 099	693	184	959 919	733	447	4 289
654	0.86 053	4 766	694	316	960 547	734	579	4 883
655	184	5 427	695	447	1 170	735	710	5 471
656	316	6 091	696	579	1 796	736	842	6 064
657	447	6 750	697	711	2 421	737	0.96 974	6 655
658	579	7 413	698	842	3 041	738	0.97 105	7 242
659	711	8 074	699	974	3 665	739	237	7 832

TABLE XII (CONTINUED)

$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$	$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$	$\frac{h}{mm.}$	$\frac{h}{760}$	$\log \frac{h}{760}$
740	0.97 368	988 416	780	1.02 632	011 283	820	1.07 895	033 001
741	500	9 005	781	763	1 837	821	1.08 026	3 529
742	632	989 592	782	1.02 895	2 394	822	158	4 059
743	763	990 175	783	1.03 026	2 947	823	289	4 584
744	0.97 895	0 761	784	158	3 504	824	421	5 113
745	0.98 026	1 341	785	289	4 054	825	553	5 642
746	158	1 926	786	421	4 609	826	684	6 166
747	289	2 505	787	553	5 163	827	816	6 693
748	421	3 088	788	684	5 712	828	1.08 947	7 215
749	553	3 670	789	816	6 264	829	1.09 079	7 741
750	0.98 684	994 247	790	1.03 947	016 812	830	1.09 211	038 267
751	816	4 827	791	1.04 079	7 363	831	342	8 787
752	0.98 947	5 403	792	211	7 914	832	471	9 299
753	0.99 079	5 982	793	342	8 459	833	605	039 831
754	211	6 560	794	474	9 008	834	737	040 353
755	342	7 133	795	605	019 552	835	1.09 868	0 871
756	474	7 710	796	737	020 100	836	1.10 000	1 393
757	605	8 281	797	1.04 868	0 643	837	132	1 913
758	737	8 856	798	1.05 000	1 189	838	263	2 430
759	0.99 868	999 426	799	132	1 735	839	395	2 949
760	1.00 000	000 000	800	1.05 263	022 276			
761	1.00 132	0 573	801	395	2 820			
762	263	1 141	802	526	3 359			
763	392	1 699	803	658	3 902			
764	526	2 278	804	789	4 441			
765	658	2 848	805	1.05 921	4 982			
766	789	3 413	806	1.06 053	5 523			
767	1.00 921	3 982	807	184	6 059			
768	1.01 053	4 549	808	316	6 598			
769	184	5 112	809	447	7 134			
770	1.01 316	005 678	810	1.06 579	027 672			
771	447	6 239	811	711	8 209			
772	579	6 804	812	842	8 742			
773	710	7 364	813	1.06 974	9 278			
774	842	7 927	814	1.07 105	029 809			
775	1.01 974	8 489	815	237	030 345			
776	1.02 105	9 047	816	368	0 875			
777	237	009 608	817	500	1 408			
778	368	010 164	818	632	1 941			
779	500	0 724	819	763	2 470			

REDUCTION OF THE VOLUME OF GASES TO 0°C.

This table contains the logarithms of the values of $\frac{1}{1 + 0.003670t}$ where $t = 0$ to 149° .

t	log	t	log	t	log	t	log
0.0	000 000	4.0	993 671	8.0	987 433	12.0	981 284
0.1	999 839	4.1	3 513	8.1	7 277	12.1	1 130
0.2	9 683	4.2	3 359	8.2	7 125	12.2	0 980
0.3	9 523	4.3	3 200	8.3	6 969	12.3	0 826
0.4	9 362	4.4	3 042	8.4	6 813	12.4	0 672
0.5	9 202	4.5	2 884	8.5	6 657	12.5	0 518
0.6	9 045	4.6	2 730	8.6	6 505	12.6	0 368
0.7	8 885	4.7	2 572	8.7	6 350	12.7	0 215
0.8	8 725	4.8	2 414	8.8	6 194	12.8	980 062
0.9	8 569	4.9	2 260	8.9	6 043	12.9	979 912
1.0	998 409	5.0	992 103	9.0	985 888	13.0	979 759
1.1	8 249	5.1	1 945	9.1	5 732	13.1	9 606
1.2	8 093	5.2	1 792	9.2	5 581	13.2	9 457
1.3	7 934	5.3	1 634	9.3	5 425	13.3	9 304
1.4	7 774	5.4	1 477	9.4	5 270	13.4	9 150
1.5	7 618	5.5	1 323	9.5	5 119	13.5	9 002
1.6	7 458	5.6	1 166	9.6	4 963	13.6	8 848
1.7	7 304	5.7	1 008	9.7	4 808	13.7	8 695
1.8	7 137	5.8	0 850	9.8	4 653	13.8	8 542
1.9	6 984	5.9	0 697	9.9	4 502	13.9	8 393
2.0	996 824	6.0	990 540	10.0	984 347	14.0	978 240
2.1	6 664	6.1	0 383	10.1	4 192	14.1	8 087
2.2	6 509	6.2	0 231	10.2	4 041	14.2	7 938
2.3	6 350	6.3	990 073	10.3	3 887	14.3	7 786
2.4	6 191	6.4	989 916	10.4	3 732	14.4	7 634
2.5	6 032	6.5	9 759	10.5	3 577	14.5	7 481
2.6	5 877	6.6	9 607	10.6	3 426	14.6	7 333
2.7	5 718	6.7	9 450	10.7	3 271	14.7	7 180
2.8	5 559	6.8	9 293	10.8	3 117	14.8	7 028
2.9	5 404	6.9	9 141	10.9	2 967	14.9	6 880
3.0	995 244	7.0	988 983	11.0	982 813	15.0	976 727
3.1	5 086	7.1	8 828	11.1	2 658	15.1	6 575
3.2	4 931	7.2	8 675	11.2	2 507	15.2	6 427
3.3	4 772	7.3	8 519	11.3	2 353	15.3	6 274
3.4	4 614	7.4	8 362	11.4	2 199	15.4	6 122
3.5	4 459	7.5	8 210	11.5	2 049	15.5	5 974
3.6	4 301	7.6	8 054	11.6	1 895	15.6	5 822
3.7	4 142	7.7	7 897	11.7	1 741	15.7	5 665
3.8	3 984	7.8	7 741	11.8	1 587	15.8	5 517
3.9	3 829	7.9	7 588	11.9	1 437	15.9	5 370

t	log	t	log	t	log	t	log
16.0	975 229	20.0	969 238	24.0	963 339	28.0	957 519
16.1	5 067	20.1	9 089	24.1	3 192	28.1	7 373
16.2	4 919	20.2	8 943	24.2	3 048	28.2	7 236
16.3	4 768	20.3	8 794	24.3	2 900	28.3	7 095
16.4	4 616	20.4	8 644	24.4	2 753	28.4	6 941
16.5	4 465	20.5	8 495	24.5	2 606	28.5	6 795
16.6	4 318	20.6	8 350	24.6	2 462	28.6	6 654
16.7	4 166	20.7	8 200	24.7	2 315	28.7	6 508
16.8	4 015	20.8	8 051	24.8	2 167	28.8	6 363
16.9	3 867	20.9	7 905	24.9	2 024	28.9	6 221
17.0	973 717	21.0	967 756	25.0	961 876	29.0	956 076
17.1	3 565	21.1	7 606	25.1	1 729	29.1	5 931
17.2	3 418	21.2	7 461	25.2	1 586	29.2	5 789
17.3	3 267	21.3	7 313	25.3	1 440	29.3	5 644
17.4	3 116	21.4	7 164	25.4	1 293	29.4	5 499
17.5	2 968	21.5	7 019	25.5	1 150	29.5	5 358
17.6	2 817	21.6	6 870	25.6	1 003	29.6	5 213
17.7	2 666	21.7	6 721	25.7	0 856	29.7	5 068
17.8	2 516	21.8	6 572	25.8	0 709	29.8	4 923
17.9	2 369	21.9	6 427	25.9	0 566	29.9	4 783
18.0	972 219	22.0	966 279	26.0	960 419	30.0	954 638
18.1	2 068	22.1	6 130	26.1	0 272	30.1	4 493
18.2	1 922	22.2	5 986	26.2	960 130	30.2	4 353
18.3	1 771	22.3	5 837	26.3	959 983	30.3	4 208
18.4	1 620	22.4	5 689	26.4	9 837	30.4	4 063
18.5	1 470	22.5	5 541	26.5	9 690	30.5	3 918
18.6	1 323	22.6	5 396	26.6	9 548	30.6	3 778
18.7	1 173	22.7	5 248	26.7	9 402	30.7	3 634
18.8	1 022	22.8	5 099	26.8	9 255	30.8	3 489
18.9	0 876	22.9	4 955	26.9	9 113	30.9	3 349
19.0	970 726	23.0	964 807	27.0	958 966	31.0	953 205
19.1	0 575	23.1	4 658	27.1	8 820	31.1	3 060
19.2	0 430	23.2	4 514	27.2	8 678	31.2	2 920
19.3	0 280	23.3	4 366	27.3	8 532	31.3	2 776
19.4	970 130	23.4	4 218	27.4	8 387	31.4	2 632
19.5	969 981	23.5	4 074	27.5	8 245	31.5	2 492
19.6	9 829	23.6	3 926	27.6	8 099	31.6	2 348
19.7	9 682	23.7	3 778	27.7	7 953	31.7	2 204
19.8	9 534	23.8	3 630	27.8	7 806	31.8	2 060
19.9	9 388	23.9	3 487	27.9	7 664	31.9	1 920

TABLE XIII (CONTINUED)

t	log	t	log	t	log	t	log
32.0	951 776	35	947 518	70	900 700	110	852 726
32.1	1 632	36	6 114	71	899 433	111	1 592
32.2	1 492	37	4 702	72	8 170	112	850 461
32.3	1 349	38	3 303	73	6 912	113	849 333
32.4	1 205	39	1 905	74	5 656	114	8 208
32.5	1 061			75	4 405	115	7 085
32.6	0 922			76	3 156	116	5 965
32.7	0 778			77	1 912	117	4 849
32.8	0 635			78	0 671	118	3 736
32.9	0 495			79	889 434	119	2 625
33.0	950 351	40	940 513	80	888 200	120	841 517
33.1	0 208	41	939 125	81	6 970	121	840 412
33.2	950 069	42	7 741	82	5 743	122	839 309
33.3	949 926	43	6 363	83	4 519	123	8 210
33.4	9 783	44	4 988	84	3 299	124	7 113
33.5	9 643	45	3 618	85	2 083	125	6 019
33.6	9 500	46	2 252	86	880 869	126	4 928
33.7	9 358	47	930 891	87	879 660	127	3 839
33.8	9 215	48	9 534	88	8 453	128	2 754
33.9	9 075	49	8 181	89	7 250	129	1 671
34.0	948 932	50	926 832	90	876 050	130	830 591
		51	5 487	91	4 854	131	829 513
		52	4 147	92	3 661	132	8 438
		53	2 810	93	2 471	133	7 365
		54	1 478	94	1 284	134	6 295
		55	920 150	95	870 101	135	5 228
		56	918 826	96	868 920	136	4 164
		57	7 506	97	7 743	137	3 102
		58	6 189	98	6 570	138	2 043
		59	4 877	99	5 399	139	820 986
		60	913 569	100	864 231	140	819 932
		61	2 265	101	3 067	141	8 880
		62	910 964	102	1 906	142	7 831
		63	909 668	103	860 748	143	6 784
		64	8 375	104	859 593	144	5 741
		65	7 087	105	8 441	145	4 699
		66	5 801	106	7 292	146	3 660
		67	4 520	107	6 146	147	2 623
		68	3 243	108	5 003	148	1 589
		69	1 969	109	3 863	149	0 558

REDUCTION OF THE VOLUME OF GASES SATURATED WITH AQUEOUS
VAPOR TO 0°, NORMAL PRESSURE, AND DRY

$$V_0 = V \frac{p_0 - h}{(1 + 0.003670 t) 760}$$

(V is the volume of the gas, p the uncorrected barometric pressure read on a glass or wooden scale, p_0 barometric pressure corrected for temperature, h the maximum tension of aqueous vapor, t the temperature. This table contains the logarithms of

$$\frac{p_0 - h}{(1 + 0.003670 t) 760},$$

where p varies from 730 to 780 and t from 12° to 24°.)

(Landolt-Börnstein)

t	p = 730 log	Differ- ence for 10 mm.	p = 740 log	Differ- ence for 10 mm.	p = 750 log	Differ- ence for 10 mm.	p = 760 log	Differ- ence for 10 mm.	p = 770 log	Differ- ence for 10 mm.	p = 780 log
12.0	95 663	599	96 262	591	96 853	584	97 437	575	98 012	568	98 580
12.2	622	600	222	591	813	583	396	576	97 972	568	540
12.4	582	599	181	592	773	583	356	576	932	568	500
12.6	541	600	141	592	733	583	316	576	892	568	460
12.8	501	599	100	592	692	584	276	576	852	568	420
13.0	95 460	600	96 060	592	96 652	584	97 236	576	97 812	568	98 380
13.2	419	600	96 019	592	611	584	195	576	771	569	340
13.4	378	601	95 979	592	571	584	155	576	731	569	300
13.6	337	601	938	592	530	584	114	577	691	568	259
13.8	296	601	897	592	489	584	073	577	650	569	219
14.0	95 256	600	95 856	592	96 448	585	97 033	576	97 609	570	98 179
14.2	214	601	815	592	407	585	96 992	577	569	569	138
14.4	173	601	774	592	366	585	951	577	528	569	097
14.6	131	601	732	593	325	585	910	577	487	570	057
14.8	090	601	691	593	284	585	869	577	446	570	016
15.0	95 048	602	95 650	593	96 243	585	96 828	577	97 405	570	97 975
15.2	95 007	601	608	593	201	585	786	578	364	570	934
15.4	94 965	601	566	594	160	585	745	578	323	570	893
15.6	923	602	525	593	118	586	704	577	281	570	851
15.8	881	602	483	594	077	585	662	578	240	570	810
16.0	94 839	602	95 441	594	96 035	585	96 620	578	97 198	571	97 769
16.2	797	602	399	594	95 993	586	579	578	157	570	727
16.4	755	602	357	594	951	586	537	578	115	571	686
16.6	712	603	315	594	909	586	495	578	073	571	644
16.8	670	602	272	595	867	586	453	579	032	570	602

TABLE XIV (CONTINUED)

t	p = 730 log	Differ- ence for 10 mm.	p = 740 log	Differ- ence for 10 mm.	p = 750 log	Differ- ence for 10 mm.	p = 760 log	Differ- ence for 10 mm.	p = 770 log	Differ- ence for 10 mm.	p = 780 log
17.0	94 627	603	95 230	594	95 824	587	96 411	579	96 990	571	97 561
17.2	585	602	187	595	782	587	369	578	947	572	519
17.4	542	603	145	595	740	586	326	579	905	572	477
17.6	499	603	102	595	697	587	284	579	863	571	434
17.8	456	603	059	595	654	587	241	580	821	571	392
18.0	94 413	603	95 016	596	95 612	587	96 199	579	96 778	572	97 350
18.2	370	603	94 973	596	569	587	156	580	736	571	307
18.4	326	604	930	596	526	587	113	580	693	572	265
18.6	283	604	887	596	483	587	070	580	650	572	222
18.8	239	604	843	596	439	588	027	580	607	573	180
19.0	94 196	604	94 800	596	95 396	588	95 984	580	96 564	573	97 137
19.2	152	604	756	597	353	588	941	580	521	573	094
19.4	108	605	713	596	309	588	897	581	478	573	051
19.6	064	605	669	596	265	589	854	580	434	573	97 007
19.8	020	605	625	596	221	589	810	581	391	573	96 964
20.0	93 975	606	94 581	597	95 178	588	95 766	581	96 347	574	96 921
20.2	931	605	536	597	133	589	722	582	304	573	877
20.4	886	606	492	597	089	589	678	582	260	573	833
20.6	842	606	448	597	045	589	634	582	216	574	790
20.8	797	606	403	598	001	589	590	582	172	574	746
21.0	93 752	606	94 358	598	94 956	590	95 546	581	96 127	575	96 702
21.2	707	606	313	598	911	590	501	582	083	574	657
21.4	662	606	268	598	866	591	457	582	96 039	574	613
21.6	616	607	223	598	821	591	412	582	95 994	575	569
21.8	571	607	178	598	776	591	367	582	949	575	524
22.0	93 525	607	94 132	599	94 731	591	95 322	583	95 905	575	96 480
22.2	479	608	087	599	686	591	277	583	860	575	435
22.4	433	608	94 041	599	640	591	231	583	814	576	390
22.6	387	608	93 995	600	595	591	186	583	769	576	345
22.8	341	608	949	600	549	591	140	584	724	575	299
23.0	93 295	608	93 903	600	94 503	591	95 094	584	95 678	576	96 254
23.2	248	609	857	600	457	592	049	583	632	577	209
23.4	202	608	810	601	411	592	95 003	584	587	576	163
23.6	155	609	764	600	364	592	94 956	585	541	576	117
23.8	108	609	717	601	318	592	910	585	495	576	071
24.0	93 061	609	93 670	601	94 271	593	94 864	584	95 448	577	96 025

OBSERVED DENSITY AND THE WEIGHT OF A LITER OF SOME COMMON GASES UNDER THE FOLLOWING CONDITIONS: 0° AND 760 M.M. PRESSURE AT SEA LEVEL AND 45° LATITUDE. AIR = 1

Substance	Density	Wt. 1 liter in grams at sea level and 45° lat.	log	Observer
Acetylene	0.92	1.1620	065 206	Berthelot
Air	1.00	1.2928	111 532	Leduc
Ammonia	0.5971	0.7621	882 012	Lord Rayleigh
Argon	1.379	1.782	250 908	Leduc
Bromine	{ 5.5243 at 227.92° }	7.1426	853 856	Ramsay and Travers
Carbon dioxide	1.52909	1.9652	293 407	Jahn
Carbon monoxide	0.96716	1.2506	097 118	Lord Rayleigh
Chlorine	2.491	3.1666	500 593	Leduc
Ethane	1.075	1.3421	127 785	Kolbe
Ethylene	0.9852	1.2520	097 604	Saussure
Hydrogen	0.06926	0.09004	954 435	Regnault
Hydrogen sulphide	1.1895	1.5230	182 700	Leduc
Hydrobromic acid	2.71	3.6163	558 265	Löwig
Hydrochloric acid	1.2692	1.6283	211 734	Leduc
Hydriodic acid	4.3757	5.7106	756 682	Thomson
Methane	0.5576	0.7160	854 913	Thomson
Methyl ether	1.617	2.0567	313 171	Dumas and Peligot
Nitrogen	0.96737	1.2542	098 367	Lord Rayleigh
Nitrogen dioxide	1.0372	1.3417	127 655	Leduc
Nitrogen monoxide	1.5301	1.9688	294 202	Leduc
Oxygen	1.10535	1.4292	155 093	Lord Rayleigh
Sulphur dioxide	2.2639	2.8611	456 533	Leduc

DENSITY OF DRY ATMOSPHERIC AIR AT 760 MM. PRESSURE AND
TEMPERATURES RANGING FROM 0° TO 35°

$$\left(\text{Values of } d_{t, 760} = \frac{.0012928}{1 + .003670 t} \right)$$

t	d _{t, 760}	log	t	d _{t, 760}	log	t	d _{t, 760}	log
0.0	0.0 012 928	111 531	4.0	0.0 012 741	105 204	8.0	0.0 012 559	098 955
0.1	12 923	1 363	4.1	12 736	5 033	8.1	12 555	8 817
0.2	12 919	1 229	4.2	12 732	4 897	8.2	12 550	8 644
0.3	12 914	1 061	4.3	12 728	4 760	8.3	12 546	8 505
0.4	12 909	0 893	4.4	12 723	4 590	8.4	12 541	8 332
0.5	12 904	0 724	4.5	12 718	4 419	8.5	12 537	8 194
0.6	12 900	0 590	4.6	12 713	4 248	8.6	12 532	8 020
0.7	12 895	0 421	4.7	12 709	4 111	8.7	12 528	7 882
0.8	12 890	0 253	4.8	12 704	3 941	8.8	12 524	7 743
0.9	12 885	110 084	4.9	12 700	3 804	8.9	12 519	7 570
1.0	0.0 012 881	109 950	5.0	0.0 012 695	103 633	9.0	0.0 012 515	097 431
1.1	12 876	9 781	5.1	12 690	3 462	9.1	12 511	7 292
1.2	12 871	9 612	5.2	12 686	3 325	9.2	12 506	7 118
1.3	12 867	9 477	5.3	12 681	3 154	9.3	12 501	6 945
1.4	12 862	9 309	5.4	12 677	3 017	9.4	12 497	6 806
1.5	12 857	9 140	5.5	12 672	2 845	9.5	12 492	6 632
1.6	12 853	9 005	5.6	12 668	2 708	9.6	12 488	6 493
1.7	12 848	8 836	5.7	12 663	2 537	9.7	12 484	6 354
1.8	12 843	8 667	5.8	12 659	2 399	9.8	12 479	6 180
1.9	12 838	8 497	5.9	12 654	2 228	9.9	12 475	6 041
2.0	0.0 012 834	108 362	6.0	0.0 012 649	102 056	10.0	0.0 012 470	095 867
2.1	12 829	8 193	6.1	12 645	1 919	10.1	12 466	5 727
2.2	12 824	8 024	6.2	12 640	1 747	10.2	12 462	5 588
2.3	12 820	7 888	6.3	12 636	1 610	10.3	12 457	5 414
2.4	12 815	7 719	6.4	12 631	1 438	10.4	12 453	5 274
2.5	12 810	7 549	6.5	12 627	1 300	10.5	12 448	5 100
2.6	12 806	7 414	6.6	12 622	1 128	10.6	12 444	4 960
2.7	12 801	7 244	6.7	12 618	0 991	10.7	12 440	4 820
2.8	12 797	7 108	6.8	12 613	0 818	10.8	12 435	4 646
2.9	12 792	6 939	6.9	12 609	0 681	10.9	12 431	4 506
3.0	0.0 012 787	106 769	7.0	0.0 012 604	100 508	11.0	0.0 012 426	094 331
3.1	12 783	6 633	7.1	12 600	0 371	11.1	12 422	4 192
3.2	12 778	6 463	7.2	12 595	0 198	11.2	12 418	4 052
3.3	12 773	6 293	7.3	12 591	100 060	11.3	12 413	3 877
3.4	12 769	6 157	7.4	12 586	099 888	11.4	12 409	3 737
3.5	12 764	5 987	7.5	12 582	9 750	11.5	12 404	3 562
3.6	12 759	5 817	7.6	12 577	9 577	11.6	12 400	3 422
3.7	12 755	5 681	7.7	12 573	9 439	11.7	12 396	3 282
3.8	12 750	5 510	7.8	12 568	9 266	11.8	12 391	3 106
3.9	12 746	5 374	7.9	12 564	9 128	11.9	12 387	2 966

t	d _t , 760	log	t	d _t , 760	log	t	d _t , 760	log
12.0	0.0 012 383	092 826	16.0	0.0 012 211	086 751	20.0	0.0 012 044	080 770
12.1	12 378	2 651	16.1	12 207	6 609	20.1	12 040	0 627
12.2	12 374	2 510	16.2	12 203	6 467	20.2	12 036	0 482
12.3	12 370	2 370	16.3	12 198	6 289	20.3	12 032	0 338
12.4	12 365	2 194	16.4	12 194	6 146	20.4	12 028	0 193
12.5	12 361	2 054	16.5	12 190	6 004	20.5	12 023	080 013
12.6	12 357	1 913	16.6	12 186	5 861	20.6	12 019	079 868
12.7	12 352	1 737	16.7	12 181	5 683	20.7	12 015	9 724
12.8	12 348	1 597	16.8	12 177	5 540	20.8	12 011	9 579
12.9	12 344	1 456	16.9	12 173	5 398	20.9	12 007	9 435
13.0	0.0 012 339	091 280	17.0	0.0 012 169	085 255	21.0	0.0 012 003	079 290
13.1	12 335	1 139	17.1	12 165	5 112	21.1	11 999	9 145
13.2	12 331	0 998	17.2	12 160	4 934	21.2	11 995	9 000
13.3	12 326	0 822	17.3	12 156	4 791	21.3	11 991	8 855
13.4	12 322	0 681	17.4	12 152	4 648	21.4	11 987	8 711
13.5	12 318	0 540	17.5	12 148	4 505	21.5	11 982	8 529
13.6	12 313	0 364	17.6	12 144	4 362	21.6	11 978	8 384
13.7	12 309	0 223	17.7	12 139	4 183	21.7	11 974	8 239
13.8	12 305	090 082	17.8	12 135	4 040	21.8	11 970	8 094
13.9	12 301	089 940	17.9	12 131	3 897	21.9	11 966	7 949
14.0	0.0 012 296	089 764	18.0	0.0 012 127	083 753	22.0	0.0 011 962	077 804
14.1	12 292	9 623	18.1	12 123	3 610	22.1	11 958	7 659
14.2	12 288	9 481	18.2	12 119	3 467	22.2	11 954	7 513
14.3	12 283	9 305	18.3	12 114	3 288	22.3	11 950	7 368
14.4	12 279	9 163	18.4	12 110	3 144	22.4	11 946	7 223
14.5	12 275	9 022	18.5	12 106	3 001	22.5	11 942	7 077
14.6	12 270	8 845	18.6	12 102	2 857	22.6	11 938	6 932
14.7	12 266	8 703	18.7	12 098	2 714	22.7	11 934	6 786
14.8	12 262	8 561	18.8	12 094	2 570	22.8	11 930	6 640
14.9	12 258	8 420	18.9	12 089	2 390	22.9	11 926	6 495
15.0	0.0 012 253	088 242	19.0	0.0 012 085	082 247	23.0	0.0 011 922	076 349
15.1	12 249	8 101	19.1	12 081	2 103	23.1	11 918	6 203
15.2	12 245	7 959	19.2	12 077	1 959	23.2	11 914	6 058
15.3	12 241	7 817	19.3	12 073	1 815	23.3	11 910	5 912
15.4	12 236	7 640	19.4	12 069	1 671	23.4	11 906	5 766
15.5	12 232	7 498	19.5	12 065	1 527	23.5	11 902	5 620
15.6	12 228	7 355	19.6	12 060	1 347	23.6	11 898	5 474
15.7	12 224	7 213	19.7	12 056	1 203	23.7	11 894	5 328
15.8	12 219	7 036	19.8	12 052	1 059	23.8	11 889	5 145
15.9	12 215	6 894	19.9	12 048	0 915	23.9	11 885	4 999

TABLE XVI (CONTINUED)

t	d _t , 760	log	t	d _t , 760	log	t	d _t , 760	log
24.0	0.0 011 881	074 853	28.0	0.0 011 723	069 039	32.0	0.0 011 569	063 296
24.1	11 877	4 707	28.1	11 719	8 891	32.1	11 566	3 183
24.2	11 873	4 561	28.2	11 716	8 779	32.2	11 562	3 033
24.3	11 869	4 414	28.3	11 712	8 631	32.3	11 558	2 883
24.4	11 865	4 268	28.4	11 708	8 483	32.4	11 554	2 732
24.5	11 861	4 121	28.5	11 704	8 334	32.5	11 550	2 582
24.6	11 857	3 975	28.6	11 700	8 186	32.6	11 547	2 469
24.7	11 853	3 828	28.7	11 696	8 037	32.7	11 543	2 319
24.8	11 849	3 682	28.8	11 692	7 889	32.8	11 539	2 168
24.9	11 846	3 572	28.9	11 688	7 740	32.9	11 535	2 018
25.0	0.0 011 842	073 425	29.0	0.0 011 684	067 592	33.0	0.0 011 531	061 867
25.1	11 838	3 278	29.1	11 681	7 480	33.1	11 528	1 754
25.2	11 834	3 132	29.2	11 677	7 331	33.2	11 524	1 603
25.3	11 830	2 985	29.3	11 673	7 183	33.3	11 520	1 453
25.4	11 826	2 838	29.4	11 669	7 034	33.4	11 516	1 302
25.5	11 822	2 691	29.5	11 665	6 885	33.5	11 513	1 189
25.6	11 818	2 544	29.6	11 661	6 736	33.6	11 509	1 038
25.7	11 814	2 397	29.7	11 657	6 587	33.7	11 505	0 887
25.8	11 810	2 250	29.8	11 654	6 475	33.8	11 501	0 736
25.9	11 806	2 103	29.9	11 650	6 326	33.9	11 497	0 585
26.0	0.0 011 802	071 956	30.0	0.0 011 646	066 177	34.0	0.0 011 494	060 471
26.1	11 798	1 808	30.1	11 642	6 028	34.1	11 490	0 320
26.2	11 794	1 661	30.2	11 638	5 878	34.2	11 486	0 169
26.3	11 790	1 514	30.3	11 634	5 729	34.3	11 483	060 055
26.4	11 786	1 366	30.4	11 630	5 580	34.4	11 479	059 904
26.5	11 782	1 219	30.5	11 627	5 468	34.5	11 475	9 753
26.6	11 778	1 072	30.6	11 623	5 318	34.6	11 471	9 601
26.7	11 774	0 924	30.7	11 619	5 169	34.7	11 468	9 488
26.8	11 770	0 777	30.8	11 615	5 019	34.8	11 464	9 336
26.9	11 768	0 703	30.9	11 611	4 870	34.9	11 460	9 185
27.0	0.0 011 762	070 481	31.0	0.0 011 607	064 720	35.0	0.0 011 456	059 033
27.1	11 759	0 370	31.1	11 603	4 570			
27.2	11 755	0 223	31.2	11 600	4 458			
27.3	11 751	070 075	31.3	11 596	4 308			
27.4	11 747	069 927	31.4	11 592	4 158			
27.5	11 743	9 779	31.5	11 588	4 009			
27.6	11 739	9 631	31.6	11 585	3 896			
27.7	11 735	9 483	31.7	11 581	3 746			
27.8	11 731	9 335	31.8	11 577	3 596			
27.9	11 727	9 187	31.9	11 573	3 446			

TABLE XVII

(Ostwald-Luther. Physiko-chemische Messungen)

Degrees C.	Apparent weight of a cc. of water	log	Volume of an apparent gram of water	log
10	.9 986	999 392	1.0 014	.000 608
11	85	9 348	15	0 651
12	84	9 305	16	0 694
13	83	9 261	17	0 738
14	82	9 218	18	0 781
15	81	9 174	19	0 824
16	79	9 087	21	0 911
17	77	9 000	23	0 998
18	76	8 956	24	1 041
19	74	8 869	26	1 128
20	72	8 782	28	1 214
21	70	8 695	30	1 301
22	67	8 565	33	1 431
23	65	8 477	35	1 517
24	63	8 390	37	1 604
25	60	8 259	40	1 734

SPECIFIC VOLUME OF WATER

(Thiesen, Scheel, and Diesselhorst, Wiss. Abh. d. Phys. Techn. Reichsanst. 3, 69)

Hydrogen Scale

Degrees	Tenth Degrees									
	0	1	2	3	4	5	6	7	8	9
0	1.000 132	126	119	113	107	101	095	089	084	079
1	073	069	064	059	055	051	047	043	039	035
2	032	029	026	023	020	018	016	013	011	009
3	008	006	005	004	003	002	001	001	000	000
4	000	000	000	001	001	002	003	004	005	007
5	008	010	012	014	016	018	021	023	026	029
6	032	035	039	042	046	050	054	058	062	066
7	071	075	080	085	090	096	101	107	112	118
8	124	130	137	143	149	156	163	170	177	184
9	192	199	207	215	223	231	239	247	256	264
10	273	282	291	300	309	319	328	338	348	358
11	368	378	388	399	409	420	431	442	453	464
12	476	487	499	511	522	534	547	559	571	584
13	596	609	622	635	648	661	675	688	702	715
14	729	743	757	772	786	800	815	830	844	859
15	874	890	905	920	936	951	967	983	999	*015
16	1.001 031	048	064	081	098	114	131	148	165	183
17	200	218	235	253	271	289	307	325	343	361
18	380	399	417	436	455	474	493	513	532	551
19	571	591	610	630	650	671	691	711	732	752
20	773	794	815	836	857	878	899	921	942	964
21	985	*007	*029	*051	*073	*096	*118	*140	*163	*186
22	1.002 208	231	254	277	300	324	347	370	394	418
23	441	465	489	513	538	562	586	611	635	660
24	685	710	735	760	785	810	835	861	886	912
25	938	964	990	*016	*042	*068	*094	*121	*147	*174
26	1.003 201	227	254	281	308	336	363	390	418	445
27	473	501	529	556	585	613	641	669	698	726
28	755	783	812	841	870	899	928	957	987	*016
29	1.004 046	075	105	135	165	194	225	255	285	315
30	346	376	407	437	468	499	530	561	592	623
31	655	686	717	749	781	812	844	876	908	940
32	972	*005	*037	*070	*102	*135	*167	*200	*233	*266
33	1.005 299	332	365	399	432	465	499	533	566	600
34	634	668	702	736	771	805	839	874	908	943
35	978	*013	*047	*082	*118	*153	*188	*223	*259	*294

DENSITY OF WATER

(Thiesen, Scheel, and Diesselhorst, Wiss. Abh. d. Phys. Techn. Reichsanst. 3, 68)

Hydrogen Scale

Degrees	Tenth Degrees									
	0	1	2	3	4	5	6	7	8	9
0	0.999 868	874	881	887	893	899	905	911	916	922
1	927	932	936	941	945	950	954	957	961	965
2	968	971	974	977	980	982	985	987	989	991
3	992	994	995	996	997	998	999	999	*000	*000
4	1.000 000	000	000	*999	*999	*998	*997	*996	*995	*993
5	0.999 992	990	988	986	984	982	979	977	974	971
6	968	965	962	958	954	951	947	943	938	934
7	929	925	920	915	910	904	899	893	888	882
8	876	870	864	857	851	844	837	830	823	816
9	808	801	793	785	778	769	761	753	744	736
10	727	718	709	700	691	681	672	662	652	642
11	632	622	612	601	591	580	569	558	547	536
12	525	513	502	490	478	466	454	442	429	417
13	404	391	379	366	353	339	326	312	299	285
14	271	257	243	229	215	200	186	171	156	141
15	126	111	096	081	065	050	034	018	002	*986
16	0.998 970	953	937	920	904	887	870	853	836	819
17	801	784	766	749	731	713	695	677	659	640
18	622	603	585	566	547	528	509	490	471	451
19	432	412	392	372	352	332	312	292	271	251
20	230	210	189	168	147	126	105	083	062	040
21	019	*997	*975	*953	*931	*909	*887	*864	*842	*819
22	0.997 797	774	751	728	705	682	659	635	612	588
23	565	541	517	493	469	445	421	396	372	347
24	323	298	273	248	223	198	173	147	122	096
25	071	045	019	*994	*968	*941	*915	*889	*863	*836
26	0.996 810	783	756	730	703	676	648	621	594	567
27	539	512	484	456	428	400	372	344	316	288
28	259	231	202	174	145	116	087	058	029	000
29	0.995 971	941	912	882	853	823	793	763	733	703
30	673	643	613	582	552	521	491	460	429	398
31	367	336	305	273	242	211	179	148	116	084
32	052	020	*988	*956	*924	*892	*859	*827	*794	*762
33	0.994 729	696	663	630	597	564	531	498	464	431
34	398	364	330	296	263	229	195	161	126	092
35	058	023	*989	*954	*920	*885	*850	*815	*780	*745

THE PROPORTION BY WEIGHT OF ABSOLUTE ALCOHOL IN 100 PARTS OF SPIRITS OF DIFFERENT SPE- CIFIC GRAVITIES (Fownes)						THE PROPORTION BY VOLUME OF ABSOLUTE ALCOHOL IN 100 VOL- UMES OF SPIRITS OF DIFFERENT SPECIFIC GRAVITIES (Gay-Lussac)					
Sp. G. at 15.5°	Per cent of real alco- hol	Sp. G. at 15.5°	Per cent of real alco- hol	Sp. G. at 15.5°	Per cent of real alco- hol	Sp. G. at 15°	100 vol. spirits con- tain vol. of real alco- hol	Sp. G. at 15°	100 vol. spirits con- tain vol. of real alco- hol	Sp. G. at 15°	100 vol. spirits con- tain vol. of real alco- hol
.9991	0.5	.9511	34	.8769	68	.9985	1	.9594	35	.8932	69
.9981	1	.9490	35	.8745	69	.9970	2	.9581	36	.8907	70
.9965	2	.9470	36	.8721	70	.9956	3	.9567	37	.8882	71
.9947	3	.9452	37	.8696	71	.9942	4	.9553	38	.8857	72
.9930	4	.9434	38	.8672	72	.9929	5	.9538	39	.8831	73
.9914	5	.9416	39	.8649	73	.9916	6	.9523	40	.8805	74
.9898	6	.9396	40	.8625	74	.9903	7	.9507	41	.8779	75
.9884	7	.9376	41	.8603	75	.9891	8	.9491	42	.8753	76
.9869	8	.9356	42	.8581	76	.9878	9	.9474	43	.8726	77
.9855	9	.9335	43	.8557	77	.9867	10	.9457	44	.8699	78
.9841	10	.9314	44	.8533	78	.9855	11	.9440	45	.8672	79
.9828	11	.9292	45	.8508	79	.9844	12	.9422	46	.8645	80
.9815	12	.9270	46	.8483	80	.9833	13	.9404	47	.8617	81
.9802	13	.9249	47	.8459	81	.9822	14	.9386	48	.8589	82
.9789	14	.9228	48	.8434	82	.9812	15	.9367	49	.8560	83
.9778	15	.9206	49	.8408	83	.9802	16	.9348	50	.8531	84
.9766	16	.9184	50	.8382	84	.9792	17	.9329	51	.8502	85
.9753	17	.9160	51	.8357	85	.9782	18	.9309	52	.8472	86
.9741	18	.9135	52	.8331	86	.9773	19	.9289	53	.8442	87
.9728	19	.9113	53	.8305	87	.9763	20	.9269	54	.8411	88
.9716	20	.9090	54	.8279	88	.9753	21	.9248	55	.8379	89
.9704	21	.9069	55	.8254	89	.9742	22	.9227	56	.8346	90
.9691	22	.9047	56	.8228	90	.9732	23	.9206	57	.8312	91
.9678	23	.9025	57	.8199	91	.9721	24	.9185	58	.8278	92
.9665	24	.9001	58	.8172	92	.9711	25	.9163	59	.8242	93
.9652	25	.8979	59	.8145	93	.9700	26	.9141	60	.8206	94
.9638	26	.8956	60	.8118	94	.9690	27	.9119	61	.8168	95
.9623	27	.8932	61	.8089	95	.9679	28	.9096	62	.8128	96
.9609	28	.8908	62	.8061	96	.9668	29	.9073	63	.8086	97
.9593	29	.8886	63	.8031	97	.9657	30	.9050	64	.8042	98
.9578	30	.8863	64	.8001	98	.9645	31	.9027	65	.8006	99
.9560	31	.8840	65	.7969	99	.9633	32	.9004	66	.7947	100
.9544	32	.8816	66	.7938	100	.9621	33	.8980	67		
.9528	33	.8793	67			.9608	34	.8956	68		

SPECIFIC GRAVITY OF SOLUTIONS OF AMMONIUM HYDROXIDE AT 15° C.

(Lunge and Wiernik, Zeit. f. angew. Chem., 1889, 181)

Sp. G. at $\frac{15^{\circ}}{4}$ in vacuo	Per cent NH ₃ grams	1 liter contains NH ₃ grams	Sp. G. at $\frac{15^{\circ}}{4}$ in vacuo	Per cent NH ₃ grams	1 liter contains NH ₃ grams	Sp. G. at $\frac{15^{\circ}}{4}$ in vacuo	Per cent NH ₃ grams	1 liter contains NH ₃ grams
1.000	.00	0.0	0.960	9.91	95.1	0.920	21.75	200.1
0.998	.45	4.5	958	10.47	100.3	918	22.39	205.6
996	.91	9.1	956	11.03	105.4	916	23.03	210.9
994	1.37	13.6	954	11.60	110.7	914	23.68	216.3
992	1.84	18.2	952	12.17	115.9	912	24.33	221.9
990	2.31	22.9	950	12.74	121.0	910	24.99	227.4
988	2.80	27.7	948	13.31	126.2	908	25.65	232.9
986	3.30	32.5	946	13.88	131.3	906	26.31	238.3
984	3.80	37.4	944	14.46	136.5	904	26.98	243.9
982	4.30	42.2	942	15.04	141.7	902	27.65	249.4
980	4.80	47.0	940	15.63	146.9	900	28.33	255.0
978	5.30	51.8	938	16.22	152.1	898	29.01	260.5
976	5.80	56.6	936	16.82	157.4	896	29.69	266.0
974	6.30	61.4	934	17.42	162.7	894	30.37	271.5
972	6.80	66.1	932	18.03	168.1	892	31.05	277.0
970	7.31	70.9	930	18.64	173.4	890	31.75	282.6
968	7.82	75.7	928	19.25	178.6	888	32.50	288.6
966	8.33	80.5	926	19.87	184.2	886	33.25	294.6
964	8.84	85.2	924	20.49	189.3	884	34.10	301.4
962	9.35	89.9	922	21.12	194.7	882	34.95	308.3

TABLE XXII

SPECIFIC GRAVITY OF SOLUTIONS OF HYDROCHLORIC ACID AT 15° C.

(Lunge and Marchlewski, Zeit. angew. Chem., 1891, 135)

Sp. G. at $\frac{15^{\circ}}{4}$ in vacuo	100 pts. by wt. contain grams HCl	1 liter contains grams HCl	Sp. g. at $\frac{15^{\circ}}{4}$ in vacuo	100 pts. by wt. contain grams HCl	1 liter contains grams HCl	Sp. G. at $\frac{15^{\circ}}{4}$ in vacuo	100 pts. by wt. contain grams HCl	1 liter contains grams HCl
1.000	0.16	1.6	1.070	14.17	152	1.140	27.66	315
1.005	1.15	12.0	1.075	15.16	163	1.145	28.61	328
1.010	2.14	22.0	1.080	16.15	174	1.150	29.57	340
1.015	3.12	32.0	1.085	17.13	186	1.155	30.55	353
1.020	4.13	42.0	1.090	18.11	197	1.160	31.52	366
1.025	5.15	53	1.095	19.06	209	1.165	32.49	379
1.030	6.15	64	1.100	20.01	220	1.170	33.46	392
1.035	7.15	74	1.105	20.97	232	1.175	34.42	404
1.040	8.16	85	1.110	21.92	243	1.180	35.39	418
1.045	9.16	96	1.115	22.86	255	1.185	36.31	430
1.050	10.17	107	1.120	23.82	267	1.190	37.23	443
1.055	11.18	118	1.125	24.78	278	1.195	38.16	456
1.060	12.19	129	1.130	25.75	291	1.200	39.11	469
1.065	13.19	141	1.135	26.70	303			

CONSTANT BOILING SOLUTION OF HYDROCHLORIC ACID

(Hulett and Bonner, Jour. Am. Chem. Soc., 31, 390)

Barometric pressure	Per cent HCl	Grams constant boiling distillate containing 1 mol HCl
770	20.218	180.390
760	20.242	180.170
750	20.266	179.960
740	20.290	179.745
730	20.314	179.530

The easiest and most accurate method of preparing standard solutions of hydrochloric acid is to weigh out a definite amount of the constant boiling solution of hydrochloric acid and dilute this to a certain volume. The constant boiling solution is obtained by diluting the concentrated hydrochloric acid of the laboratory with an equal volume of water. Distill from a retort or distilling flask connected with a condenser. When three fourths has been distilled off, change the receiver and collect as much of the remainder as is desirable. The last fraction is the constant boiling solution, and if the barometric pressure is noted, the exact weight of this solution which when diluted to a liter yields a normal solution can be ascertained by reference to the table.

SPECIFIC GRAVITY OF NITRIC ACID AT 15° C.

(Lunge and Rey, Zeit. angew. Chem., 1891, 165)

Specific gravity at 15° in vacuo	100 pts. by wt. contain grams HNO_3	1 liter contains grams HNO_3	Specific gravity at 15° in vacuo	100 pts. by wt. contain grams HNO_3	1 liter contains grams HNO_3	Specific gravity at 15° in vacuo	100 pts. by wt. contain grams HNO_3	1 liter contains grams HNO_3
1.000	0.10	1	1.205	33.09	399	1.410	67.50	952
1.005	1.00	10	1.210	33.82	409	1.415	68.63	971
1.010	1.90	19	1.215	34.55	420	1.420	69.80	991
1.015	2.80	28	1.220	35.28	430	1.425	70.98	1011
1.020	3.70	38	1.225	36.03	441	1.430	72.17	1032
1.025	4.60	47	1.230	36.78	452	1.435	73.39	1053
1.030	5.50	57	1.235	37.53	463	1.440	74.68	1075
1.035	6.38	66	1.240	38.29	475	1.445	75.98	1098
1.040	7.26	75	1.245	39.05	486	1.450	77.28	1121
1.045	8.13	85	1.250	39.82	498	1.455	78.60	1144
1.050	8.99	94	1.255	40.58	509	1.460	79.98	1168
1.055	9.84	104	1.260	41.34	521	1.465	81.42	1193
1.060	10.68	113	1.265	42.10	533	1.470	82.90	1219
1.065	11.51	123	1.270	42.87	544	1.475	84.45	1246
1.070	12.33	132	1.275	43.64	556	1.480	86.05	1274
1.075	13.15	141	1.280	44.41	568	1.485	87.70	1302
1.080	13.95	151	1.285	45.18	581	1.490	89.60	1335
1.085	14.74	160	1.290	45.95	593	1.495	91.60	1369
1.090	15.53	169	1.295	46.72	603	1.500	94.09	1411
1.095	16.32	179	1.300	47.49	617	1.501	94.60	1420
1.100	17.11	188	1.305	48.26	630	1.502	95.08	1428
1.105	17.89	198	1.310	49.07	643	1.503	95.55	1436
1.110	18.67	207	1.315	49.89	656	1.504	96.00	1444
1.115	19.45	217	1.320	50.71	669	1.505	96.39	1451
1.120	20.23	227	1.325	51.53	683	1.506	96.76	1457
1.125	21.00	236	1.330	52.37	697	1.507	97.13	1464
1.130	21.77	246	1.335	53.22	710	1.508	97.50	1470
1.135	22.54	256	1.340	54.07	725	1.509	97.84	1476
1.140	23.31	266	1.345	54.93	739	1.510	98.10	1481
1.145	24.08	276	1.350	55.79	753	1.511	98.32	1486
1.150	24.84	286	1.355	56.66	768	1.512	98.53	1490
1.155	25.60	296	1.360	57.57	783	1.513	98.73	1494
1.160	26.36	306	1.365	58.48	798	1.514	98.90	1497
1.165	27.12	316	1.370	59.39	814	1.515	99.01	1501
1.170	27.88	326	1.375	60.30	829	1.516	99.21	1504
1.175	28.63	336	1.380	61.27	846	1.517	99.34	1507
1.180	29.38	347	1.385	62.24	862	1.518	99.46	1510
1.185	30.13	357	1.390	63.23	879	1.519	99.57	1512
1.190	30.88	367	1.395	64.25	896	1.520	99.67	1515
1.195	31.62	378	1.400	65.30	914			
1.200	32.36	388	1.405	66.40	933			

SPECIFIC GRAVITY OF SULPHURIC ACID AT 15° C.

(Lunge, Isler and Naef, Zeit. angew. Chem., 1890, 131)

Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H ₂ SO ₄	1 liter contains grams H ₂ SO ₄	Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H ₂ SO ₄	1 liter contains grams H ₂ SO ₄	Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H ₂ SO ₄	1 liter contains grams H ₂ SO ₄
1.000	.09	1	1.225	30.48	373	1.450	55.03	798
1.005	.83	8	1.230	31.11	382	1.455	55.50	808
1.010	1.57	16	1.235	31.70	391	1.460	55.97	817
1.015	2.30	23	1.240	32.28	400	1.465	56.43	827
1.020	3.03	31	1.245	32.86	409	1.470	56.90	837
1.025	3.76	39	1.250	33.43	418	1.475	57.37	846
1.030	4.49	46	1.255	34.00	426	1.480	57.83	856
1.035	5.23	54	1.260	34.57	435	1.485	58.28	865
1.040	5.96	62	1.265	35.14	444	1.490	58.74	876
1.045	6.67	71	1.270	35.71	454	1.495	59.22	885
1.050	7.37	77	1.275	36.29	462	1.500	59.70	896
1.055	8.07	85	1.280	36.87	472	1.505	60.18	906
1.060	8.77	93	1.285	37.45	481	1.510	60.65	916
1.065	9.47	102	1.290	38.03	490	1.515	61.12	926
1.070	10.19	109	1.295	38.61	500	1.520	61.59	936
1.075	10.90	117	1.300	39.19	510	1.525	62.06	946
1.080	11.60	125	1.305	39.77	519	1.530	62.53	957
1.085	12.30	133	1.310	40.35	529	1.535	63.00	967
1.090	12.99	142	1.315	40.93	538	1.540	63.43	977
1.095	13.67	150	1.320	41.50	548	1.545	63.85	987
1.100	14.35	158	1.325	42.08	557	1.550	64.26	996
1.105	15.03	166	1.330	42.66	567	1.555	64.67	1006
1.110	15.71	175	1.335	43.20	577	1.560	65.08	1015
1.115	16.36	183	1.340	43.74	586	1.565	65.49	1025
1.120	17.01	191	1.345	44.28	596	1.570	65.90	1035
1.125	17.66	199	1.350	44.82	605	1.575	66.30	1044
1.130	18.31	207	1.355	45.35	614	1.580	66.71	1054
1.135	18.96	215	1.360	45.88	624	1.585	67.13	1064
1.140	19.61	223	1.365	46.41	633	1.590	67.59	1075
1.145	20.26	231	1.370	46.94	643	1.595	68.05	1085
1.150	20.91	239	1.375	47.47	653	1.600	68.51	1096
1.155	21.55	248	1.380	48.00	662	1.605	68.97	1107
1.160	22.19	257	1.385	48.53	672	1.610	69.43	1118
1.165	22.83	266	1.390	49.06	682	1.615	69.89	1128
1.170	23.47	275	1.395	49.59	692	1.620	70.32	1139
1.175	24.12	283	1.400	50.11	702	1.625	70.74	1150
1.180	24.76	292	1.405	50.63	711	1.630	71.16	1160
1.185	25.40	301	1.410	51.15	721	1.635	71.57	1170
1.190	26.04	310	1.415	51.66	730	1.640	71.99	1181
1.195	26.68	319	1.420	52.15	740	1.645	72.40	1192
1.200	27.32	328	1.425	52.63	750	1.650	72.82	1202
1.205	27.95	337	1.430	53.11	759	1.655	73.23	1212
1.210	28.58	346	1.435	53.59	769	1.660	73.64	1222
1.215	29.21	355	1.440	54.07	779	1.665	74.07	1233
1.220	29.84	364	1.445	54.55	789	1.670	74.51	1244

SPECIFIC GRAVITY OF SULFURIC ACID AT 15° C.

(Lunge, Isler and Naef, Zeit. angew. Chem., 1890, 131)

Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H_2SO_4	1 liter contains grams H_2SO_4	Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H_2SO_4	1 liter contains grams H_2SO_4	Sp. G. at 15° in vacuo	100 pts. by wt. contain grams H_2SO_4	1 liter contains grams H_2SO_4
1.675	74.97	1256	1.775	83.90	1489	1.831	92.30	1690
1.680	75.42	1267	1.780	84.50	1504	1.832	92.52	1695
1.685	75.86	1278	1.785	85.10	1519	1.833	92.75	1700
1.690	76.30	1289	1.790	85.70	1534	1.834	93.05	1706
1.695	76.73	1301	1.795	86.30	1549	1.835	93.43	1713
1.700	77.17	1312	1.800	86.90	1564	1.836	93.80	1722
1.705	77.60	1323	1.805	87.60	1581	1.837	94.20	1730
1.710	78.04	1334	1.810	88.30	1598	1.838	94.60	1739
1.715	78.48	1346	1.815	89.05	1621	1.839	95.00	1748
1.720	78.92	1357	1.820	90.05	1639	1.840	95.60	1759
1.725	79.36	1369	1.821	90.20	1643	1.8405	95.95	1765
1.730	79.80	1381	1.822	90.40	1647	1.8410	97.00	1786
1.735	80.24	1392	1.823	90.60	1651	1.8415	97.70	1799
1.740	80.68	1404	1.824	90.80	1656	1.8410	98.20	1808
1.745	81.12	1416	1.825	91.00	1661	1.8405	98.70	1816
1.750	81.56	1427	1.826	91.25	1666	1.8400	99.20	1825
1.755	82.00	1439	1.827	91.50	1671	1.8395	99.45	1830
1.760	82.44	1451	1.828	91.70	1676	1.8390	99.70	1834
1.765	82.88	1463	1.829	91.90	1681	1.8385	99.95	1838
1.770	83.32	1475	1.830	92.10	1685			

CORRECTIONS FOR THE EXPOSED THREAD OF MERCURY THERMOMETERS

(Landolt-Börnstein)

$$n\beta(T-t)$$

n is the length of exposed thread expressed in terms of the thermometer graduations, β the apparent coefficient of expansion of mercury in glass, T the temperature read off, t , the mean temperature of the exposed thread. For temperatures lower than 100° β varies from $\frac{1}{6300}$ to $\frac{1}{6100}$, depending on the glass, and for higher temperatures the fraction is somewhat smaller.

 $\frac{1}{10}^\circ$ THERMOMETERS, GRADUATED FROM 0° TO 100°

(Length of degrees about 4 mm.)

$T - t =$	30°	35°	40°	45°	50°	55°	60°	65°	70°	75°	80°	85°
$n = 10^\circ$.05	.05	.05	.05	.05	.05	.05	.05	.1	.1	.1	.1
20°	.1	.1	.15	.15	.15	.15	.15	.20	.2	.2	.2	.25
30°	.2	.2	.25	.25	.25	.25	.25	.3	.3	.35	.35	.35
40°	.3	.3	.3	.35	.35	.35	.4	.4	.45	.45	.5	.5
50°	.35	.4	.4	.4	.45	.45	.5	.5	.55	.55	.6	.65
60°	.45	.5	.5	.55	.55	.55	.6	.65	.65	.7	.75	.8
70°						.65	.7	.7	.75	.8	.85	.9
80°							.75	.8	.85	.95	1.0	1.1
90°								.9	1.0	1.1	1.1	1.2
100°									1.1	1.2	1.3	1.3

THERMOMETERS GRADUATED FROM 0° TO 360°

(Length of degrees 1 to 1.6 mm.)

$T - t =$	70°	80°	90°	100°	110°	120°	130°	140°	150°	160°	170°	180°	190°	200°	210°	220°
$n = 10^\circ$	0.	.05	.05	.05	.1	.1	.1	.15	.2	.2	.2	.25	.3	.35	.35	.40
20°	.15	.15	.2	.2	.25	.3	.3	.4	.45	.45	.5	.55	.55	.60	.65	.65
30°	.25	.3	.35	.4	.45	.5	.55	.6	.65	.7	.75	.8	.85	.9	.95	.95
40°	.35	.4	.5	.55	.6	.7	.75	.8	.90	.95	1.0	1.0	1.1	1.2	1.2	1.3
50°	.45	.55	.6	.7	.8	.9	.95	1.0	1.1	1.2	1.2	1.3	1.4	1.4	1.5	1.6
60°	.55	.65	.75	.9	1.0	1.1	1.2	1.2	1.3	1.4	1.5	1.6	1.7	1.7	1.8	1.9
70°	.7	.8	.9	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	1.9	2.0	2.1	2.2
80°	.8	.9	1.0	1.2	1.4	1.5	1.6	1.7	1.8	1.9	2.0	2.1	2.2	2.3	2.4	2.5
90°	.9	1.0	1.2	1.4	1.6	1.7	1.9	2.0	2.1	2.2	2.3	2.4	2.5	2.6	2.8	2.9
100°	1.0	1.2	1.3	1.6	1.8	2.0	2.1	2.2	2.3	2.4	2.6	2.7	2.8	2.9	3.1	3.2
110°				1.8	2.0	2.2	2.3	2.4	2.5	2.7	2.8	3.0	3.1	3.3	3.4	3.6
120°				2.0	2.2	2.4	2.6	2.7	2.8	2.9	3.1	3.3	3.4	3.6	3.7	3.9
130°					2.4	2.7	2.8	2.9	3.0	3.2	3.4	3.6	3.7	3.9	4.1	4.3
140°					2.7	2.9	3.1	3.2	3.3	3.5	3.7	3.9	4.0	4.2	4.4	4.6
150°									3.5	3.7	4.0	4.1	4.3	4.6	4.8	5.0
160°									3.7	4.0	4.2	4.5	4.7	4.9	5.1	5.4
170°									4.0	4.3	4.5	4.8	5.0	5.2	5.5	5.8
180°									4.3	4.5	4.8	5.1	5.3	5.6	5.9	6.1
190°												5.4	5.6	5.9	6.2	6.5
200°												5.7	6.0	6.3	6.6	6.9
210°													6.3	6.7	7.0	7.3
220°													6.7	7.0	7.4	7.7

TABLE XXVII

FIXED POINTS OF THE THERMOMETRIC SCALE

(Transition temperatures)

	H. Scale	
$\text{Na}_2\text{CrO}_4 \cdot 10 \text{H}_2\text{O} - \text{Na}_2\text{CrO}_4 \cdot 6 \text{H}_2\text{O}$	19.525	Richards and Kelley
$\text{Na}_2\text{CrO}_4 \cdot 10 \text{H}_2\text{O} - \text{Na}_2\text{CrO}_4 \cdot 4 \text{H}_2\text{O}$	19.987	
$\text{Na}_2\text{CrO}_4 \cdot 6 \text{H}_2\text{O} - \text{Na}_2\text{CrO}_4 \cdot 4 \text{H}_2\text{O}$	25.90	
$\text{Na}_2\text{CO}_3 \cdot 10 \text{H}_2\text{O} - \text{Na}_2\text{CO}_3 \cdot 7 \text{H}_2\text{O}$	32.00	Wells and McAdam
$\text{Na}_2\text{CO}_3 \cdot 10 \text{H}_2\text{O} - \text{Na}_2\text{CO}_3 \cdot \text{H}_2\text{O}$	32.96	
$\text{Na}_2\text{CO}_3 \cdot 7 \text{H}_2\text{O} - \text{Na}_2\text{CO}_3 \cdot \text{H}_2\text{O}$	35.37	
$\text{Na}_2\text{SO}_4 \cdot 10 \text{H}_2\text{O} - \text{Na}_2\text{SO}_4$	32.383	Richards and Wells
$\text{NaBr} \cdot 2 \text{H}_2\text{O} - \text{NaBr}$	50.674	
$\text{MnCl}_2 \cdot 4 \text{H}_2\text{O} - \text{MnCl}_2 \cdot 2 \text{H}_2\text{O}$	58.089	Richards and Wrede

CORRECTIONS FOR LOSS OF WEIGHT IN AIR

The following table, calculated by Kohlrausch, contains corrections, C , expressed in milligrams, to be added algebraically to each gram of apparent weight of a substance, the specific gravity of which is S .

S	C	S	C	S	C
0.7	+ 1.57	2.0	+ 0.458	9	— 0.009
0.8	+ 1.36	2.5	+ 0.337	10	— 0.023
0.9	+ 1.19	3.0	+ 0.257	11	— 0.034
1.0	+ 1.06	3.5	+ 0.200	12	— 0.043
1.1	+ 0.95	4.0	+ 0.157	13	— 0.050
1.2	+ 0.86	4.5	+ 0.142	14	— 0.057
1.3	+ 0.78	5.0	+ 0.097	15	— 0.063
1.4	+ 0.71	5.5	+ 0.075	16	— 0.068
1.5	+ 0.66	6.0	+ 0.057	17	— 0.072
1.6	+ 0.61	6.5	+ 0.042	18	— 0.076
1.7	+ 0.56	7.0	+ 0.029	19	— 0.080
1.8	+ 0.52	7.5	+ 0.017	20	— 0.083
1.9	+ 0.49	8.0	+ 0.007		

The following values are of constant use in revising the atomic weights of the elements by means of their halides.

	Vacuum correction per apparent gram	
Ag	— 0.000031	gram
AgBr	+ 0.000041	gram
AgCl	+ 0.000075	gram
AgI	+ 0.000071	gram
	Specific gravity	Vacuum correction per apparent gram
Brass weights	8.3	— 0.000145
Glass	2.5	+ 0.000335

LOGARITHMS OF NUMBERS

(From 1 to 10,000)

N.	log	N.	log	N.	log	N.	log
1	0.000000	26	1.414973	51	1.707570	76	1.880814
2	0.301030	27	1.431364	52	1.716003	77	1.886491
3	0.477121	28	1.447158	53	1.724276	78	1.892095
4	0.602060	29	1.462398	54	1.732394	79	1.897627
5	0.698970	30	1.477121	55	1.740363	80	1.903090
6	0.778151	31	1.491362	56	1.748188	81	1.908485
7	0.845098	32	1.505150	57	1.755875	82	1.913814
8	0.903090	33	1.518514	58	1.763428	83	1.919078
9	0.954243	34	1.531479	59	1.770852	84	1.924279
10	1.000000	35	1.544068	60	1.778151	85	1.929419
11	1.041393	36	1.556303	61	1.785330	86	1.934498
12	1.079181	37	1.568202	62	1.792392	87	1.939519
13	1.113943	38	1.579784	63	1.799341	88	1.944483
14	1.146128	39	1.591065	64	1.806181	89	1.949390
15	1.176091	40	1.602060	65	1.812913	90	1.954243
16	1.204120	41	1.612784	66	1.819544	91	1.959041
17	1.230449	42	1.623249	67	1.826075	92	1.963788
18	1.255273	43	1.633468	68	1.832509	93	1.968483
19	1.278754	44	1.643453	69	1.838849	94	1.973128
20	1.301030	45	1.653213	70	1.845098	95	1.977724
21	1.322219	46	1.662758	71	1.851258	96	1.982271
22	1.342423	47	1.672098	72	1.857333	97	1.986772
23	1.361728	48	1.681241	73	1.863323	98	1.991226
24	1.380211	49	1.690196	74	1.869232	99	1.995635
25	1.397940	50	1.698970	75	1.875061	100	2.000000

REMARK. In the following table, in the nine right-hand columns of each page, where the first or leading figures change from 9's to 0's, asterisks are introduced instead of the 0's, to catch the eye, and to indicate that from thence the two figures of the logarithm to be taken from the second column stand in the next line below.

N.	0	1	2	3	4	5	6	7	8	9	D.
100	000000	0434	0868	1301	1734	2166	2598	3029	3461	3891	432
101	4321	4751	5181	5609	6038	6466	6894	7321	7748	8174	428
102	8600	9026	9451	9876	*300	*724	1147	1570	1993	2415	424
103	012837	3259	3680	4100	4521	4940	5360	5779	6197	6616	419
104	7033	7451	7868	8284	8700	9116	9532	9947	*361	*775	416
105	021189	1603	2016	2428	2841	3252	3664	4075	4486	4896	412
106	5306	5715	6125	6533	6942	7350	7757	8164	8571	8978	408
107	9384	9789	*195	*600	1004	1408	1812	2216	2619	3021	404
108	033424	3826	4227	4628	5029	5430	5830	6230	6629	7028	400
109	7426	7825	8223	8620	9017	9414	9811	*207	*602	*998	396
110	041393	1787	2182	2576	2969	3362	3755	4148	4540	4932	393
111	5323	5714	6105	6495	6885	7275	7664	8053	8442	8830	389
112	9218	9606	9993	*380	*766	1153	1538	1924	2309	2694	386
113	053078	3463	3846	4230	4613	4996	5378	5760	6142	6524	382
114	6905	7286	7666	8046	8426	8805	9185	9563	9942	*320	379
115	060698	1075	1452	1829	2206	2582	2958	3333	3709	4083	376
116	4458	4832	5206	5580	5953	6326	6699	7071	7443	7815	372
117	8186	8557	8928	9298	9668	**38	*407	*776	1145	1514	369
118	071882	2250	2617	2985	3352	3718	4085	4451	4816	5182	366
119	5547	5912	6276	6640	7004	7368	7731	8094	8457	8819	363
120	079181	9543	9904	*266	*626	*987	1347	1707	2067	2426	360
121	082785	3144	3503	3861	4219	4576	4934	5291	5647	6004	357
122	6360	6716	7071	7426	7781	8136	8490	8845	9198	9552	355
123	9905	*258	*611	*963	1315	1667	2018	2370	2721	3071	351
124	093422	3772	4122	4471	4820	5169	5518	5866	6215	6562	349
125	6910	7257	7604	7951	8298	8644	8990	9335	9681	**26	346
126	100371	0715	1059	1403	1747	2091	2434	2777	3119	3462	343
127	3804	4146	4487	4828	5169	5510	5851	6191	6531	6871	340
128	7210	7549	7888	8227	8565	8903	9241	9579	9916	*253	338
129	110590	0926	1263	1599	1934	2270	2605	2940	3275	3609	335
130	113943	4277	4611	4944	5278	5611	5943	6276	6608	6940	333
131	7271	7603	7934	8265	8595	8926	9256	9586	9915	*245	330
132	120574	0903	1231	1560	1888	2216	2544	2871	3198	3525	328
133	3852	4178	4504	4830	5156	5481	5806	6131	6456	6781	325
134	7105	7429	7753	8076	8399	8722	9045	9368	9690	**12	323
135	130334	0655	0977	1298	1619	1939	2260	2580	2900	3219	321
136	3539	3858	4177	4496	4814	5133	5451	5769	6086	6403	318
137	6721	7037	7354	7671	7987	8303	8618	8934	9249	9564	315
138	9879	*194	*508	*822	1136	1450	1763	2076	2389	2702	314
139	143015	3327	3639	3951	4263	4574	4885	5196	5507	5818	311
140	146128	6438	6748	7058	7367	7676	7985	8294	8603	8911	309
141	9219	9527	9835	*142	*449	*756	1063	1370	1676	1982	307
142	152288	2594	2900	3205	3510	3815	4120	4424	4728	5032	305
143	5336	5640	5943	6246	6549	6852	7154	7457	7759	8061	303
144	8362	8664	8965	9266	9567	9868	*168	*469	*769	1068	301
145	161368	1667	1967	2266	2564	2863	3161	3460	3758	4055	299
146	4353	4650	4947	5244	5541	5838	6134	6430	6726	7022	297
147	7317	7613	7908	8203	8497	8792	9086	9380	9674	9968	295
148	170262	0555	0848	1141	1434	1726	2019	2311	2603	2895	293
149	3186	3478	3769	4060	4351	4641	4932	5222	5512	5802	291
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151	8977	9264	9552	9839	*126	*413	*699	*985	1272	1558	287
152	181844	2129	2415	2700	2985	3270	3555	3839	4123	4407	285
153	4691	4975	5259	5542	5825	6108	6391	6674	6956	7239	283
154	7521	7803	8084	8366	8647	8928	9209	9490	9771	**51	281
155	190332	0612	0892	1171	1451	1730	2010	2289	2567	2846	279
156	3125	3403	3681	3959	4237	4514	4792	5069	5346	5623	278
157	5899	6176	6453	6729	7005	7281	7556	7832	8107	8382	276
158	8657	8932	9206	9481	9755	**29	*303	*577	*850	1124	274
159	201397	1670	1943	2216	2488	2761	3033	3305	3577	3848	272
160	204120	4391	4663	4934	5204	5475	5746	6016	6286	6556	271
161	6826	7096	7365	7634	7904	8173	8441	8710	8979	9247	269
162	9515	9783	**51	*319	*586	*853	1121	1388	1654	1921	267
163	212188	2454	2720	2986	3252	3518	3783	4049	4314	4579	266
164	4844	5109	5373	5638	5902	6166	6430	6694	6957	7221	264
165	7484	7747	8010	8273	8536	8798	9060	9323	9585	9846	262
166	220108	0370	0631	0892	1153	1414	1675	1936	2196	2456	261
167	2716	2976	3236	3496	3755	4015	4274	4533	4792	5051	259
168	5309	5568	5826	6084	6342	6600	6858	7115	7372	7630	258
169	7887	8144	8400	8657	8913	9170	9426	9682	9938	*193	256
170	230449	0704	0960	1215	1470	1724	1979	2234	2488	2742	254
171	2996	3250	3504	3757	4011	4264	4517	4770	5023	5276	253
172	5528	5781	6033	6285	6537	6789	7041	7292	7544	7795	252
173	8046	8297	8548	8799	9049	9299	9550	9800	**50	*300	250
174	240549	0799	1048	1297	1546	1795	2044	2293	2541	2790	249
175	3038	3286	3534	3782	4030	4277	4525	4772	5019	5266	248
176	5513	5759	6006	6252	6499	6745	6991	7237	7482	7728	246
177	7973	8219	8464	8709	8954	9198	9443	9687	9932	*176	245
178	250420	0664	0908	1151	1395	1638	1881	2125	2368	2610	243
179	2853	3096	3338	3580	3822	4064	4306	4548	4790	5031	242
180	255273	5514	5755	5996	6237	6477	6718	6958	7198	7439	241
181	7679	7918	8158	8398	8637	8877	9116	9355	9594	9833	239
182	260071	0310	0548	0787	1025	1263	1501	1739	1976	2214	238
183	2451	2688	2925	3162	3399	3636	3873	4109	4346	4582	237
184	4818	5054	5290	5525	5761	5996	6232	6467	6702	6937	235
185	7172	7406	7641	7875	8110	8344	8578	8812	9046	9279	234
186	9513	9746	9980	*213	*446	*679	*912	1144	1377	1609	233
187	271842	3074	2306	2538	2770	3001	3233	3464	3696	3927	232
188	4158	4389	4620	4850	5081	5311	5542	5772	6002	6232	230
189	6462	6692	6921	7151	7380	7609	7838	8067	8296	8525	229
190	278754	8982	9211	9439	9667	9895	*123	*351	*578	*806	228
191	281033	1261	1488	1715	1942	2169	2396	2622	2849	3075	227
192	3301	3527	3753	3979	4205	4431	4656	4882	5107	5332	226
193	5557	5782	6007	6232	6456	6681	6905	7130	7354	7578	225
194	7802	8026	8249	8473	8696	8920	9143	9366	9589	9812	223
195	290035	0257	0480	0702	0925	1147	1369	1591	1813	2034	222
196	2256	2478	2699	2920	3141	3363	3584	3804	4025	4246	221
197	4466	4687	4907	5127	5347	5567	5787	6007	6226	6446	220
198	6665	6884	7104	7323	7542	7761	7979	8198	8416	8635	219
199	8853	9071	9289	9507	9725	9943	*161	*378	*595	*813	218
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TABLE XXIX (CONTINUED)

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201	3196	3412	3628	3844	4059	4275	4491	4706	4921	5136	216
202	5351	5566	5781	5996	6211	6425	6639	6854	7068	7282	215
203	7496	7710	7924	8137	8351	8564	8778	8991	9204	9417	213
204	9630	9843	*56	*268	*481	*693	*906	1118	1330	1542	212
205	311754	1966	2177	2389	2600	2812	3023	3234	3445	3656	211
206	3867	4078	4289	4499	4710	4920	5130	5340	5551	5760	210
207	5970	6180	6390	6599	6809	7018	7227	7436	7646	7854	209
208	8063	8272	8481	8689	8898	9106	9314	9522	9730	9938	208
209	320146	0354	0562	0769	0977	1184	1391	1598	1805	2012	207
210	322219	2426	2633	2839	3046	3252	3458	3665	3871	4077	206
211	4282	4488	4694	4899	5105	5310	5516	5721	5926	6131	205
212	6336	6541	6745	6950	7155	7359	7563	7767	7972	8176	204
213	8380	8583	8787	8991	9194	9398	9601	9805	***8	*211	203
214	330414	0617	0819	1022	1225	1427	1630	1832	2034	2236	202
215	2438	2640	2842	3044	3246	3447	3649	3850	4051	4253	202
216	4454	4655	4856	5057	5257	5458	5658	5859	6059	6260	201
217	6460	6660	6860	7060	7260	7459	7659	7858	8058	8257	200
218	8456	8656	8855	9054	9253	9451	9650	9849	**47	*246	199
219	340444	0642	0841	1039	1237	1435	1632	1830	2028	2225	198
220	342423	2620	2817	3014	3212	3409	3606	3802	3999	4196	197
221	4392	4589	4785	4981	5178	5374	5570	5766	5962	6157	196
222	6353	6549	6744	6939	7135	7330	7525	7720	7915	8110	195
223	8305	8500	8694	8889	9083	9278	9472	9666	9860	***4	194
224	350248	0402	0636	0829	1023	1216	1410	1603	1796	1989	193
225	2183	2375	2568	2761	2954	3147	3339	3532	3724	3916	193
226	4108	4301	4493	4685	4876	5068	5260	5452	5643	5834	192
227	6026	6217	6408	6599	6790	6981	7172	7363	7554	7744	191
228	7935	8125	8316	8506	8696	8886	9076	9266	9456	9646	190
229	9835	**25	*215	*404	*593	*783	*972	1161	1350	1539	189
230	361728	1917	2105	2294	2482	2671	2859	3048	3236	3424	188
231	3612	3800	3988	4176	4363	4551	4739	4926	5113	5301	188
232	5488	5675	5862	6049	6236	6423	6610	6796	6983	7169	187
233	7356	7542	7729	7915	8101	8287	8473	8659	8845	9030	186
234	9216	9401	9587	9772	9958	*143	*328	*513	*698	*883	185
235	371068	1253	1437	1622	1806	1991	2175	2360	2544	2728	184
236	2912	3096	3280	3464	3647	3831	4015	4198	4382	4565	184
237	4748	4932	5115	5298	5481	5664	5846	6029	6212	6394	183
238	6577	6759	6942	7124	7306	7488	7670	7852	8034	8216	182
239	8398	8580	8761	8943	9124	9306	9487	9668	9849	**30	181
240	380211	0392	0573	0754	0934	1115	1296	1476	1656	1837	181
241	2017	2197	2377	2557	2737	2917	3097	3277	3456	3636	180
242	3815	3995	4174	4353	4533	4712	4891	5070	5249	5428	179
243	5606	5785	5964	6142	6321	6499	6677	6856	7034	7212	178
244	7390	7568	7746	7923	8101	8279	8456	8634	8811	8989	178
245	9166	9343	9520	9698	9875	**51	*228	*405	*582	*759	177
246	390935	1112	1288	1464	1641	1817	1993	2169	2345	2521	176
247	2697	2873	3048	3224	3400	3575	3751	3926	4101	4277	176
248	*4452	4627	4802	4977	5152	5326	5501	5676	5850	6025	175
249	6199	6374	6548	6722	6896	7071	7245	7419	7592	7766	174
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250	397940	8114	8287	8461	8634	8808	8981	9154	9328	9501	173
251	9674	9847	**20	*192	*365	*538	*711	*883	1056	1228	173
252	401401	1573	1745	1917	2089	2261	2433	2605	2777	2949	172
253	3121	3292	3464	3635	3807	3978	4149	4320	4492	4663	171
254	4834	5005	5176	5346	5517	5688	5858	6029	6199	6370	171
255	6540	6710	6881	7051	7221	7391	7561	7731	7901	8070	170
256	8240	8410	8579	8749	8918	9087	9257	9426	9595	9764	169
257	9933	*102	*271	*440	*609	*777	*946	1114	1283	1451	169
258	411620	1788	1956	2124	2293	2461	2629	2796	2964	3132	168
259	3300	3467	3635	3803	3970	4137	4305	4472	4639	4806	167
260	414973	5140	5307	5474	5641	5808	5974	6141	6308	6474	167
261	6641	6807	6973	7139	7306	7472	7638	7804	7970	8135	166
262	8301	8467	8633	8798	8964	9129	9295	9460	9625	9791	165
263	9956	*121	*286	*451	*616	*781	*945	1110	1275	1439	165
264	421604	1788	1933	2097	2261	2426	2590	2754	2918	3082	164
265	3246	3410	3574	3737	3901	4065	4228	4392	4555	4718	164
266	4882	5045	5208	5371	5534	5697	5860	6023	6186	6349	163
267	6511	6674	6836	6999	7161	7324	7486	7648	7811	7973	162
268	8135	8297	8459	8621	8783	8944	9106	9268	9429	9591	162
269	9752	9914	**75	*236	*398	*559	*720	*881	1042	1203	161
270	431364	1525	1685	1846	2007	2167	2328	2488	2649	2809	161
271	2969	3130	3290	3450	3610	3770	3930	4090	4249	4409	160
272	4569	4729	4888	5048	5207	5367	5526	5685	5844	6004	159
273	6163	6322	6481	6640	6798	6957	7116	7275	7433	7592	159
274	7751	7909	8067	8226	8384	8542	8701	8859	9017	9175	158
275	9333	9491	9648	9806	9964	*122	*279	*437	*594	*752	158
276	440909	1066	1224	1381	1538	1695	1852	2009	2166	2323	157
277	2480	2637	2793	2950	3106	3263	3419	3576	3732	3889	157
278	4045	4201	4357	4513	4669	4825	4981	5137	5293	5449	156
279	5604	5760	5915	6071	6226	6382	6537	6692	6848	7003	155
280	447158	7313	7468	7623	7778	7933	8088	8242	8397	8552	155
281	8706	8861	9015	9170	9324	9478	9633	9787	9941	**95	154
282	450249	0403	0557	0711	0865	1018	1172	1326	1479	1633	154
283	1786	1940	2093	2247	2400	2553	2706	2859	3012	3165	153
284	3318	3471	3624	3777	3930	4082	4235	4387	4540	4692	153
285	4845	4997	5150	5302	5454	5606	5758	5910	6062	6214	152
286	6366	6518	6670	6821	6973	7125	7276	7428	7579	7731	152
287	7882	8033	8184	8336	8487	8638	8789	8940	9091	9242	151
288	9392	9543	9694	9845	9995	*146	*296	*447	*597	*748	151
289	460898	1048	1198	1348	1499	1649	1799	1948	2098	2248	150
290	462398	2548	2697	2847	2997	3146	3296	3445	3594	3744	150
291	3893	4042	4191	4340	4490	4639	4788	4936	5085	5234	149
292	5383	5532	5680	5829	5977	6126	6274	6423	6571	6719	149
293	6868	7016	7164	7312	7460	7608	7756	7904	8052	8200	148
294	8347	8495	8643	8790	8938	9085	9233	9380	9527	9675	148
295	9822	9969	*116	*263	*410	*557	*704	*851	*998	1145	147
296	471292	1438	1585	1732	1878	2025	2171	2318	2464	2610	146
297	2756	2903	3049	3195	3341	3487	3633	3779	3925	4071	146
298	4216	4362	4508	4653	4799	4944	5090	5235	5381	5526	146
299	5671	5816	5962	6107	6252	6397	6542	6687	6832	6976	145
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TABLE XXIX (CONTINUED)

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301	8566	8711	8855	8999	9143	9287	9431	9575	9719	9863	144
302	480007	0151	0294	0438	0582	0725	0869	1012	1156	1299	144
303	1443	1586	1729	1872	2016	2159	2302	2445	2588	2731	143
304	2874	3016	3159	3302	3445	3587	3730	3872	4015	4157	143
305	4300	4442	4585	4727	4869	5011	5153	5295	5437	5579	142
306	5721	5863	6005	6147	6289	6430	6572	6714	6855	6997	142
307	7138	7280	7421	7563	7704	7845	7986	8127	8269	8410	141
308	8551	8692	8833	8974	9114	9255	9396	9537	9677	9818	141
309	9958	**99	*239	*380	*520	*661	*801	*941	1081	1222	140
310	491362	1502	1642	1782	1922	2062	2201	2341	2481	2621	140
311	2760	2900	3040	3179	3319	3458	3597	3737	3876	4015	139
312	4155	4294	4433	4572	4711	4850	4989	5128	5267	5406	139
313	5544	5683	5822	5960	6099	6238	6376	6515	6653	6791	139
314	6930	7068	7206	7344	7483	7621	7759	7897	8035	8173	138
315	8311	8448	8586	8724	8862	8999	9137	9275	9412	9550	138
316	9687	9824	9962	**99	*236	*374	*511	*648	*785	*922	137
317	501059	1196	1333	1470	1607	1744	1880	2017	2154	2291	137
318	2427	2564	2700	2837	2973	3109	3246	3382	3518	3655	136
319	3791	3927	4063	4199	4335	4471	4607	4743	4878	5014	136
320	505150	5286	5421	5557	5693	5828	5964	6099	6234	6370	136
321	6505	6640	6776	6911	7046	7181	7316	7451	7586	7721	135
322	7856	7991	8126	8260	8395	8530	8664	8799	8934	9068	135
323	9203	9337	9471	9606	9740	9874	***9	*143	*277	*411	134
324	510545	0679	0813	0947	1081	1215	1349	1482	1616	1750	134
325	1883	2017	2151	2284	2418	2551	2684	2818	2951	3084	133
326	3218	3351	3484	3617	3750	3883	4016	4149	4282	4414	133
327	4548	4681	4813	4946	5079	5211	5344	5476	5609	5741	133
328	5874	6006	6139	6271	6403	6535	6668	6800	6932	7064	132
329	7196	7328	7460	7592	7724	7855	7987	8119	8251	8382	132
330	518514	8646	8777	8909	9040	9171	9303	9434	9566	9697	131
331	9828	9959	**90	*221	*353	*484	*615	*745	*876	1007	131
332	521138	1269	1400	1530	1661	1792	1922	2053	2183	2314	131
333	2444	2575	2705	2835	2966	3096	3226	3356	3486	3616	130
334	3746	3876	4006	4136	4266	4396	4526	4656	4785	4915	130
335	5045	5174	5304	5434	5563	5693	5822	5951	6081	6210	129
336	6339	6469	6598	6727	6856	6985	7114	7243	7372	7501	129
337	7630	7759	7888	8016	8145	8274	8402	8531	8660	8788	129
338	8917	9045	9174	9302	9430	9559	9687	9815	9943	**72	128
339	530200	0328	0456	0584	0712	0840	0968	1096	1223	1351	128
340	531479	1607	1734	1862	1990	2117	2245	2372	2500	2627	128
341	2754	2882	3009	3136	3264	3391	3518	3645	3772	3899	127
342	4026	4153	4280	4407	4534	4661	4787	4914	5041	5167	127
343	5294	5421	5547	5674	5800	5927	6053	6180	6306	6432	126
344	6558	6685	6811	6937	7063	7189	7315	7441	7567	7693	126
345	7819	7945	8071	8197	8322	8448	8574	8699	8825	8951	126
346	9076	9202	9327	9452	9578	9703	9829	9954	**79	*204	125
347	540329	0455	0580	0705	0830	0955	1080	1205	1330	1454	125
348	1579	1704	1829	1953	2078	2203	2327	2452	2576	2701	125
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351	5307	5431	5555	5678	5802	5925	6049	6172	6296	6419	124
352	6543	6666	6789	6913	7036	7159	7282	7405	7529	7652	123
353	7775	7898	8021	8144	8267	8389	8512	8635	8758	8881	123
354	9003	9126	9249	9371	9494	9616	9739	9861	9984	*106	123
355	550228	0351	0473	0595	0717	0840	0962	1084	1206	1328	122
356	1450	1572	1694	1816	1938	2060	2181	2303	2425	2547	122
357	2668	2790	2911	3033	3155	3276	3398	3519	3640	3762	121
358	3883	4004	4126	4247	4368	4489	4610	4731	4852	4973	121
359	5094	5215	5336	5457	5578	5699	5820	5940	6061	6182	121
360	556303	6423	6544	6664	6785	6905	7026	7146	7267	7387	120
361	7507	7627	7748	7868	7988	8108	8228	8349	8469	8589	120
362	8709	8829	8948	9068	9188	9308	9428	9548	9667	9787	120
363	9907	**26	*146	*265	*385	*504	*624	*743	*863	*982	119
364	561101	1221	1340	1459	1578	1698	1817	1936	2055	2174	119
365	2293	2412	2531	2650	2769	2887	3006	3125	3244	3362	119
366	3481	3600	3718	3837	3955	4074	4192	4311	4429	4548	119
367	4666	4784	4903	5021	5139	5257	5376	5494	5612	5730	118
368	5848	5966	6084	6202	6320	6437	6555	6673	6791	6909	118
369	7026	7144	7262	7379	7497	7614	7732	7849	7967	8084	118
370	568202	8319	8436	8554	8671	8788	8905	9023	9140	9257	117
371	9374	9491	9608	9725	9842	9959	**76	*193	*309	*426	117
372	570543	0660	0776	0893	1010	1126	1243	1359	1476	1592	117
373	1709	1825	1942	2058	2174	2291	2407	2523	2639	2755	116
374	2872	2988	3104	3220	3336	3452	3568	3684	3800	3915	116
375	4031	4147	4263	4379	4494	4610	4726	4841	4957	5072	116
376	5188	5303	5419	5534	5650	5765	5880	5996	6111	6226	115
377	6341	6457	6572	6687	6802	6917	7032	7147	7262	7377	115
378	7492	7607	7722	7836	7951	8066	8181	8295	8410	8525	115
379	8639	8754	8868	8983	9097	9212	9326	9441	9555	9669	114
380	579784	9898	**12	*126	*241	*355	*469	*583	*697	*811	114
381	580925	1039	1153	1267	1381	1495	1608	1722	1836	1950	114
382	2063	2177	2291	2404	2518	2631	2745	2858	2972	3085	114
383	3199	3312	3426	3539	3652	3765	3879	3992	4105	4218	113
384	4331	4444	4557	4670	4783	4896	5009	5122	5235	5348	113
385	5461	5574	5686	5799	5912	6024	6137	6250	6362	6475	113
386	6587	6700	6812	6925	7037	7149	7262	7374	7486	7599	112
387	7711	7823	7935	8047	8160	8272	8384	8496	8608	8720	112
388	8832	8944	9056	9167	9279	9391	9503	9615	9726	9838	112
389	9950	**61	*173	*284	*396	*507	*619	*730	*842	*953	112
390	591065	1176	1287	1399	1510	1621	1732	1843	1955	2066	111
391	2177	2288	2399	2510	2621	2732	2843	2954	3064	3175	111
392	3286	3397	3508	3618	3729	3840	3950	4061	4171	4282	111
393	4393	4503	4614	4724	4834	4945	5055	5165	5276	5386	110
394	5496	5606	5717	5827	5937	6047	6157	6267	6377	6487	110
395	6597	6707	6817	6927	7037	7146	7256	7366	7476	7586	110
396	7695	7805	7914	8024	8134	8243	8353	8462	8572	8681	110
397	8791	8900	9009	9119	9228	9337	9446	9556	9665	9774	109
398	9883	9992	*101	*210	*319	*428	*537	*646	*755	*864	109
399	600973	1082	1191	1299	1408	1517	1625	1734	1843	1951	109
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402	4226	4334	4442	4550	4658	4766	4874	4982	5089	5197	108
403	5305	5413	5521	5628	5736	5844	5951	6059	6166	6274	108
404	6381	6489	6596	6704	6811	6919	7026	7133	7241	7348	107
405	7455	7562	7669	7777	7884	7991	8098	8205	8312	8419	107
406	8526	8633	8740	8847	8954	9061	9167	9274	9381	9488	107
407	9594	9701	9808	9914	**21	*128	*234	*341	*447	*554	107
408	610660	0767	0873	0979	1086	1192	1298	1405	1511	1617	106
409	1723	1829	1936	2042	2148	2254	2360	2466	2572	2678	106
410	612784	2890	2996	3102	3207	3313	3419	3525	3630	3736	106
411	3842	3947	4053	4159	4264	4370	4475	4581	4686	4792	106
412	4897	5003	5108	5213	5319	5424	5529	5634	5740	5845	105
413	5950	6055	6160	6265	6370	6476	6581	6686	6790	6895	105
414	7000	7105	7210	7315	7420	7525	7629	7734	7839	7943	105
415	8048	8153	8257	8362	8466	8571	8676	8780	8884	8989	105
416	9093	9198	9302	9406	9511	9615	9719	9824	9928	**32	104
417	620136	0240	0344	0448	0552	0656	0760	0864	0968	1072	104
418	1176	1280	1384	1488	1592	1695	1799	1903	2007	2110	104
419	2214	2318	2421	2525	2628	2732	2835	2939	3042	3146	104
420	623249	3353	3456	3559	3663	3766	3869	3973	4076	4179	103
421	4282	4385	4488	4591	4695	4798	4901	5004	5107	5210	103
422	5312	5415	5518	5621	5724	5827	5929	6032	6135	6238	103
423	6340	6443	6546	6648	6751	6853	6956	7058	7161	7263	103
424	7366	7468	7571	7673	7775	7878	7980	8082	8185	8287	102
425	8389	8491	8593	8695	8797	8900	9002	9104	9206	9308	102
426	9410	9512	9613	9715	9817	9919	**21	*123	*224	*326	102
427	630428	0530	0631	0733	0835	0936	1038	1139	1241	1342	102
428	1444	1545	1647	1748	1849	1951	2052	2153	2255	2356	101
429	2457	2559	2660	2761	2862	2963	3064	3165	3266	3367	101
430	633468	3569	3670	3771	3872	3973	4074	4175	4276	4376	100
431	4477	4578	4679	4779	4880	4981	5081	5182	5283	5383	100
432	5484	5584	5685	5785	5886	5986	6087	6187	6287	6388	100
433	6488	6588	6688	6789	6889	6989	7089	7189	7290	7390	100
434	7490	7590	7690	7790	7890	7990	8090	8190	8290	8389	99
435	8489	8589	8689	8789	8888	8988	9088	9188	9287	9387	99
436	9486	9586	9686	9785	9885	9984	**84	*183	*283	*382	99
437	640481	0581	0680	0779	0879	0978	1077	1177	1276	1375	99
438	1474	1573	1672	1771	1871	1970	2069	2168	2267	2366	99
439	2465	2563	2662	2761	2860	2959	3058	3156	3255	3354	99
440	643453	3551	3650	3749	3847	3946	4044	4143	4242	4340	98
441	4439	4537	4636	4734	4832	4931	5029	5127	5226	5324	98
442	5422	5521	5619	5717	5815	5913	6011	6110	6208	6306	98
443	6404	6502	6600	6698	6796	6894	6992	7089	7187	7285	98
444	7383	7481	7579	7676	7774	7872	7969	8067	8165	8262	98
445	8360	8458	8555	8653	8750	8848	8945	9043	9140	9237	97
446	9335	9432	9530	9627	9724	9821	9919	**16	*113	*210	97
447	650308	0405	0502	0599	0696	0793	0890	0987	1084	1181	97
448	1278	1375	1472	1569	1666	1762	1859	1956	2053	2150	97
449	2246	2343	2440	2536	2633	2730	2826	2923	3019	3116	97
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452	5138	5235	5331	5427	5523	5619	5715	5810	5906	6002	96
453	6098	6194	6290	6386	6482	6577	6673	6769	6864	6960	96
454	7056	7152	7247	7343	7438	7534	7629	7725	7820	7916	96
455	8011	8107	8202	8298	8393	8488	8584	8679	8774	8870	95
456	8965	9060	9155	9250	9346	9441	9536	9631	9726	9821	95
457	9916	**11	*106	*201	*296	*391	*486	*581	*676	*771	95
458	660865	0960	1055	1150	1245	1339	1434	1529	1623	1718	95
459	1813	1907	2002	2096	2191	2286	2380	2475	2569	2663	95
460	662758	2852	2947	3041	3135	3230	3324	3418	3512	3607	94
461	3701	3795	3889	3983	4078	4172	4266	4360	4454	4548	94
462	4642	4736	4830	4924	5018	5112	5206	5299	5393	5487	94
463	5581	5675	5769	5862	5956	6050	6143	6237	6331	6424	94
464	6518	6612	6705	6799	6892	6986	7079	7173	7266	7360	94
465	7453	7546	7640	7733	7826	7920	8013	8106	8199	8293	93
466	8386	8479	8572	8665	8759	8852	8945	9038	9131	9224	93
467	9317	9410	9503	9596	9689	9782	9875	9967	**60	*153	93
468	670246	0339	0431	0524	0617	0710	0802	0895	0988	1080	93
469	1173	1265	1358	1451	1543	1636	1728	1821	1913	2005	93
470	672098	2190	2283	2375	2467	2560	2652	2744	2836	2929	92
471	3021	3113	3205	3297	3390	3482	3574	3666	3758	3850	92
472	3942	4034	4126	4218	4310	4402	4494	4586	4677	4769	92
473	4861	4953	5045	5137	5228	5320	5412	5503	5595	5687	92
474	5778	5870	5962	6053	6145	6236	6328	6419	6511	6602	92
475	6694	6785	6876	6968	7059	7151	7242	7333	7424	7516	91
476	7607	7698	7789	7881	7972	8063	8154	8245	8336	8427	91
477	8518	8609	8700	8791	8882	8973	9064	9155	9246	9337	91
478	9428	9519	9610	9700	9791	9882	9973	**63	*154	*245	91
479	680336	0426	0517	0607	0698	0789	0879	0970	1060	1151	91
480	681241	1332	1422	1513	1603	1693	1784	1874	1964	2055	90
481	2145	2235	2326	2416	2506	2596	2686	2777	2867	2957	90
482	3047	3137	3227	3317	3407	3497	3587	3677	3767	3857	90
483	3947	4037	4127	4217	4307	4396	4486	4576	4666	4756	90
484	4845	4935	5025	5114	5204	5294	5383	5473	5563	5652	90
485	5742	5831	5921	6010	6100	6189	6279	6368	6458	6547	89
486	6636	6726	6815	6904	6994	7083	7172	7261	7351	7440	89
487	7529	7618	7707	7796	7886	7975	8064	8153	8242	8331	89
488	8420	8509	8598	8687	8776	8865	8953	9042	9131	9220	89
489	9309	9398	9486	9575	9664	9753	9841	9930	**19	*107	89
490	690196	0285	0373	0462	0550	0639	0728	0816	0905	0993	89
491	1081	1170	1258	1347	1435	1524	1612	1700	1789	1877	88
492	1965	2053	2142	2230	2318	2406	2494	2583	2671	2759	88
493	2847	2935	3023	3111	3199	3287	3375	3463	3551	3639	88
494	3727	3815	3903	3991	4078	4166	4254	4342	4430	4517	88
495	4605	4693	4781	4868	4956	5044	5131	5219	5307	5394	88
496	5482	5569	5657	5744	5832	5919	6007	6094	6182	6269	87
497	6356	6444	6531	6618	6706	6793	6880	6968	7055	7142	87
498	7229	7317	7404	7491	7578	7665	7752	7839	7926	8014	87
499	8101	8188	8275	8362	8449	8535	8622	8709	8796	8883	87
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TABLE XXIX (CONTINUED)

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501	9838	9924	**11	**98	*184	*271	*358	*444	*531	*617	87
502	700704	0790	0877	0963	1050	1136	1222	1309	1395	1482	86
503	1568	1654	1741	1827	1913	1999	2086	2172	2258	2344	86
504	2431	2517	2603	2689	2775	2861	2947	3033	3119	3205	86
505	3291	3377	3463	3549	3635	3721	3807	3893	3979	4065	86
506	4151	4236	4322	4408	4494	4579	4665	4751	4837	4922	86
507	5008	5094	5179	5265	5350	5436	5522	5607	5693	5778	86
508	5864	5949	6035	6120	6206	6291	6376	6462	6547	6632	85
509	6718	6803	6888	6974	7059	7144	7229	7315	7400	7485	85
510	707570	7655	7740	7826	7911	7996	8081	8166	8251	8336	85
511	8421	8506	8591	8676	8761	8846	8931	9015	9100	9185	85
512	9270	9355	9440	9524	9609	9694	9779	9863	9948	**33	85
513	710117	0202	0287	0371	0456	0540	0625	0710	0794	0879	85
514	0963	1048	1132	1217	1301	1385	1470	1554	1639	1723	84
515	1807	1892	1976	2060	2144	2229	2313	2397	2481	2566	84
516	2650	2734	2818	2902	2986	3070	3154	3238	3323	3407	84
517	3491	3575	3659	3742	3826	3910	3994	4078	4162	4246	84
518	4330	4414	4497	4581	4665	4749	4833	4916	5000	5084	84
519	5167	5251	5335	5418	5502	5586	5669	5753	5836	5920	84
520	716003	6087	6170	6254	6337	6421	6504	6588	6671	6754	83
521	6838	6921	7004	7088	7171	7254	7338	7421	7504	7587	83
522	7671	7754	7837	7920	8003	8086	8169	8253	8336	8419	83
523	8502	8585	8668	8751	8834	8917	9000	9083	9165	9248	83
524	9331	9414	9497	9580	9663	9745	9828	9911	9994	**77	83
525	720159	0242	0325	0407	0490	0573	0655	0738	0821	0903	83
526	0986	1068	1151	1233	1316	1398	1481	1563	1646	1728	82
527	1811	1893	1975	2058	2140	2222	2305	2387	2469	2552	82
528	2634	2716	2798	2881	2963	3045	3127	3209	3291	3374	82
529	3456	3538	3620	3702	3784	3866	3948	4030	4112	4194	82
530	724276	4358	4440	4522	4604	4685	4767	4849	4931	5013	82
531	5095	5176	5258	5340	5422	5503	5585	5667	5748	5830	82
532	5912	5993	6075	6156	6238	6320	6401	6483	6564	6646	82
533	6727	6809	6890	6972	7053	7134	7216	7297	7379	7460	81
534	7541	7623	7704	7785	7866	7948	8029	8110	8191	8273	81
535	8354	8435	8516	8597	8678	8759	8841	8922	9003	9084	81
536	9165	9246	9327	9408	9489	9570	9651	9732	9813	9893	81
537	9974	**55	*136	*217	*298	*378	*459	*540	*621	*702	81
538	730782	0863	0944	1024	1105	1186	1266	1347	1428	1508	81
539	1589	1669	1750	1830	1911	1991	2072	2152	2233	2313	81
540	732394	2474	2555	2635	2715	2796	2876	2956	3037	3117	80
541	3197	3278	3358	3438	3518	3598	3679	3759	3839	3919	80
542	3999	4079	4160	4240	4320	4400	4480	4560	4640	4720	80
543	4800	4880	4960	5040	5120	5200	5279	5359	5439	5519	80
544	5599	5679	5759	5838	5918	5998	6078	6157	6237	6317	80
545	6397	6476	6556	6635	6715	6795	6874	6954	7034	7113	80
546	7193	7272	7352	7431	7511	7590	7670	7749	7829	7908	79
547	7987	8067	8146	8225	8305	8384	8463	8543	8622	8701	79
548	8781	8860	8939	9018	9097	9177	9256	9335	9414	9493	79
549	9572	9651	9731	9810	9889	9968	**47	*126	*205	*284	79
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551	1152	1230	1309	1388	1467	1546	1624	1703	1782	1860	79
552	1939	2018	2096	2175	2254	2332	2411	2489	2568	2647	79
553	2725	2804	2882	2961	3039	3118	3196	3275	3353	3431	78
554	3510	3588	3667	3745	3823	3902	3980	4058	4136	4215	78
555	4293	4371	4449	4528	4606	4684	4762	4840	4919	4997	78
556	5075	5153	5231	5309	5387	5465	5543	5621	5699	5777	78
557	5855	5933	6011	6089	6167	6245	6323	6401	6479	6556	78
558	6634	6712	6790	6868	6945	7023	7101	7179	7256	7334	78
559	7412	7489	7567	7645	7722	7800	7878	7955	8033	8110	78
560	748188	8266	8343	8421	8498	8576	8653	8731	8808	8885	77
561	8963	9040	9118	9195	9272	9350	9427	9504	9582	9659	77
562	9736	9814	9891	9968	**45	*123	*200	*277	*354	*431	77
563	750508	0586	0663	0740	0817	0894	0971	1048	1125	1202	77
564	1279	1356	1433	1510	1587	1664	1741	1818	1895	1972	77
565	2048	2125	2202	2279	2356	2433	2509	2586	2663	2740	77
566	2816	2893	2970	3047	3123	3200	3277	3353	3430	3506	77
567	3583	3660	3736	3813	3889	3966	4042	4119	4195	4272	77
568	4348	4425	4501	4578	4654	4730	4807	4883	4960	5036	76
569	5112	5189	5265	5341	5417	5494	5570	5646	5722	5799	76
570	755875	5951	6027	6103	6180	6256	6332	6408	6484	6560	76
571	6636	6712	6788	6864	6940	7016	7092	7168	7244	7320	76
572	7396	7472	7548	7624	7700	7775	7851	7927	8003	8079	76
573	8155	8230	8306	8382	8458	8533	8609	8685	8761	8836	76
574	8912	8988	9063	9139	9214	9290	9366	9441	9517	9592	76
575	9668	9743	9819	9894	9970	**45	*121	*196	*272	*347	75
576	760422	0498	0573	0649	0724	0799	0875	0950	1025	1101	75
577	1176	1251	1326	1402	1477	1552	1627	1702	1778	1853	75
578	1928	2003	2078	2153	2228	2303	2378	2453	2529	2604	75
579	2679	2754	2829	2904	2978	3053	3128	3203	3278	3353	75
580	763428	3503	3578	3653	3727	3802	3877	3952	4027	4101	75
581	4176	4251	4326	4400	4475	4550	4624	4699	4774	4848	75
582	4923	4998	5072	5147	5221	5296	5370	5445	5520	5594	75
583	5669	5743	5818	5892	5966	6041	6115	6190	6264	6338	74
584	6413	6487	6562	6636	6710	6785	6859	6933	7007	7082	74
585	7156	7230	7304	7379	7453	7527	7601	7675	7749	7823	74
586	7898	7972	8046	8120	8194	8268	8342	8416	8490	8564	74
587	8638	8712	8786	8860	8934	9008	9082	9156	9230	9303	74
588	9377	9451	9525	9599	9673	9746	9820	9894	9968	**42	74
589	770115	0189	0263	0336	0410	0484	0557	0631	0705	0778	74
590	770852	0926	0999	1073	1146	1220	1293	1367	1440	1514	74
591	1587	1661	1734	1808	1881	1955	2028	2102	2175	2248	73
592	2322	2395	2468	2542	2615	2688	2762	2835	2908	2981	73
593	3055	3128	3201	3274	3348	3421	3494	3567	3640	3713	73
594	3786	3860	3933	4006	4079	4152	4225	4298	4371	4444	73
595	4517	4590	4663	4736	4809	4882	4955	5028	5100	5173	73
596	5246	5319	5392	5465	5538	5610	5683	5756	5829	5902	73
597	5974	6047	6120	6193	6265	6338	6411	6483	6556	6629	73
598	6701	6774	6846	6919	6992	7064	7137	7209	7282	7354	73
599	7427	7499	7572	7644	7717	7789	7862	7934	8006	8079	72
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601	8874	8947	9019	9091	9163	9236	9308	9380	9452	9524	72
602	9596	9669	9741	9813	9885	9957	**29	*101	*173	*245	72
603	780317	0389	0461	0533	0605	0677	0749	0821	0893	0965	72
604	1037	1109	1181	1253	1324	1396	1468	1540	1612	1684	72
605	1755	1827	1899	1971	2042	2114	2186	2258	2329	2401	72
606	2473	2544	2616	2688	2759	2831	2902	2974	3046	3117	72
607	3189	3260	3332	3403	3475	3546	3618	3689	3761	3832	71
608	3904	3975	4046	4118	4189	4261	4332	4403	4475	4546	71
609	4617	4689	4760	4831	4902	4974	5045	5116	5187	5259	71
610	785330	5401	5472	5543	5615	5686	5757	5828	5899	5970	71
611	6041	6112	6183	6254	6325	6396	6467	6538	6609	6680	71
612	6751	6822	6893	6964	7035	7106	7177	7248	7319	7390	71
613	7460	7531	7602	7673	7744	7815	7885	7956	8027	8098	71
614	8168	8239	8310	8381	8451	8522	8593	8663	8734	8804	71
615	8875	8946	9016	9087	9157	9228	9299	9369	9440	9510	71
616	9581	9651	9722	9792	9863	9933	***4	**74	*144	*215	70
617	790285	0356	0426	0496	0567	0637	0707	0778	0848	0918	70
618	0988	1059	1129	1199	1269	1340	1410	1480	1550	1620	70
619	1691	1761	1831	1901	1971	2041	2111	2181	2252	2322	70
620	792392	2462	2532	2602	2672	2742	2812	2882	2952	3022	70
621	3092	3162	3231	3301	3371	3441	3511	3581	3651	3721	70
622	3790	3860	3930	4000	4070	4139	4209	4279	4349	4418	70
623	4488	4558	4627	4697	4767	4836	4906	4976	5045	5115	70
624	5185	5254	5324	5393	5463	5532	5602	5672	5741	5811	70
625	5880	5949	6019	6088	6158	6227	6297	6366	6436	6505	69
626	6574	6644	6713	6782	6852	6921	6990	7060	7129	7198	69
627	7268	7337	7406	7475	7545	7614	7683	7752	7821	7890	69
628	7960	8029	8098	8167	8236	8305	8374	8443	8513	8582	69
629	8651	8720	8789	8858	8927	8996	9065	9134	9203	9272	69
630	799341	9409	9478	9547	9616	9685	9754	9823	9892	9961	69
631	800029	0098	0167	0236	0305	0373	0442	0511	0580	0648	69
632	0717	0786	0854	0923	0992	1061	1129	1198	1266	1335	69
633	1404	1472	1541	1609	1678	1747	1815	1884	1952	2021	69
634	2089	2158	2226	2295	2363	2432	2500	2568	2637	2705	69
635	2774	2842	2910	2979	3047	3116	3184	3252	3321	3389	68
636	3457	3525	3594	3662	3730	3798	3867	3935	4003	4071	68
637	4139	4208	4276	4344	4412	4480	4548	4616	4685	4753	68
638	4821	4889	4957	5025	5093	5161	5229	5297	5365	5433	68
639	5501	5569	5637	5705	5773	5841	5908	5976	6044	6112	68
640	806180	6248	6316	6384	6451	6519	6587	6655	6723	6790	68
641	6858	6926	6994	7061	7129	7197	7264	7332	7400	7467	68
642	7535	7603	7670	7738	7806	7873	7941	8008	8076	8143	68
643	8211	8279	8346	8414	8481	8549	8616	8684	8751	8818	67
644	8886	8953	9021	9088	9156	9223	9290	9358	9425	9492	67
645	9560	9627	9694	9762	9829	9896	9964	**31	**98	*165	67
646	810233	0300	0367	0434	0501	0569	0636	0703	0770	0837	67
647	0904	0971	1039	1106	1173	1240	1307	1374	1441	1508	67
648	1575	1642	1709	1776	1843	1910	1977	2044	2111	2178	67
649	2245	2312	2379	2445	2512	2579	2646	2713	2780	2847	67
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651	3581	3648	3714	3781	3848	3914	3981	4048	4114	4181	67
652	4248	4314	4381	4447	4514	4581	4647	4714	4780	4847	67
653	4913	4980	5046	5113	5179	5246	5312	5378	5445	5511	66
654	5578	5644	5711	5777	5843	5910	5976	6042	6109	6175	66
655	6241	6308	6374	6440	6506	6573	6639	6705	6771	6838	66
656	6904	6970	7036	7102	7169	7235	7301	7367	7433	7499	66
657	7565	7631	7698	7764	7830	7896	7962	8028	8094	8160	66
658	8226	8292	8358	8424	8490	8556	8622	8688	8754	8820	66
659	8885	8951	9017	9083	9149	9215	9281	9346	9412	9478	66
660	819544	9610	9676	9741	9807	9873	9939	***4	**70	*136	66
661	820201	0267	0333	0399	0464	0530	0595	0661	0727	0792	66
662	0858	0924	0989	1055	1120	1186	1251	1317	1382	1448	66
663	1514	1579	1645	1710	1775	1841	1906	1972	2037	2103	65
664	2168	2233	2299	2364	2430	2495	2560	2626	2691	2756	65
665	2822	2887	2952	3018	3083	3148	3213	3279	3344	3409	65
666	3474	3539	3605	3670	3735	3800	3865	3930	3996	4061	65
667	4126	4191	4256	4321	4386	4451	4516	4581	4646	4711	65
668	4776	4841	4906	4971	5036	5101	5166	5231	5296	5361	65
669	5426	5491	5556	5621	5686	5751	5815	5880	5945	6010	65
670	826075	6140	6204	6269	6334	6399	6464	6528	6593	6658	65
671	6723	6787	6852	6917	6981	7046	7111	7175	7240	7305	65
672	7369	7434	7499	7563	7628	7692	7757	7821	7886	7951	65
673	8015	8080	8144	8209	8273	8338	8402	8467	8531	8595	64
674	8660	8724	8789	8853	8918	8982	9046	9111	9175	9239	64
675	9304	9368	9432	9497	9561	9625	9690	9754	9818	9882	64
676	9947	**11	**75	*139	*204	*268	*332	*396	*460	*525	64
677	830589	0653	0717	0781	0845	0909	0973	1037	1102	1166	64
678	1230	1294	1358	1422	1486	1550	1614	1678	1742	1806	64
679	1870	1934	1998	2062	2126	2189	2253	2317	2381	2445	64
680	832509	2573	2637	2700	2764	2828	2892	2956	3020	3083	64
681	3147	3211	3275	3338	3402	3466	3530	3593	3657	3721	64
682	3784	3848	3912	3975	4039	4103	4166	4230	4294	4357	64
683	4421	4484	4548	4611	4675	4739	4802	4866	4929	4993	64
684	5056	5120	5183	5247	5310	5373	5437	5500	5564	5627	63
685	5691	5754	5817	5881	5944	6007	6071	6134	6197	6261	63
686	6324	6387	6451	6514	6577	6641	6704	6767	6830	6894	63
687	6957	7020	7083	7146	7210	7273	7336	7399	7462	7525	63
688	7588	7652	7715	7778	7841	7904	7967	8030	8093	8156	63
689	8219	8282	8345	8408	8471	8534	8597	8660	8723	8786	63
690	838849	8912	8975	9038	9101	9164	9227	9289	9352	9415	63
691	9478	9541	9604	9667	9729	9792	9855	9918	9981	**43	63
692	840106	0169	0232	0294	0357	0420	0482	0545	0608	0671	63
693	0733	0796	0859	0921	0984	1046	1109	1172	1234	1297	63
694	1359	1422	1485	1547	1610	1672	1735	1797	1860	1922	63
695	1985	2047	2110	2172	2235	2297	2360	2422	2484	2547	62
696	2609	2672	2734	2796	2859	2921	2983	3046	3108	3170	62
697	3233	3295	3357	3420	3482	3544	3606	3669	3731	3793	62
698	3855	3918	3980	4042	4104	4166	4229	4291	4353	4415	62
699	4477	4539	4601	4664	4726	4788	4850	4912	4974	5036	62
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TABLE XXIX (CONTINUED)

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701	5718	5780	5842	5904	5966	6028	6090	6151	6213	6275	62
702	6337	6399	6461	6523	6585	6646	6708	6770	6832	6894	62
703	6955	7017	7079	7141	7202	7264	7326	7388	7449	7511	62
704	7573	7634	7696	7758	7819	7881	7943	8004	8066	8128	62
705	8189	8251	8312	8374	8435	8497	8559	8620	8682	8743	62
706	8805	8866	8928	8989	9051	9112	9174	9235	9297	9358	61
707	9419	9481	9542	9604	9665	9726	9788	9849	9911	9972	61
708	850033	0095	0156	0217	0279	0340	0401	0462	0524	0585	61
709	0646	0707	0769	0830	0891	0952	1014	1075	1136	1197	61
710	851258	1320	1381	1442	1503	1564	1625	1686	1747	1809	61
711	1870	1931	1992	2053	2114	2175	2236	2297	2358	2419	61
712	2480	2541	2602	2663	2724	2785	2846	2907	2968	3029	61
713	3090	3150	3211	3272	3333	3394	3455	3516	3577	3637	61
714	3698	3759	3820	3881	3941	4002	4063	4124	4185	4245	61
715	4306	4367	4428	4488	4549	4610	4670	4731	4792	4852	61
716	4913	4974	5034	5095	5156	5216	5277	5337	5398	5459	61
717	5519	5580	5640	5701	5761	5822	5882	5943	6003	6064	61
718	6124	6185	6245	6306	6366	6427	6487	6548	6608	6668	60
719	6729	6789	6850	6910	6970	7031	7091	7152	7212	7272	60
720	857332	7393	7453	7513	7574	7634	7694	7755	7815	7875	60
721	7935	7995	8056	8116	8176	8236	8297	8357	8417	8477	60
722	8537	8597	8657	8718	8778	8838	8898	8958	9018	9078	60
723	9138	9198	9258	9318	9379	9439	9499	9559	9619	9679	60
724	9739	9799	9859	9918	9978	**38	**98	*158	*218	*278	60
725	860338	0398	0458	0518	0578	0637	0697	0757	0817	0877	60
726	0937	0996	1056	1116	1176	1236	1295	1355	1415	1475	60
727	1534	1594	1654	1714	1773	1833	1893	1952	2012	2072	60
728	2131	2191	2251	2310	2370	2430	2489	2549	2608	2668	60
729	2728	2787	2847	2906	2966	3025	3085	3144	3204	3263	60
730	863323	3382	3442	3501	3561	3620	3680	3739	3799	3858	59
731	3917	3977	4036	4096	4155	4214	4274	4333	4392	4452	59
732	4511	4570	4630	4689	4748	4808	4867	4926	4985	5045	59
733	5104	5163	5222	5282	5341	5400	5459	5519	5578	5637	59
734	5696	5755	5814	5874	5933	5992	6051	6110	6169	6228	59
735	6287	6346	6405	6465	6524	6583	6642	6701	6760	6819	59
736	6878	6937	6996	7055	7114	7173	7232	7291	7350	7409	59
737	7467	7526	7585	7644	7703	7762	7821	7880	7939	7998	59
738	8056	8115	8174	8233	8292	8350	8409	8468	8527	8586	59
739	8644	8703	8762	8821	8879	8938	8997	9056	9114	9173	59
740	869232	9290	9349	9408	9466	9525	9584	9642	9701	9760	59
741	9818	9877	9935	9994	**53	*111	*170	*228	*287	*345	59
742	870404	0462	0521	0579	0638	0696	0755	0813	0872	0930	58
743	0989	1047	1106	1164	1223	1281	1339	1398	1456	1515	58
744	1573	1631	1690	1748	1806	1865	1923	1981	2040	2098	58
745	2156	2215	2273	2331	2389	2448	2506	2564	2622	2681	58
746	2739	2797	2855	2913	2972	3030	3088	3146	3204	3262	58
747	3321	3379	3437	3495	3553	3611	3669	3727	3785	3844	58
748	3902	3960	4018	4076	4134	4192	4250	4308	4366	4424	58
749	4482	4540	4598	4656	4714	4772	4830	4888	4945	5003	58
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751	5640	5698	5756	5813	5871	5929	5987	6045	6102	6160	58
752	6218	6276	6333	6391	6449	6507	6564	6622	6680	6737	58
753	6795	6853	6910	6968	7026	7083	7141	7199	7256	7314	58
754	7371	7429	7487	7544	7602	7659	7717	7774	7832	7889	58
755	7947	8004	8062	8119	8177	8234	8292	8349	8407	8464	57
756	8522	8579	8637	8694	8752	8809	8866	8924	8981	9039	57
757	9096	9153	9211	9268	9325	9383	9440	9497	9555	9612	57
758	9669	9726	9784	9841	9898	9956	**13	**70	*127	*185	57
759	880242	0299	0356	0413	0471	0528	0585	0642	0699	0756	57
760	880814	0871	0928	0985	1042	1099	1156	1213	1271	1328	57
761	1385	1442	1499	1556	1613	1670	1727	1784	1841	1898	57
762	1955	2012	2069	2126	2183	2240	2297	2354	2411	2468	57
763	2525	2581	2638	2695	2752	2809	2866	2923	2980	3037	57
764	3093	3150	3207	3264	3321	3377	3434	3491	3548	3605	57
765	3661	3718	3775	3832	3888	3945	4002	4059	4115	4172	57
766	4229	4285	4342	4399	4455	4512	4569	4625	4682	4739	57
767	4795	4852	4909	4965	5022	5078	5135	5192	5248	5305	57
768	5361	5418	5474	5531	5587	5644	5700	5757	5813	5870	57
769	5926	5983	6039	6096	6152	6209	6265	6321	6378	6434	56
770	886491	6547	6604	6660	6716	6773	6829	6885	6942	6998	56
771	7054	7111	7167	7223	7280	7336	7392	7449	7505	7561	56
772	7617	7674	7730	7786	7842	7898	7955	8011	8067	8123	56
773	8179	8236	8292	8348	8404	8460	8516	8573	8629	8685	56
774	8741	8797	8853	8909	8965	9021	9077	9134	9190	9246	56
775	9302	9358	9414	9470	9526	9582	9638	9694	9750	9806	56
776	9862	9918	9974	**30	**86	*141	*197	*253	*309	*365	56
777	890421	0477	0533	0589	0645	0700	0756	0812	0868	0924	56
778	0980	1035	1091	1147	1203	1259	1314	1370	1426	1482	56
779	1537	1593	1649	1705	1760	1816	1872	1928	1983	2039	56
780	892095	2150	2206	2262	2317	2373	2429	2484	2540	2595	56
781	2651	2707	2762	2818	2873	2929	2985	3040	3096	3151	56
782	3207	3262	3318	3373	3429	3484	3540	3595	3651	3706	56
783	3762	3817	3873	3928	3984	4039	4094	4150	4205	4261	55
784	4316	4371	4427	4482	4538	4593	4648	4704	4759	4814	55
785	4870	4925	4980	5036	5091	5146	5201	5257	5312	5367	55
786	5423	5478	5533	5588	5644	5699	5754	5809	5864	5920	55
787	5975	6030	6085	6140	6195	6251	6306	6361	6416	6471	55
788	6526	6581	6636	6692	6747	6802	6857	6912	6967	7022	55
789	7077	7132	7187	7242	7297	7352	7407	7462	7517	7572	55
790	897627	7682	7737	7792	7847	7902	7957	8012	8067	8122	55
791	8176	8231	8286	8341	8396	8451	8506	8561	8615	8670	55
792	8725	8780	8835	8890	8944	8999	9054	9109	9164	9218	55
793	9273	9328	9383	9437	9492	9547	9602	9656	9711	9766	55
794	9821	9875	9930	9985	**39	**94	*149	*203	*258	*312	55
795	900367	0422	0476	0531	0586	0640	0695	0749	0804	0859	55
796	0913	0968	1022	1077	1131	1186	1240	1295	1349	1404	55
797	1458	1513	1567	1622	1676	1731	1785	1840	1894	1948	54
798	2003	2057	2112	2166	2221	2275	2329	2384	2438	2492	54
799	2547	2601	2655	2710	2764	2818	2873	2927	2981	3036	54
N.	0	1	2	3	4	5	6	7	8	9	D.

TABLE XXIX (CONTINUED)

N.	0	1	2	3	4	5	6	7	8	9	D.
800	903090	3144	3199	3253	3307	3361	3416	3470	3524	3578	54
801	3633	3687	3741	3795	3849	3904	3958	4012	4066	4120	54
802	4174	4229	4283	4337	4391	4445	4499	4553	4607	4661	54
803	4716	4770	4824	4878	4932	4986	5040	5094	5148	5202	54
804	5256	5310	5364	5418	5472	5526	5580	5634	5688	5742	54
805	5796	5850	5904	5958	6012	6066	6119	6173	6227	6281	54
806	6335	6389	6443	6497	6551	6604	6658	6712	6766	6820	54
807	6874	6927	6981	7035	7089	7143	7196	7250	7304	7358	54
808	7411	7465	7519	7573	7626	7680	7734	7787	7841	7895	54
809	7949	8002	8056	8110	8163	8217	8270	8324	8378	8431	54
810	908485	8539	8592	8646	8699	8753	8807	8860	8914	8967	54
811	9021	9074	9128	9181	9235	9289	9342	9396	9449	9503	54
812	9556	9610	9663	9716	9770	9823	9877	9930	9984	**37	53
813	910091	0144	0197	0251	0304	0358	0411	0464	0518	0571	53
814	0624	0678	0731	0784	0838	0891	0944	0998	1051	1104	53
815	1158	1211	1264	1317	1371	1424	1477	1530	1584	1637	53
816	1690	1743	1797	1850	1903	1956	2009	2063	2116	2169	53
817	2222	2275	2328	2381	2435	2488	2541	2594	2647	2700	53
818	2753	2806	2859	2913	2966	3019	3072	3125	3178	3231	53
819	3284	3337	3390	3443	3496	3549	3602	3655	3708	3761	53
820	913814	3867	3920	3973	4026	4079	4132	4184	4237	4290	53
821	4343	4396	4449	4502	4555	4608	4660	4713	4766	4819	53
822	4872	4925	4977	5030	5083	5136	5189	5241	5294	5347	53
823	5400	5453	5505	5558	5611	5664	5716	5769	5822	5875	53
824	5927	5980	6033	6085	6138	6191	6243	6296	6349	6401	53
825	6454	6507	6559	6612	6664	6717	6770	6822	6875	6927	53
826	6980	7033	7085	7138	7190	7243	7295	7348	7400	7453	53
827	7506	7558	7611	7663	7716	7768	7820	7873	7925	7978	52
828	8030	8083	8135	8188	8240	8293	8345	8397	8450	8502	52
829	8555	8607	8659	8712	8764	8816	8869	8921	8973	9026	52
830	919078	9130	9183	9235	9287	9340	9392	9444	9496	9549	52
831	9601	9653	9706	9758	9810	9862	9914	9967	**19	**71	52
832	920123	0176	0228	0280	0332	0384	0436	0489	0541	0593	52
833	0645	0697	0749	0801	0853	0906	0958	1010	1062	1114	52
834	1166	1218	1270	1322	1374	1426	1478	1530	1582	1634	52
835	1686	1738	1790	1842	1894	1946	1998	2050	2102	2154	52
836	2206	2258	2310	2362	2414	2466	2518	2570	2622	2674	52
837	2725	2777	2829	2881	2933	2985	3037	3089	3140	3192	52
838	3244	3296	3348	3399	3451	3503	3555	3607	3658	3710	52
839	3762	3814	3865	3917	3969	4021	4072	4124	4176	4228	52
840	924279	4331	4383	4434	4486	4538	4589	4641	4693	4744	52
841	4796	4848	4899	4951	5003	5054	5106	5157	5209	5261	52
842	5312	5364	5415	5467	5518	5570	5621	5673	5725	5776	52
843	5828	5879	5931	5982	6034	6085	6137	6188	6240	6291	51
844	6342	6394	6445	6497	6548	6600	6651	6702	6754	6805	51
845	6857	6908	6959	7011	7062	7114	7165	7216	7268	7319	51
846	7370	7422	7473	7524	7576	7627	7678	7730	7781	7832	51
847	7883	7935	7986	8037	8088	8140	8191	8242	8293	8345	51
848	8396	8447	8498	8549	8601	8652	8703	8754	8805	8857	51
849	8908	8959	9010	9061	9112	9163	9215	9266	9317	9368	51
N.	0	1	2	3	4	5	6	7	8	9	D.

N.	0	1	2	3	4	5	6	7	8	9	D.
850	929419	9470	9521	9572	9623	9674	9725	9776	9827	9879	51
851	9930	9981	**32	**83	*134	*185	*236	*287	*338	*389	51
852	930440	0491	0542	0592	0643	0694	0745	0796	0847	0898	51
853	0919	1000	1051	1102	1153	1204	1254	1305	1356	1407	51
854	1458	1509	1560	1610	1661	1712	1763	1814	1865	1915	51
855	1966	2017	2068	2118	2169	2220	2271	2322	2372	2423	51
856	2474	2524	2575	2626	2677	2727	2778	2829	2879	2930	51
857	2981	3031	3082	3133	3183	3234	3285	3335	3386	3437	51
858	3487	3538	3589	3639	3690	3740	3791	3841	3892	3943	51
859	3993	4044	4094	4145	4195	4246	4296	4347	4397	4448	51
860	934498	4549	4599	4650	4700	4751	4801	4852	4902	4953	50
861	5003	5054	5104	5154	5205	5255	5306	5356	5406	5457	50
862	5507	5558	5608	5658	5709	5759	5809	5860	5910	5960	50
863	6011	6061	6111	6162	6212	6262	6313	6363	6413	6463	50
864	6514	6564	6614	6665	6715	6765	6815	6865	6916	6966	50
865	7016	7066	7117	7167	7217	7267	7317	7367	7418	7468	50
866	7518	7568	7618	7668	7718	7769	7819	7869	7919	7969	50
867	8019	8069	8119	8169	8219	8269	8320	8370	8420	8470	50
868	8520	8570	8620	8670	8720	8770	8820	8870	8920	8970	50
869	9020	9070	9120	9170	9220	9270	9320	9369	9419	9469	50
870	939519	9569	9619	9669	9719	9769	9819	9869	9918	9968	50
871	940018	0068	0118	0168	0218	0267	0317	0367	0417	0467	50
872	0516	0566	0616	0666	0716	0765	0815	0865	0915	0964	50
873	1014	1064	1114	1163	1213	1263	1313	1362	1412	1462	50
874	1511	1561	1611	1660	1710	1760	1809	1859	1909	1958	50
875	2008	2058	2107	2157	2207	2256	2306	2355	2405	2455	50
876	2504	2554	2603	2653	2702	2752	2801	2851	2901	2950	50
877	3000	3049	3099	3148	3198	3247	3297	3346	3396	3445	49
878	3495	3544	3593	3643	3692	3742	3791	3841	3890	3939	49
879	3989	4038	4088	4137	4186	4236	4285	4335	4384	4433	49
880	944483	4532	4581	4631	4680	4729	4779	4828	4877	4927	49
881	4976	5025	5074	5124	5173	5222	5272	5321	5370	5419	49
882	5469	5518	5567	5616	5665	5715	5764	5813	5862	5912	49
883	5961	6010	6059	6108	6157	6207	6256	6305	6354	6403	49
884	6452	6501	6551	6600	6649	6698	6747	6796	6845	6894	49
885	6943	6992	7041	7090	7140	7189	7238	7287	7336	7385	49
886	7434	7483	7532	7581	7630	7679	7728	7777	7826	7875	49
887	7924	7973	8022	8070	8119	8168	8217	8266	8315	8364	49
888	8413	8462	8511	8560	8609	8657	8706	8755	8804	8853	49
889	8902	8951	8999	9048	9097	9146	9195	9244	9292	9341	49
890	949390	9439	9488	9536	9585	9634	9683	9731	9780	9829	49
891	9878	9926	9975	**24	**73	*121	*170	*219	*267	*316	49
892	950365	0414	0462	0511	0560	0608	0657	0706	0754	0803	49
893	0851	0900	0949	0997	1046	1095	1143	1192	1240	1289	49
894	1338	1386	1435	1483	1532	1580	1629	1677	1726	1775	49
895	1823	1872	1920	1969	2017	2066	2114	2163	2211	2260	48
896	2308	2356	2405	2453	2502	2550	2599	2647	2696	2744	48
897	2792	2841	2889	2938	2986	3034	3083	3131	3180	3228	48
898	3276	3325	3373	3421	3470	3518	3566	3615	3663	3711	48
899	3760	3808	3856	3905	3953	4001	4049	4098	4146	4194	48
N.	0	1	2	3	4	5	6	7	8	9	D.

TABLE XXIX (CONTINUED)

N.	0	1	2	3	4	5	6	7	8	9	D.
900	954243	4291	4339	4387	4435	4484	4532	4580	4628	4677	48
901	4725	4773	4821	4869	4918	4966	5014	5062	5110	5158	48
902	5207	5255	5303	5351	5399	5447	5495	5543	5592	5640	48
903	5688	5736	5784	5832	5880	5928	5976	6024	6072	6120	48
904	6168	6216	6265	6313	6361	6409	6457	6505	6553	6601	48
905	6649	6697	6745	6793	6840	6888	6936	6984	7032	7080	48
906	7128	7176	7224	7272	7320	7368	7416	7464	7512	7559	48
907	7607	7655	7703	7751	7799	7847	7894	7942	7990	8038	48
908	8086	8134	8181	8229	8277	8325	8373	8421	8468	8516	48
909	8564	8612	8659	8707	8755	8803	8850	8898	8946	8994	48
910	959041	9089	9137	9185	9232	9280	9328	9375	9423	9471	48
911	9518	9566	9614	9661	9709	9757	9804	9852	9900	9947	48
912	9995	**42	**90	*138	*185	*233	*280	*328	*376	*423	48
913	960471	0518	0566	0613	0661	0709	0756	0804	0851	0899	48
914	0946	0994	1041	1089	1136	1184	1231	1279	1326	1374	47
915	1421	1469	1516	1563	1611	1658	1706	1753	1801	1848	47
916	1895	1943	1990	2038	2085	2132	2180	2227	2275	2322	47
917	2369	2417	2464	2511	2559	2606	2653	2701	2748	2795	47
918	2843	2890	2937	2985	3032	3079	3126	3174	3221	3268	47
919	3316	3363	3410	3457	3504	3552	3599	3646	3693	3741	47
920	963788	3835	3882	3929	3977	4024	4071	4118	4165	4212	47
921	4260	4307	4354	4401	4448	4495	4542	4590	4637	4684	47
922	4731	4778	4825	4872	4919	4966	5013	5061	5108	5155	47
923	5202	5249	5296	5343	5390	5437	5484	5531	5578	5625	47
924	5672	5719	5766	5813	5860	5907	5954	6001	6048	6095	47
925	6142	6189	6236	6283	6329	6376	6423	6470	6517	6564	47
926	6611	6658	6705	6752	6799	6845	6892	6939	6986	7033	47
927	7080	7127	7173	7220	7267	7314	7361	7408	7454	7501	47
928	7548	7595	7642	7688	7735	7782	7829	7875	7922	7969	47
929	8016	8062	8109	8156	8203	8249	8296	8343	8390	8436	47
930	968483	8530	8576	8623	8670	8716	8763	8810	8856	8903	47
931	8950	8996	9043	9090	9136	9183	9229	9276	9323	9369	47
932	9416	9463	9509	9556	9602	9649	9695	9742	9789	9835	47
933	9882	9928	9975	**21	**68	*114	*161	*207	*254	*300	47
934	970347	0393	0440	0486	0533	0579	0626	0672	0719	0765	46
935	0812	0858	0904	0951	0997	1044	1090	1137	1183	1229	46
936	1276	1322	1369	1415	1461	1508	1554	1601	1647	1693	46
937	1740	1786	1832	1879	1925	1971	2018	2064	2110	2157	46
938	2203	2249	2295	2342	2388	2434	2481	2527	2573	2619	46
939	2666	2712	2758	2804	2851	2897	2943	2989	3035	3082	46
940	973128	3174	3220	3266	3313	3359	3405	3451	3497	3543	46
941	3590	3636	3682	3728	3774	3820	3866	3913	3959	4005	46
942	4051	4097	4143	4189	4235	4281	4327	4374	4420	4466	46
943	4512	4558	4604	4650	4696	4742	4788	4834	4880	4926	46
944	4972	5018	5064	5110	5156	5202	5248	5294	5340	5386	46
945	5432	5478	5524	5570	5616	5662	5707	5753	5799	5845	46
946	5891	5937	5983	6029	6075	6121	6167	6212	6258	6304	46
947	6350	6396	6442	6488	6533	6579	6625	6671	6717	6763	46
948	6808	6854	6900	6946	6992	7037	7083	7129	7175	7220	46
949	7266	7312	7358	7403	7449	7495	7541	7586	7632	7678	46
N.	0	1	2	3	4	5	6	7	8	9	D.

N.	0	1	2	3	4	5	6	7	8	9	D.
950	977724	7769	7815	7861	7906	7952	7998	8043	8089	8135	46
951	8181	8226	8272	8317	8363	8409	8454	8500	8546	8591	46
952	8637	8683	8728	8774	8819	8865	8911	8956	9002	9047	46
953	9093	9138	9184	9230	9275	9321	9366	9412	9457	9503	46
954	9548	9594	9639	9685	9730	9776	9821	9867	9912	9958	46
955	980003	0049	0094	0140	0185	0231	0276	0322	0367	0412	45
956	0458	0503	0549	0594	0640	0685	0730	0776	0821	0867	45
957	0912	0957	1003	1048	1093	1139	1184	1229	1275	1320	45
958	1365	1411	1456	1501	1547	1592	1637	1683	1728	1773	45
959	1819	1864	1909	1954	2000	2045	2090	2135	2181	2226	45
960	982271	2316	2362	2407	2452	2497	2543	2588	2633	2678	45
961	2723	2769	2814	2859	2904	2949	2994	3040	3085	3130	45
962	3175	3220	3265	3310	3356	3401	3446	3491	3536	3581	45
963	3626	3671	3716	3762	3807	3852	3897	3942	3987	4032	45
964	4077	4122	4167	4212	4257	4302	4347	4392	4437	4482	45
965	4527	4572	4617	4662	4707	4752	4797	4842	4887	4932	45
966	4977	5022	5067	5112	5157	5202	5247	5292	5337	5382	45
967	5426	5471	5516	5561	5606	5651	5696	5741	5786	5830	45
968	5875	5920	5965	6010	6055	6100	6144	6189	6234	6279	45
969	6324	6369	6413	6458	6503	6548	6593	6637	6682	6727	45
970	986772	6817	6861	6906	6951	6996	7040	7085	7130	7175	45
971	7219	7264	7309	7353	7398	7443	7488	7532	7577	7622	45
972	7666	7711	7756	7800	7845	7890	7934	7979	8024	8068	45
973	8113	8157	8202	8247	8291	8336	8381	8425	8470	8514	45
974	8559	8604	8648	8693	8737	8782	8826	8871	8916	8960	45
975	9005	9049	9094	9138	9183	9227	9272	9316	9361	9405	45
976	9450	9494	9539	9583	9628	9672	9717	9761	9806	9850	44
977	9895	9939	9983	**28	**72	*117	*161	*206	*250	*294	44
978	990339	0383	0428	0472	0516	0561	0605	0650	0694	0738	44
979	0783	0827	0871	0916	0960	1004	1049	1093	1137	1182	44
980	991226	1270	1315	1359	1403	1448	1492	1536	1580	1625	44
981	1669	1713	1758	1802	1846	1890	1935	1979	2023	2067	44
982	2111	2156	2200	2244	2288	2333	2377	2421	2465	2509	44
983	2554	2598	2642	2686	2730	2774	2819	2863	2907	2951	44
984	2995	3039	3083	3127	3172	3216	3260	3304	3348	3392	44
985	3436	3480	3524	3568	3613	3657	3701	3745	3789	3833	44
986	3877	3921	3965	4009	4053	4097	4141	4185	4229	4273	44
987	4317	4361	4405	4449	4493	4537	4581	4625	4669	4713	44
988	4757	4801	4845	4889	4933	4977	5021	5065	5108	5152	44
989	5196	5240	5284	5328	5372	5416	5460	5504	5547	5591	44
990	995635	5679	5723	5767	5811	5854	5898	5942	5986	6030	44
991	6074	6117	6161	6205	6249	6293	6337	6380	6424	6468	44
992	6512	6555	6599	6643	6687	6731	6774	6818	6862	6906	44
993	6949	6993	7037	7080	7124	7168	7212	7255	7299	7343	44
994	7386	7430	7474	7517	7561	7605	7648	7692	7736	7779	44
995	7823	7867	7910	7954	7998	8041	8085	8129	8172	8216	44
996	8259	8303	8347	8390	8434	8477	8521	8564	8608	8652	44
997	8695	8739	8782	8826	8869	8913	8956	9000	9043	9087	44
998	9131	9174	9218	9261	9305	9348	9392	9435	9479	9522	44
999	9565	9609	9652	9696	9739	9783	9826	9870	9913	9957	43
N.	0	1	2	3	4	5	6	7	8	9	D.

EXPLANATIONS OF THE PRECEDING TABLES

TABLE I

THE ATOMIC WEIGHTS OF THE ELEMENTS

This table contains the most recent values of the atomic weights of the elements, based upon the following standards: oxygen = 16.000, silver = 107.87.

There seems to be little doubt now that the atomic weight of silver is at least as low as 107.87, and for that reason all of those values which have been determined by means of silver are recalculated to this basis.

The writer has ventured to give the atomic weights of a few elements to three places of decimals, but it must be remembered that the third place is obtained by averaging a large number of analyses, and, with two exceptions, it is not definitely known. However, in view of the fact that such excellent work has been done in revising the weights in these special cases, it seems probable that the values as recorded approach more closely the true values than would be the case if the third place were dropped.

TABLES II-IV

These tables contain the molecular weights* of common compounds, multiples of the atomic weights of common elements, and of some common compounds.

They are useful in calculating the amounts of substances which are chemically equivalent to given amounts of other substances. A few examples will illustrate some of their uses:

(1) Calculate the weight of hydrochloric acid which is exactly equivalent to 1.5 grams of sodium carbonate.

$$\begin{array}{l} \text{Na}_2\text{CO}_3 + 2\text{HCl} = 2\text{NaCl} + \text{CO}_2 + \text{H}_2\text{O}. \\ \text{mol. wt. Na}_2\text{CO}_3 : \text{mol. wt. HCl} \times 2 :: 1.5 \text{ grams Na}_2\text{CO}_3 : x \text{ grams HCl.} \\ \frac{\text{mol. wt. HCl} \times 2 \times 1.5}{\text{mol. wt. Na}_2\text{CO}_3} = \text{wt. HCl required.} \end{array}$$

* The accuracy of a molecular weight is largely determined by the least accurate of the atomic weights which make it up. For example, it is useless to give the molecular weight of sulphuric acid to more than two places of decimals, although the atomic weight of hydrogen is known within a few units in the fourth place of decimals, and oxygen is the standard.

log second multiple of the mol. wt. HCl (Table IV)	= 1.862870
log 1.5 (table of logarithms)	= <u>0.176091</u>
sum	= 2.038961
log mol. wt. Na_2CO_3 (Table III)	= <u>2.025265</u>
difference	= 0.013696

The number of which 0.013696 is the logarithm is 1.03203, which is the weight of HCl required.

(2) What weight of silver must be dissolved in nitric acid and added to a solution containing two grams, of barium chloride in order to precipitate exactly all of the chlorine?

$$\text{BaCl}_2 + 2 \text{AgNO}_3 = 2 \text{AgCl} + \text{Ba}(\text{NO}_3)_2.$$

mol. wt. BaCl_2 : at. wt. Ag $\times 2$: : 2 grams BaCl_2 : x grams Ag.

$$\frac{\text{at. wt. Ag} \times 2 \times 2}{\text{mol. wt. BaCl}_2} = \text{wt. Ag required.}$$

log second multiple at. wt. Ag (Table II)	= 2.333930
log 2 (table of logarithms)	= <u>0.301030</u>
sum	= 2.634960
log mol. wt. BaCl_2 (Table III)	= <u>2.318627</u>
difference	= 0.316333

The number of which 0.316333 is the logarithm is 2.07172, which is the weight of silver required.

(3) The atomic weights of many of the elements are most readily and accurately determined by preparing certain of their halides in a state of great purity, and then in a weighed sample of such material determining the exact weight of pure silver which is equivalent to the halogen. From such data the atomic weight of the element in question may be easily calculated by means of the tables. For example, let us take a special case which will illustrate the method: A weighed sample of phosphorus tribromide was treated in such a manner that the exact weight of silver equivalent to the bromine it contained was determined, and the weight of silver bromide formed was also determined. The atomic weights of bromine and silver being accurately known, we have only to calculate from the data the molecular weight of phosphorus tribromide and subtract from it three times the atomic weight of bromine in order to obtain the atomic weight of phosphorus. Therefore we make the following proportion:

$$\text{wt. Ag} : \text{wt. PBr}_3 :: \text{at. wt. Ag} \times 3 : \text{mol. wt. PBr}_3.$$

In this calculation we need, in addition to the logarithms of the first two terms of the proportion, the logarithm of the third multiple of the atomic weight of silver, and the third multiple of the atomic weight of bromine, both of which are given in Table II.

To calculate the same value from the weight of silver bromide formed, which incidentally serves as a check on the first value and also gives one a clear idea of the purity of the precipitate, we make the following proportion :

$$\text{wt. AgBr} : \text{wt. PBr}_3 :: \text{mol. wt. AgBr} \times 3 : \text{mol. wt. PBr}_3.$$

The third multiple of the molecular weight of silver bromide is given in Table IV.

The tables are also useful in making standard solutions, especially those of certain normalities, as in many cases it is only necessary to shift the decimal point in the proper value in order to ascertain the weight of substance which a liter of the standard solution should contain.

A normal solution contains in a liter of *solution* a gram molecular weight of substance reduced to a univalent basis.

Two examples will serve to indicate the method of using the tables for this purpose.

NOTE. It is scarcely necessary to call attention to the rule of decimal fractions, i.e. that to divide by 10 is equivalent to moving the decimal point one place to the left in the dividend ; that to divide by 100 is equivalent to moving the point two places to the left, etc.

SOLUTIONS OF HYDROCHLORIC ACID OF CERTAIN NORMALITIES

$$N = \text{mol. wt. (Table III).}$$

$$\frac{N}{2} = \frac{\text{mol. wt.}}{2} \rightleftharpoons \frac{\text{mol. wt.} \times 5}{10} \text{ (Table IV).}$$

$$\frac{N}{5} = \frac{\text{mol. wt.}}{5} \rightleftharpoons \frac{\text{mol. wt.} \times 2}{10} \text{ (Table IV).}$$

$$\frac{N}{10} = \frac{\text{mol. wt.}}{10} \text{ (Table III).}$$

$$\frac{N}{25} = \frac{\text{mol. wt.}}{25} \rightleftharpoons \frac{\text{mol. wt.} \times 4}{100} \text{ (Table IV).}$$

$$\frac{N}{50} = \frac{\text{mol. wt.}}{50} \rightleftharpoons \frac{\text{mol. wt.} \times 2}{100} \text{ (Table IV).}$$

$$\frac{N}{100} = \frac{\text{mol. wt.}}{100} \text{ (Table III).}$$

SOLUTIONS OF SODIUM CARBONATE OF CERTAIN NORMALITIES

$$\begin{aligned}
 N &= \frac{\text{mol. wt.}}{2} \approx \frac{\text{mol. wt.} \times 5}{10} \text{ (Table IV).} \\
 \frac{N}{5} &= \frac{\text{mol. wt.}}{2 \times 5} \approx \frac{\text{mol. wt.}}{10} \text{ (Table III).} \\
 \frac{N}{10} &= \frac{\text{mol. wt.}}{2 \times 10} \approx \frac{\text{mol. wt.} \times 5}{100} \text{ (Table IV).} \\
 \frac{N}{25} &= \frac{\text{mol. wt.}}{2 \times 25} \approx \frac{\text{mol. wt.} \times 2}{100} \text{ (Table IV).} \\
 \frac{N}{50} &= \frac{\text{mol. wt.}}{2 \times 50} \approx \frac{\text{mol. wt.}}{100} \text{ (Table III).} \\
 \frac{N}{100} &= \frac{\text{mol. wt.}}{2 \times 100} \approx \frac{\text{mol. wt.} \times 5}{1000} \text{ (Table IV).}
 \end{aligned}$$

TABLE V

REDUCTION OF COMPOUNDS FOUND TO CONSTITUENTS
SOUGHT BY MULTIPLICATION

This table is intended to aid in calculations connected with the analysis of mineral substances, where it is so frequently necessary to determine a given substance in a state of combination different from that the proportionate amount of which we wish to know. If, for example, we wish to determine the amount of barium a given substance contains, we should probably precipitate it and weigh it as barium sulphate and from this weight calculate the barium as follows:

$$\begin{aligned}
 &\text{mol. wt. BaSO}_4 : \text{at. wt. Ba} :: \text{wt. BaSO}_4 : \text{wt. Ba.} \\
 &\frac{\text{at. wt. Ba}}{\text{mol. wt. BaSO}_4} \times \text{wt. BaSO}_4 = \text{wt. Ba.}
 \end{aligned}$$

The constituent sought, in this case barium, is given in the first column of the table, and the state of combination in which it is convenient to determine the substance, barium sulphate, is given in the second column. On the same horizontal line with BaSO₄ a factor is given which is the quotient resulting from the division of the atomic weight of barium by the molecular weight of barium sulphate, so that it is only necessary to add to the logarithm of this factor the logarithm of the actual weight of barium sulphate in order to obtain the logarithm of the required weight of barium.

From the above it is plain that the factors express the actual weight of substance sought, contained in, or equivalent to one gram of substance found; that is, the first term of the proportion is reduced to unity, the second term

is expressed by the factor, the third term is the weight of substance found. By multiplying the second and third terms together the product expresses the weight of substance sought.

(2) In analyzing orthoclase feldspar the potassium and sodium are separated from the rest of the constituents and weighed together as chlorides. The potassium is then separated from the sodium in the usual manner and weighed as K_2PtCl_6 . It is customary to express the results of such analyses in percentages K_2O and Na_2O . From the weight of combined chlorides and the weight of K_2PtCl_6 the weights of K_2O and Na_2O are calculated as follows:

$$\begin{aligned} \text{mol. wt. } K_2PtCl_6 : \text{chem. equiv. wt. } K_2O &:: \text{wt. } K_2PtCl_6 : \text{wt. } K_2O. \\ \text{wt. } K_2PtCl_6 \times 0.19383 \text{ (factor)} &= \text{wt. } K_2O. \\ \text{mol. wt. } K_2PtCl_6 : \text{chem. equiv. wt. } KCl \text{ (2 KCl)} &:: \text{wt. } K_2PtCl_6 : \text{wt. } KCl. \\ \text{wt. } K_2PtCl_6 \times 0.30683 \text{ (factor)} &= \text{wt. } KCl. \\ \text{wt. of combined chlorides} - \text{wt. } KCl &= \text{wt. } NaCl. \\ \text{chem. equiv. wt. } NaCl \text{ (2 NaCl)} : \text{mol. wt. } Na_2O &:: \text{wt. } NaCl : \text{wt. } Na_2O. \\ \text{wt. } NaCl \times 0.53028 \text{ (factor)} &= \text{wt. } Na_2O. \end{aligned}$$

CALCULATION OF INDIRECT ANALYSIS

Let us suppose that we have a mixture of a chloride and a bromide, and that we wish to determine the chlorine and the bromine. The weight of silver which is equivalent to the combined halogens is determined by the Volhard method. Then the precipitated $AgCl$ and $AgBr$ are collected and weighed together.

Let $x = \text{wt. } AgCl$,
 and $y = \text{wt. } AgBr$.
 Then $x + y = a$ (wt. of $AgCl + AgBr$),
 and $\frac{Ag}{AgCl}x + \frac{Ag}{AgBr}y = b$ (wt. Ag equiv. to Cl and Br).
 As $\frac{Ag}{AgCl}$ and $\frac{Ag}{AgBr}$ are constant quantities, we may represent them by k and k' respectively. The equations then become

$$\begin{aligned} x + y &= a, \\ kx + k'y &= b. \end{aligned}$$

Multiplying the first equation by k and subtracting the second from it in order to eliminate x , we have

$$\begin{aligned} kx + ky &= ka, \\ kx + k'y &= b, \\ (k - k')y &= ka - b, \\ y &= \frac{ka - b}{k - k'}. \end{aligned}$$

As $k - k'$ is a single constant we have $y = \frac{ka - b}{K}$. By substituting the value thus obtained for y in the first equation we have $x = a -$ value of y .

$$\text{wt. AgCl} \times 0.24737 = \text{wt. Cl.}$$

$$\text{wt. AgBr} \times 0.42555 = \text{wt. Br.}$$

The values of $\frac{\text{Ag}}{\text{AgBr}}$ and $\frac{\text{Ag}}{\text{AgCl}}$ are given in Table V under Ag and opposite AgBr and AgCl respectively.

TABLES VI-IX

Normal atmospheric pressure is equal to the pressure exerted at sea level and 45° latitude by a vertical column of pure mercury 760 mm. long, the temperature of which is zero degrees C.

Barometric readings made under ordinary conditions must be reduced to standard conditions; that is, corrections must be applied for temperature, latitude, and elevation.

Temperature corrections. In view of the fact that the cubical expansion of mercury is much greater than that of glass, and the length of the barometer scale also changes with the temperature, it is necessary to consider all of these factors in making the temperature corrections. However, these have been combined and the values are given in Table VI.

Latitude corrections. Gravity at 45° latitude and sea level is considered normal. The values of this force in other latitudes as compared with the normal, taken as unity, are given in Table VII for a few important places. The length a barometric column of any latitude would have if it were acted upon by normal gravity may be calculated by multiplying the observed reading by that fraction which the force of gravity at the latitude in question is of normal gravity, or the proper correction may be taken from Table VIII, A.

Elevation corrections. These are necessary, because gravity diminishes as we proceed from the center of gravity of the earth (Table VIII, B).

Capillary depression corrections. Manufacturers of straight barometers make due allowance, in the adjustment of the scale, for capillary depression of the mercury; and in U-shaped barometers and manometers the forces on the two surfaces compensate, provided the mercury is of uniform purity and the arms are of the same diameter. However, there are other purposes for which the values of the capillary depression of mercury may be needed, and they are given in Table IX.

TABLES XII AND XIII

REDUCTION OF GAS VOLUMES TO NORMAL CONDITIONS OF
PRESSURE AND TEMPERATURE

Boyle's Law. The volume of a given mass of any gas varies inversely as the pressure upon it, provided the temperature remains constant.

If v represents the volume of a given mass of gas at 760 mm. pressure, and v_1 any other volume of the same mass at the pressure h , then $760 v = h v_1$, and $v = \frac{h}{760} v_1$.

In order to calculate the volume any given amount of gas would have if it existed under normal pressure, we have only to add to the logarithm of the observed volume the logarithm of the value of $\frac{h}{760}$, taken from Table XII. The sum will be the logarithm of the required volume.

Moist gases are assisted in sustaining the pressure of the atmosphere by the partial pressure of water vapor. Therefore, in order to find the pressure which the gas itself is actually exerting (which is equal to the pressure under which it exists in equilibrium), we must subtract from the pressure of the atmosphere the aqueous tension.

If the volume of a gas cannot be measured under exactly atmospheric pressure, it is frequently convenient to determine its pressure by measuring the difference between it and that of the atmosphere by means of an open arm manometer. The pressure of the atmosphere is then altered by the amount of this difference in order to ascertain the pressure under which the gas exists. The pressure which the gas alone exerts is represented by h of Table XII.

Charles's Law. The volume of any gas increases by $\frac{1}{273}$ part of its volume at 0°C . for every degree its temperature increases.

If V_t is the volume of a gas at the temperature t , we have

$$V_t = V_0 + V_0 \times 0.00367 t = V_0(1 + 0.00367 t); \text{ then } V_0 = \frac{1}{1 + 0.00367 t} \times V_t.$$

The values of $\frac{1}{1 + 0.00367 t}$ are given in Table XIII for temperatures ranging from 0° to 149° .

To calculate the volume a given amount of gas would have if its temperature were reduced to zero, we have to add to the logarithm of the observed

volume the logarithm of the value of $\frac{1}{1 + 0.00367 t}$ (Table XIII). The sum will be the logarithm of the required volume.

We may combine the expressions given above if we wish, as is usually the case, to reduce the volume to standard conditions of both pressure and temperature, thus

$$V_{0^{\circ}, 760 \text{ mm.}} = \frac{h}{760} \times \frac{1}{1 + 0.00367 t} \times V_{t^{\circ}, h \text{ mm.}}$$

These reductions may be summed up as follows: Correct the barometric reading for temperature, latitude, and elevation. Subtract from the corrected reading the tension of aqueous vapor, and apply the manometer correction, if there be one. The result is the value represented by h . Add to the logarithm of the observed volume, the logarithm of $\frac{h}{760}$ (Table XII) and of $\frac{1}{1 + 0.00367 t}$ (Table XIII). The sum will be the logarithm of the required volume.

TABLE XIV

This table is intended to minimize the labor of reducing the volume of moist gases to normal conditions and dry. It is assumed that the temperature of the barometer and of the gas and water over which the gas is measured is the same. Under this condition the barometric reading is corrected for temperature, the tension of aqueous vapor subtracted, and the resulting value of $\frac{h}{760}$ combined with $\frac{1}{1 + 0.00367 t}$ for certain combinations of temperature and pressure.

Take from the table the logarithm corresponding to the temperature and approximate pressure. Interpolate to find the logarithm corresponding to the exact pressure, and add to it the logarithm of the observed volume of the gas. The sum will be the logarithm of the volume under normal conditions and dry.

TABLE XV

If one wishes to know the weight of an observed volume of gas, as in the analysis of nitrogenous organic substances by the Dumas method, the volume should be reduced to standard conditions, and then to the logarithm of this volume add the logarithm of the weight of one liter of the gas, taking care to express the volume read off as a fraction of a liter.

TABLE XXVIII

BUOYANCY OF AIR

In view of the fact that the buoyant effect of the atmosphere changes considerably and often rapidly, it is necessary in work where great accuracy is required to reduce the apparent weight of a substance to a vacuum standard.

If d is the weight of 1 cc. of air and v the volume of the object weighed, the true weight is $w + vd$, where w is the apparent weight.

If the specific gravity of the substance is known, its volume is calculated by dividing its weight by the specific gravity. The error introduced by using the apparent weight instead of the true weight in the expression $v = \frac{w}{s}$ is negligible. Therefore the true weight of a substance is $w + \frac{w}{s}d$.

If we wish to obtain absolute weighings, the same kind of correction must be applied to the weights. For brass weights ($s = 8.3$) the correction is 0.000145 per gram. This correction is negative and is to be subtracted from the calculated true weight of the substance.

The true, absolute weight, then, of a substance weighed in air with brass weights is $w_0 = w \left(1 + \frac{d}{s} - 0.000145 \right)$.

The values of d (Table XVI) are calculated for 760 mm. pressure. In work where the greatest accuracy possible is required, the value of d must be reduced to the existing condition of pressure; namely, $d \times \frac{h}{760}$.

In many instances, however, it is sufficiently accurate to consider d constant and equal to 0.0012 g. at room temperature. Under this condition the above expression becomes

$$w_0 = w \left(1 + \frac{0.0012}{s} - 0.000145 \right) = w(1 + c). \quad (\text{See Table XXVIII.})$$

THE COMMON SYSTEM OF LOGARITHMS

This system of logarithms is in general use because it greatly abridges numerical computation, and with due care arithmetical errors are largely eliminated.

The logarithm of a number is the exponent of the power to which it is necessary to raise a fixed number, in order to produce the first number.*

* The definition is based upon the assumption that there always exists a real number x which satisfies the equation $b^x = a$, where a and b are positive numbers and b is greater than 1.

The base of the common system is 10, and since

$10^0 = 1$	$10^{-1} = 0.1$
$10^1 = 10$	$10^{-2} = 0.01$
$10^2 = 100$	$10^{-3} = 0.001$
$10^3 = 1000$	$10^{-4} = 0.0001$

it follows from the definition of a logarithm that

$\log 1 = 0$	$\log 0.1 = -1$
$\log 10 = 1$	$\log 0.01 = -2$
$\log 100 = 2$	$\log 0.001 = -3$
$\log 1000 = 3$	$\log 0.0001 = -4$

It is quite evident from the above table that the logarithms of all numbers between 0 and 1 are negative and that the logarithms of all numbers greater than 1 are positive.

NOTE. A negative number is considered as having no logarithm.

We see also that the logarithm of any number between 1 and 10 is greater than 0 and less than 1; thus

$$\log 2.71 = 0.432969.$$

The logarithm of any number greater than 10 and less than 100 is greater than 1 and less than 2; thus

$$\log 26. = 1.414973.$$

It is plain that if a number is not an exact power of 10, its logarithm must consist at least in part of a decimal fraction.

It is true that such logarithms can be expressed only approximately, but if the fractions are given to six places, they are sufficiently accurate for even the best atomic weight work.

The integral part of a logarithm is called the characteristic, and the decimal part the mantissa. In the case just given 1 is the characteristic and .414973 the mantissa of the log 26.

To find the characteristic of the logarithm of a number:

(a) When the number is greater than unity, the characteristic of its logarithm is one less than the number of digits to the left of the decimal point. Thus the characteristic of the logarithm of 46783.85 is 4.

(b) When the number is less than unity, subtract from 9 the number of ciphers between the decimal point and the first significant figure, writing -10 after the mantissa. Thus the characteristic of the logarithm of 0.00089 is 6 with -10 written after the mantissa: $\log 0.00089 = 6.949390 - 10$.

Some prefer to combine the two parts of such characteristics, writing the result as a negative characteristic, in which case it is one greater than the number of zeros preceding the first significant figure. The minus sign is written above the characteristic to show it applies only to it, for in constructing logarithmic tables it is convenient to make all mantissas positive even if the logarithm is a negative number. For example, $\log \frac{1}{4} = -0.602060$; but since $-0.602060 = -1 + .397940$, this may be written $\log \frac{1}{4} = \bar{1}.397940$ or $9.397940 - 10$ with a positive mantissa. In order to avoid complications it is best to adhere to the first form of expression mentioned under (b); that is, when a logarithm has a negative characteristic to add 10 to and subtract 10 from it. For example, instead of writing the logarithm $-1 + .397940$, or $\bar{1}.397940$, we should write $+10 - 1 + .397940 - 10 = 9.397940 - 10$. This is convenient when we wish to divide a logarithm by a number. Since mantissas are always positive, it would not be correct to divide $\bar{1}.397940$ by 2, as we should confuse the positive and negative parts. If the form $9.397940 - 10$ is used, the confusion is avoided, and the result of the division by 2 is $4.698970 - 5 = \bar{1}.698970$, the actual logarithm resulting from the division.

TABLE OF LOGARITHMS

The great value of the common system of logarithms for the purposes of the analytical chemist is due to the fact that short tables can be constructed which contain the mantissas of the logarithms of all numbers from 1 or 100 to some given number, generally 1000 or 10,000, this being sufficient to cover all cases, and the characteristics can be determined by inspection.

In order to use a table of logarithms one must know how to find the logarithm of any number, and how to take from the table the number which has a given logarithm, and also how to point the numbers off.

To find from the table the logarithm of any number:

(a) When the number consists of two significant figures.

All of these numbers are given on the first page of the table in columns marked *N*. The logarithm of each number is placed opposite the number.

(b) When the number consists of three or four significant figures.

Find in the column of numbers the first three significant figures of the given number, then glance across the page along a horizontal line to the column under the fourth figure of the given number; four figures of the required mantissa are given at this point, to which two figures taken from the zero column must be prefixed. If the four figures of the required mantissa are

opposite a row of six figures in the zero column, the first two of the six are to be prefixed; but if they are opposite only four figures in the zero column, the two figures to be prefixed will be found above, unless in passing back to the zero column asterisks be met with, in which case the two figures will be found immediately below the horizontal line in the zero column. Zeros should be written wherever asterisks occur. Characteristics are then prefixed in accordance with the rules already given.

Examples: $\log 106 = 2.025306$

$\log 1264 = 3.101747$

$\log 2041 = 3.309843$

$\log 2042 = 3.310056$

$\log 2048 = 3.311330$

(c) When the number consists of more than four significant figures.

The mantissas of the logarithms of these numbers are not to be found in the table, but they can be easily calculated from values given in the table by a process of interpolation. The principle of proportional parts assumes that for a small change in a number there corresponds a proportional change in the logarithm. This is not strictly true, but the approximation is sufficiently close for most purposes.

For example, required the $\log 521257$. We find from the table $\log 5212 = 3.717004$ and $\log 5213 = 3.717088$. That is, an increase of one unit in the fourth figure produces an increase of .000084 in the logarithm. Therefore an increase of .57 of this unit will produce an increase in the logarithm equal to $.57 \times .000084$, or .000048. Hence $\log 521257 = 3.717052$.

NOTE. In order to facilitate the process of interpolation it is customary to give the differences between the logarithms of consecutive numbers of four figures in a separate column. Such numbers are called tabular differences. In the table one number is given at the end of each horizontal line, and in each case it is nearly a mean of the differences of any two logarithms on the same line. It is intended that these numbers should serve only as a guide, and the last figure should be checked in every instance by glancing at the logarithms involved.

The following rule is derived from the above: Place a decimal point after the fourth significant figure from the left, converting the given number into a whole number and a fraction, and this irrespective of any decimal point that may occur in the given number.* Find from the table the mantissa

* Numbers with the same sequence of figures and which differ only in the position of the decimal point have the same mantissa, for one is the product of the other and an integral power of 10; hence their logarithms differ only by integers. Therefore the mantissa of the common logarithm of a number is independent of the decimal point.

of the entire part and multiply the decimal part by the tabular difference; add the product thus obtained to the mantissa of the entire part and prefix the proper characteristic, determined with respect to the position of decimal point in the original number.

To find from the table the number which corresponds to a given logarithm:

(a) Required the number the logarithm of which is 1.874772. We find this exact mantissa given in the table, and opposite in the column of numbers we find 749, the first three figures of the required number, and at the head of the column 5 the fourth figure.

(b) Required the number the logarithm of which is 2.137860. The mantissa of this logarithm is not given in the table, but it lies between the two mantissas .137671 and .137987, and the numbers corresponding to these are 1373 and 1374 respectively. The difference between the two mantissas taken from the table is 316, and the difference between the given mantissa and the smaller of the two taken from the table is 189; that is, an increase of 316 in the mantissa produces an increase of one unit in the corresponding number. Therefore an increase of 189 in the smaller of the two mantissas taken from the table will produce an increase of $\frac{189}{316}$ of a unit in the corresponding number. Hence the required number is 137.359 nearly.

The following rule is derived from the above:

Search in the table for the mantissa of the given logarithm, and if it cannot be found, set aside the number corresponding to the next less mantissa. Subtract this mantissa from that of the given logarithm and divide the remainder by the tabular difference, carrying the division as far as desirable. Annex the quotient to the number set aside, and point off from the left one more integer figure than there are units in the characteristic of the given logarithm. If the characteristic is negative, the number is less than 1, and the number of zeros to be placed before the first figure is one less than the number of units in the characteristic.

MULTIPLICATION BY LOGARITHMS

Find from the table the logarithms of all the numbers to be multiplied together. Add these algebraically, remembering that negative signs apply only to the characteristic. The sum is the logarithm of the product.

Thus multiply 27.1 by 119.86.

$$\begin{array}{r} \log 27.1 = 1.432969 \\ \log 119.86 = 2.078674 \\ \hline 3.511643 = \log \text{ of product} \end{array}$$

The number of which this is the logarithm is 3248.201.

DIVISION BY LOGARITHMS

Find the logarithm of the dividend and subtract from it the logarithm of the divisor. The difference is the logarithm of the quotient. The word "difference" is used here in its algebraic sense. That is, if the characteristic of the logarithm of the divisor is negative, its sign must be changed; but if that of the dividend is negative, it must be treated as a negative quantity. Let it be said once more that mantissas without exception are positive.

1. To divide 100.07 by 56.07.

$$\begin{array}{r} \log 100.07 = 2.000304 \\ \log 56.07 = \underline{1.748731} \\ 0.251573 = \text{log of quotient} \end{array}$$

The number of which this is the logarithm is 1.78473.

2. To divide 107.87 by 0.0187779.

$$\begin{array}{r} \log 107.87 = 2.032901 \\ \log 0.0187779 = \underline{\bar{2}.273647} \\ 3.759254 = \text{log of quotient} \end{array}$$

The number of which this is the logarithm is 5744.5.

3. To divide 0.13736 by 153.36.

$$\begin{array}{r} \log 0.13736 = \bar{1}.137860 \\ \log 153.36 = \underline{2.185712} \\ 4.952148 = \text{log of quotient} \end{array}$$

The number of which this is the logarithm is .00089568.

In regard to involution and evolution it is only necessary to say that the logarithm of any power of a number is obtained by multiplying the logarithm of the number by the exponent of the power, and that the logarithm of any root of a number is obtained by dividing the logarithm of the number by the index of the root.

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